

Waters™



Philadelphia Short Course: Day II

## Section IV: DMA Theory and Instrumentation

*Terri Chen, PhD*

*Principal Application Scientist*

*TA Instruments – Waters LLC*

# DMA: An introduction

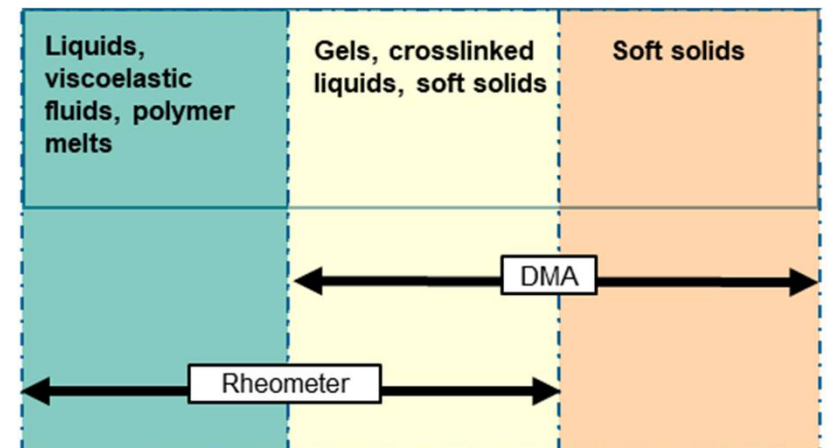
A Dynamic Mechanical Analyzer (DMA) measures the mechanical/rheological properties of a material as a function of time, frequency, temperature, stress, and strain.

## Typical materials tested on a DMA - Solids

- Thermoplastic and thermosets
- Elastomers/rubbers
- Gels
- Foams
- More....



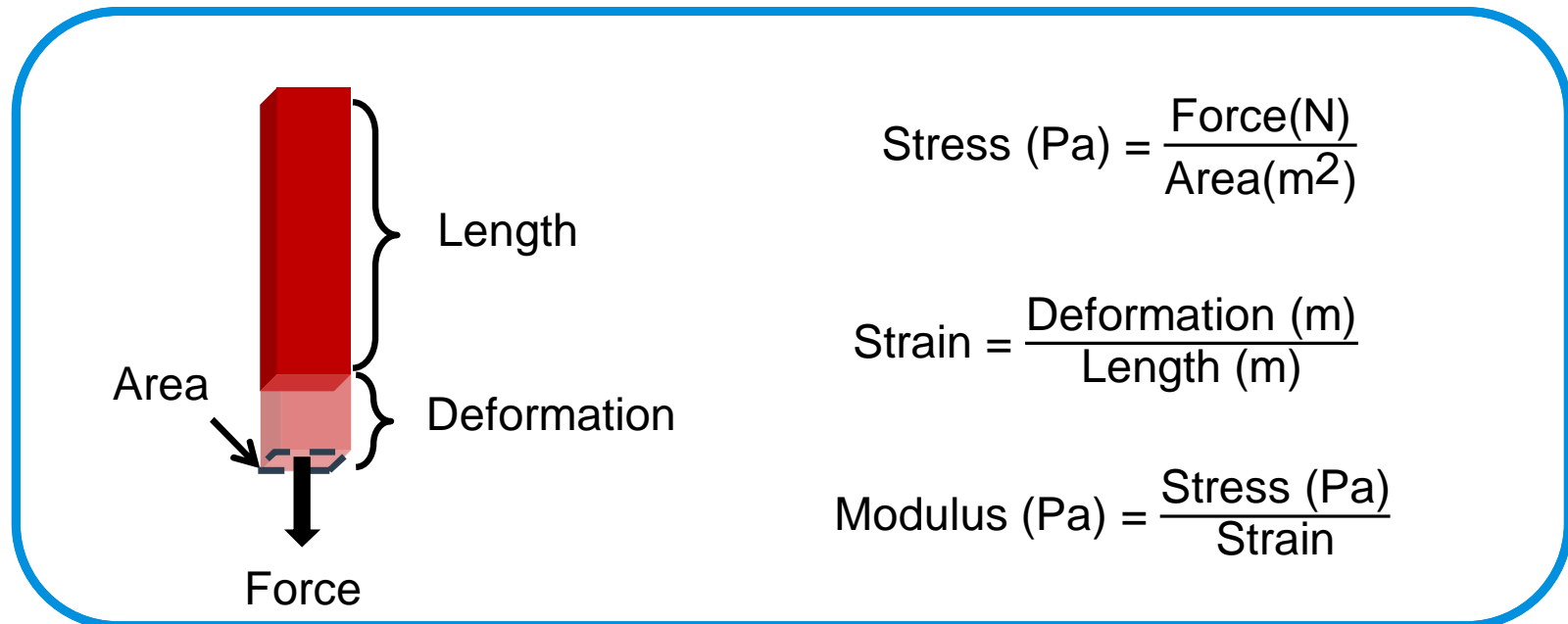
Rheology and DMA are complimentary  
DHR Rheometers can do both



# Working principle of DMA

Apply a **force** or a **deformation** to a sample, then measure the sample's response, which will be a **deformation** or a **force**.

All mechanical parameters (stress, strain, modulus, stiffness) are calculated from these 2 raw signals.

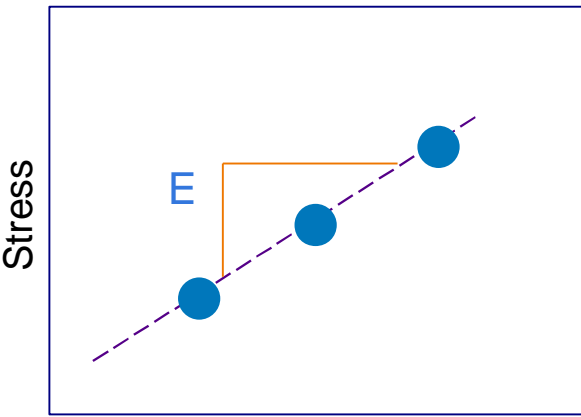


# Hook's law of elasticity, Newton's law of viscosity

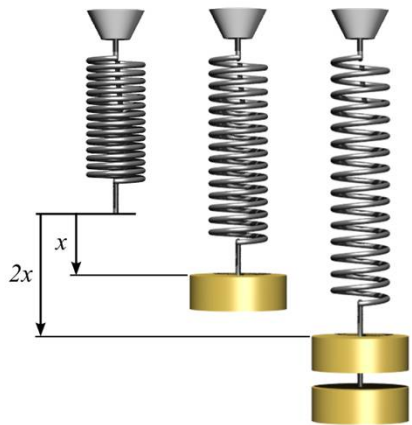
For a purely Elastic Solid, Stress and Strain have a constant proportionality

The slope of stress over strain is the Young's modulus of the material

$$\sigma = E^* \epsilon$$



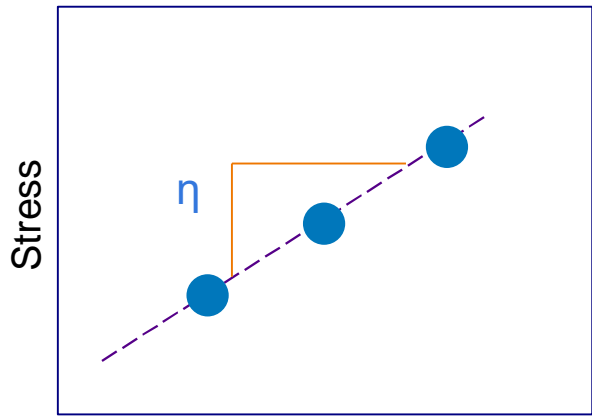
Strain



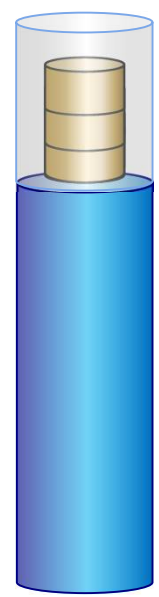
For a purely Viscous Liquid, Stress is proportional to Strain Rate  $d\epsilon/dt$

The slope of stress over strain rate is the viscosity of the material

$$\sigma = \eta^* \frac{d\epsilon}{dt}$$



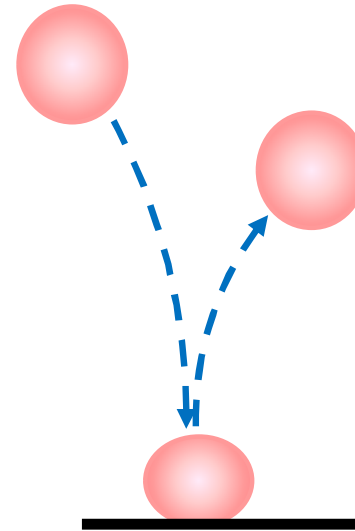
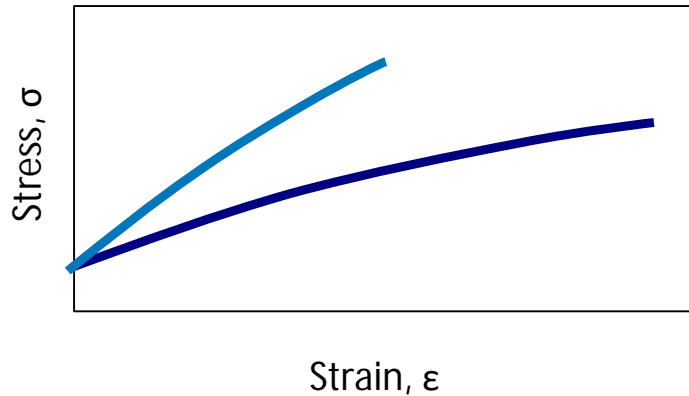
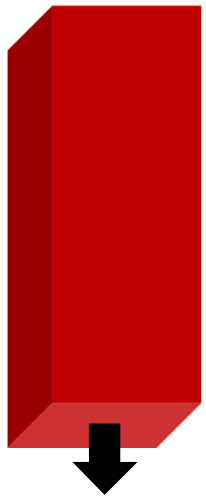
Strain rate



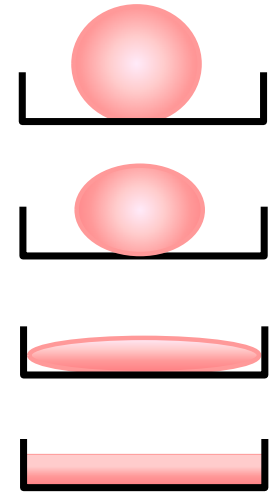
# Time dependency of viscoelastic materials

- In tensile testing of viscoelastic materials, the rate of extension will give different results
- the stress depends on both the strain, and the strain rate

$$\sigma = E \varepsilon + \eta \frac{d\varepsilon}{dt}$$

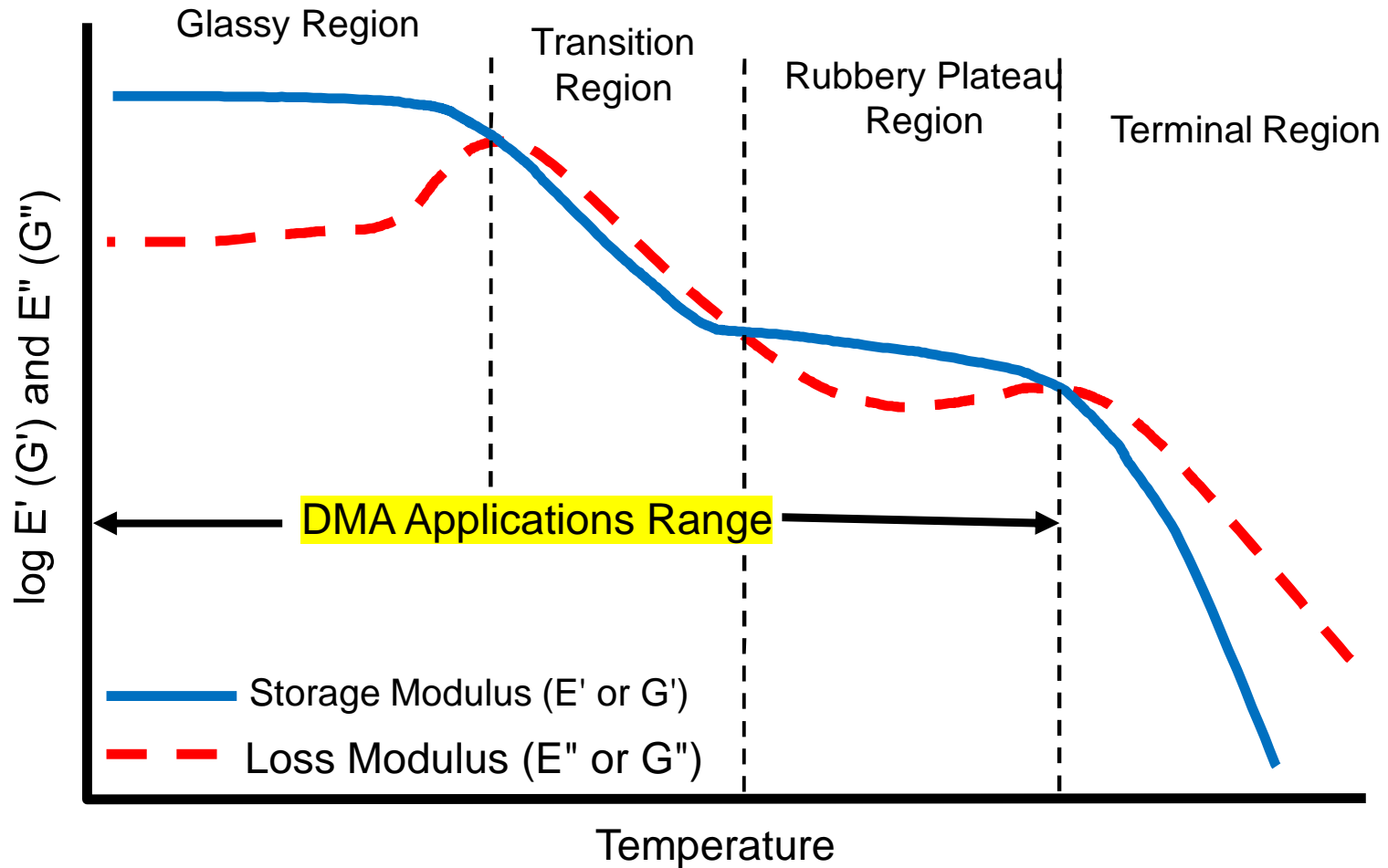


Fast deformation  
(high frequency)



Slow deformation  
(low frequency)

# Viscoelastic spectrum for an amorphous polymer



# DMA instrumentation

Discovery DMA850



RSA G2



Electroforce series



HR series








ARES G2



Standalone DMA

Rheometers with DMA mode

# DMA instrumentation – Load Cell and Sensitivity

Discovery DMA850	RSA G2 & ARES G2	HR 20 & 30 + DMA Mode	Electroforce series (high load frame, fatigue)
 <p data-bbox="357 950 441 990">18N</p>	 <p data-bbox="924 657 1008 698">35N</p>  <p data-bbox="924 950 1008 990">20N</p>	 <p data-bbox="1207 1055 1291 1096">50N</p>	 <p data-bbox="1638 1063 1732 1104">300N</p>

Load Cell Size (Maximum Force)



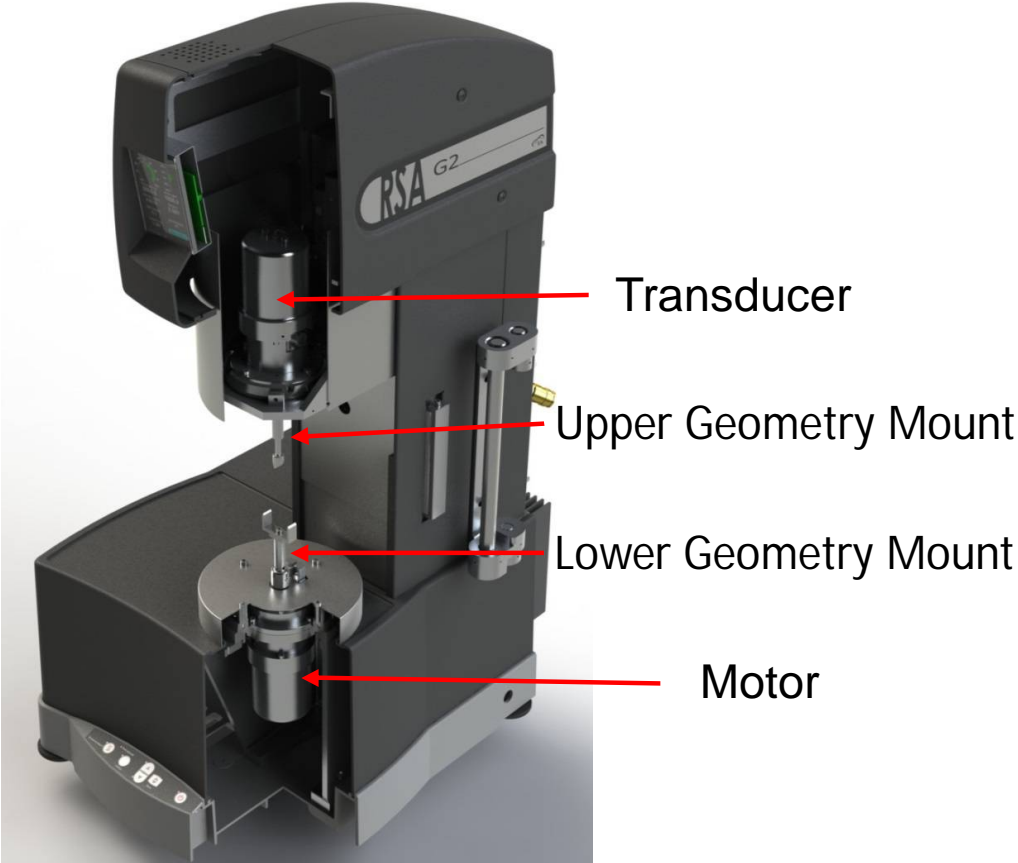
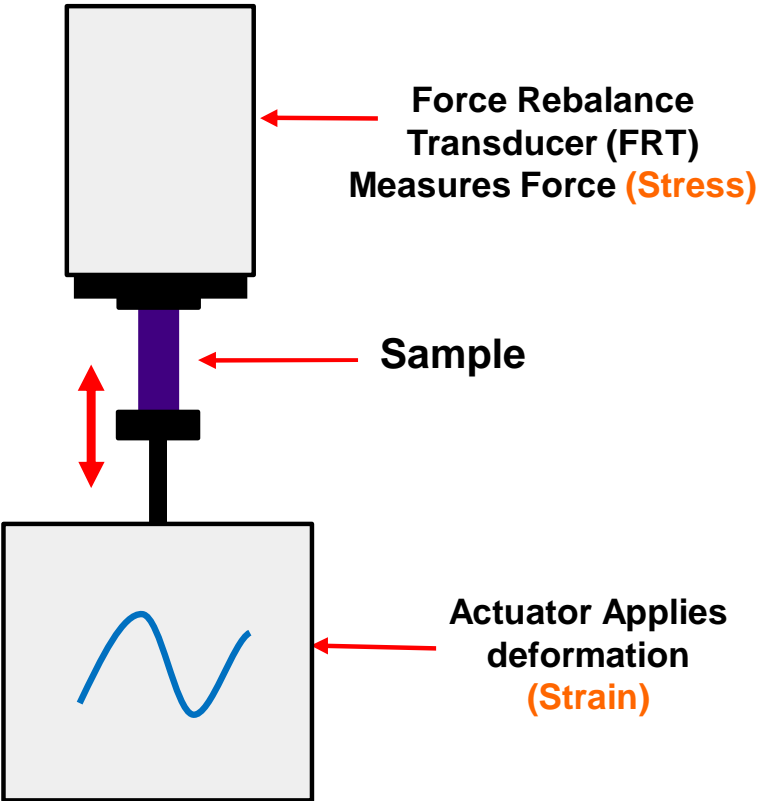
Load Cell Sensitivity (Force resolution & minimum force)





# Separate motor and transducer

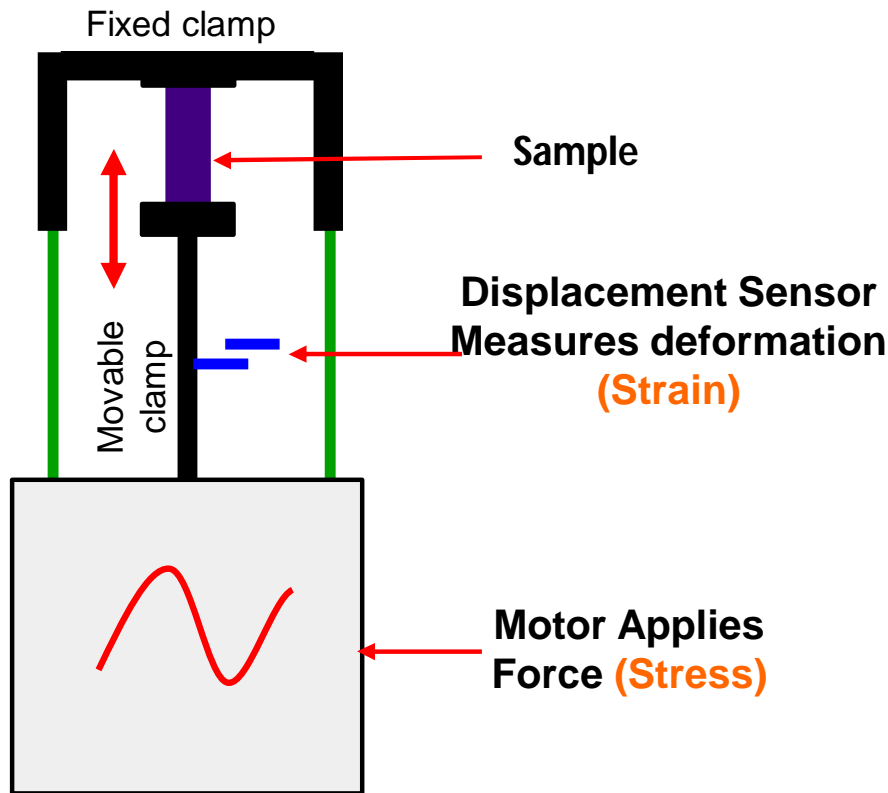
## RSA G2 Separate Motor & Transducer



# Combined motor and transducer

## DMA850

### Combined Motor & Transducer



# Instrument specifications

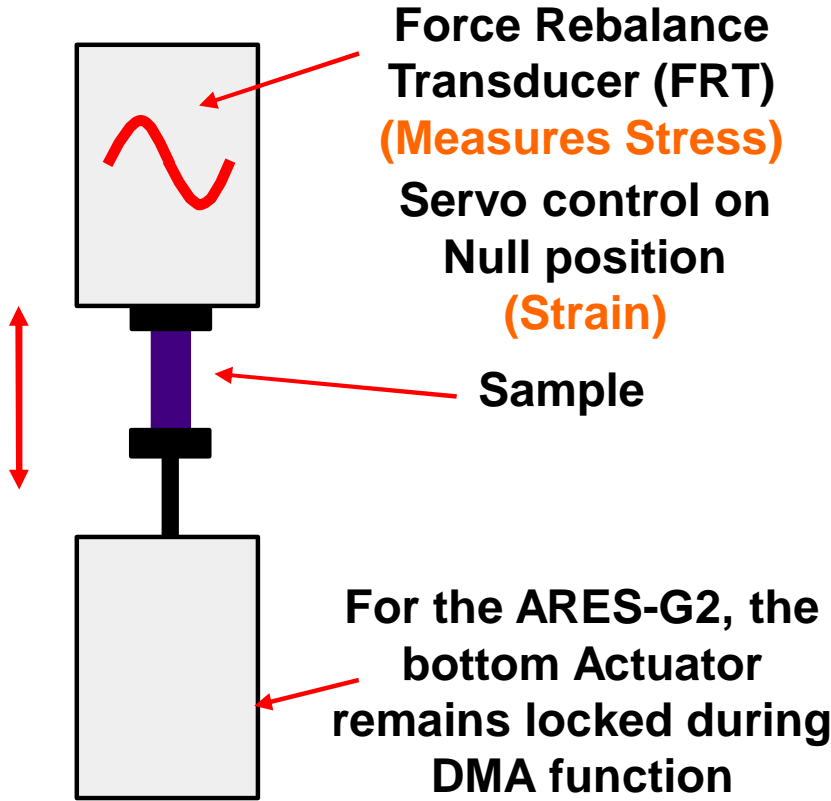
	RSA G2	DMA850
Max Force	35 N	18 N
Min Force	0.0005 N	0.0001 N
Displacement Resolution	1 nm	0.1 nm
Frequency Range	$2 \times 10^{-6}$ to 100 Hz	$1 \times 10^{-4}$ to 200 Hz
Dynamic Deformation Range	$\pm 5 \times 10^{-5}$ to 1.5 mm	$\pm 5 \times 10^{-6}$ to 10 mm
Temperature range	-150 to 600°C	-150 to 600°C
Isothermal Stability	$\pm 0.1$	$\pm 0.1$
Heating Rate	0.1°C to 60°C/min	0.1°C to 20°C/min
Cooling Rate	0.1°C to 60°C/min	0.1°C to 10°C/min

# DMA on TA rheometers

**ARES-G2**



**HR 20/30**

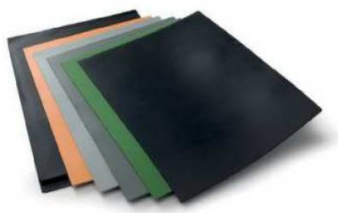


# Specifications of HR and ARES-G2 DMA mode

Parameter	HR20/30 DMA mode	ARES-G2 DMA mode
Motor Control	FRT	FRT
Minimum Force (N) Oscillation	0.003	0.001
Maximum Axial Force (N)	50	20
Minimum Displacement (μm) Oscillation	0.01	0.5
Maximum Displacement (μm) Oscillation	100	50
Axial Frequency Range (Hz)	1 x 10 <sup>-5</sup> to 16	1 x 10 <sup>-5</sup> to 16

# Samples tested on DMA

By changing the clamp, we can test a range of different materials



Elastomers



Films



Fibers



Gels



Plastics



Foams



Composites

# Popular DMA850 clamps

S/D Cantilever



Film/Fiber Tension



3-Point Bending



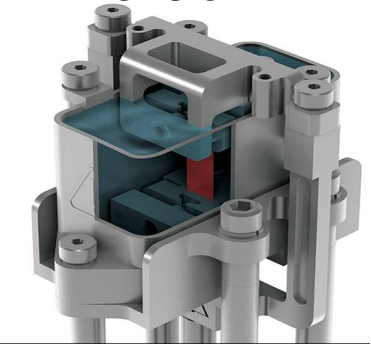
Compression



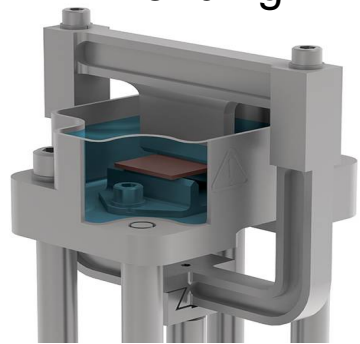
Shear Sandwich



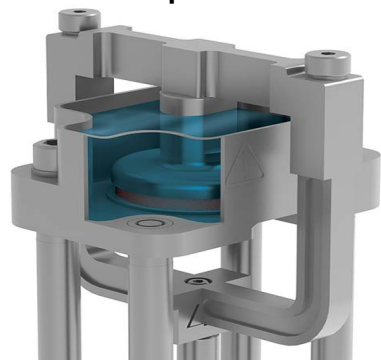
Submersible Tension



Submersible Bending



Submersible Compression



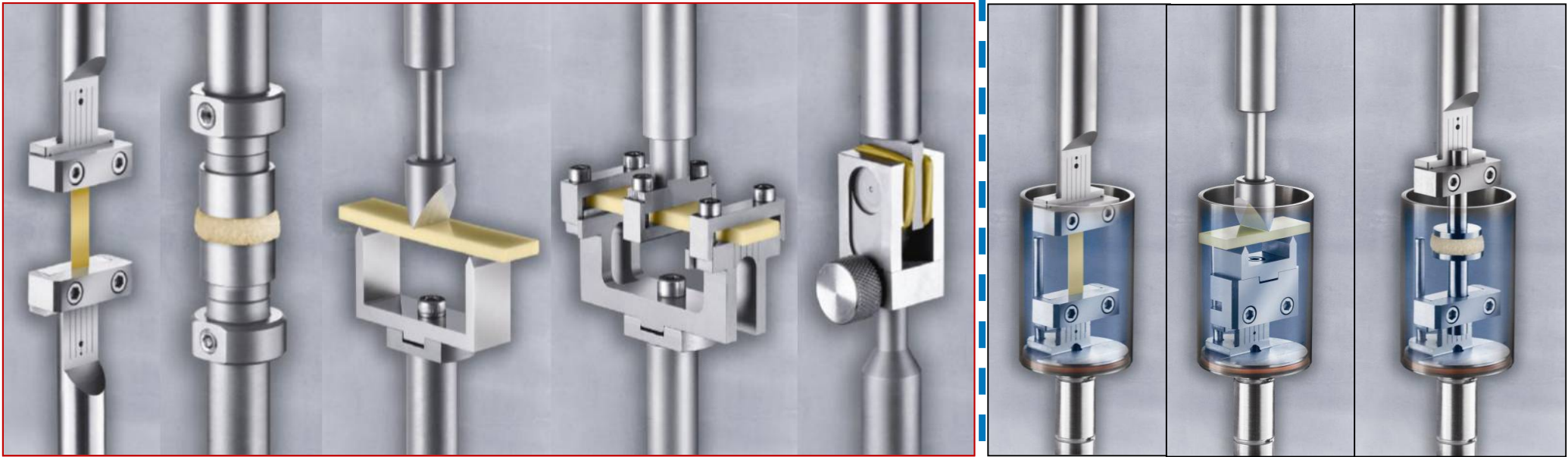
# Popular RSA G2 clamps

Tension

3-Point Bending

Shear Sandwich

3 Point Bending



Compression

S/D Cantilever

Tension

Compression

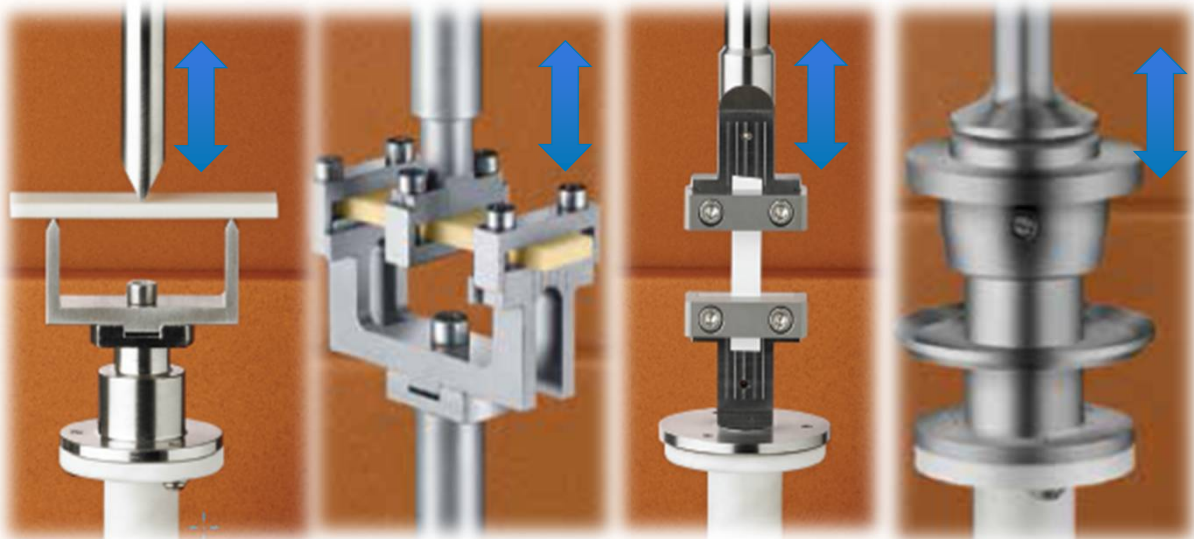
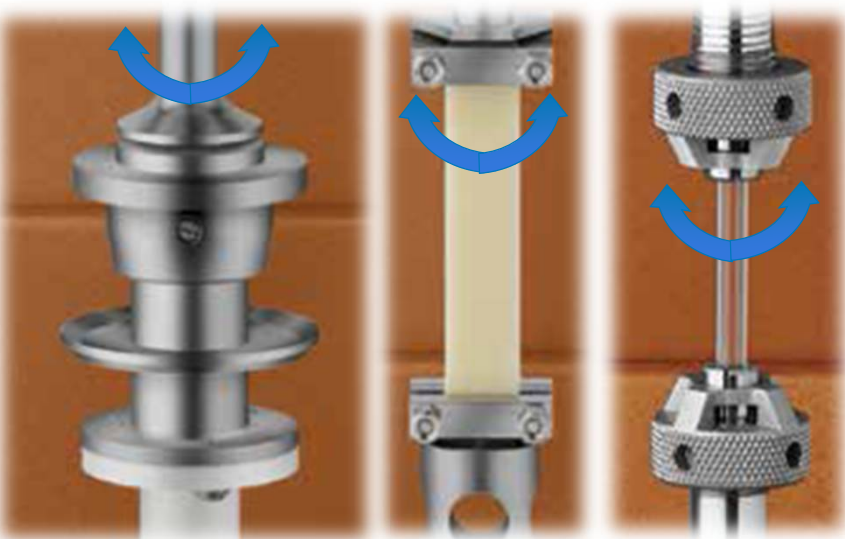


# Popular HR solid testing clamps

Torsion (rotational) and DMA (axial) geometries allow solid samples to be characterized in a temperature-controlled environment.

Shear Modulus:  $G'$ ,  $G''$ ,  $G^*$

Young's Modulus:  $E'$ ,  $E''$ ,  $E^*$



Parallel plate

Rectangular and cylindrical torsion

3-point bending

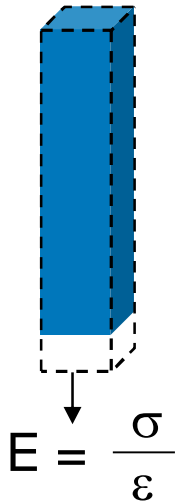
Cantilever

Tension

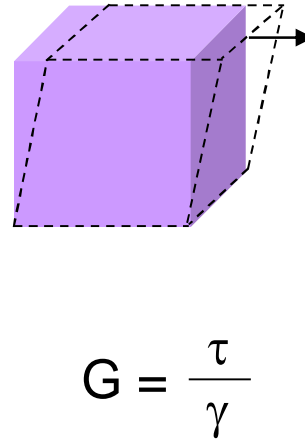
Compression

# Three fundamental modes of deformation

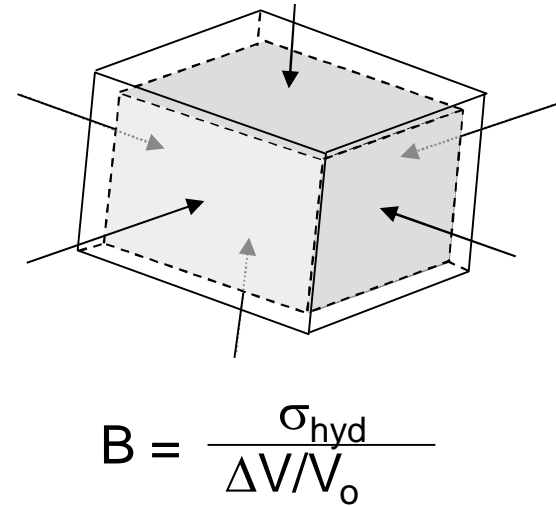
Young's  
Modulus



Shear  
Modulus



Bulk  
Modulus

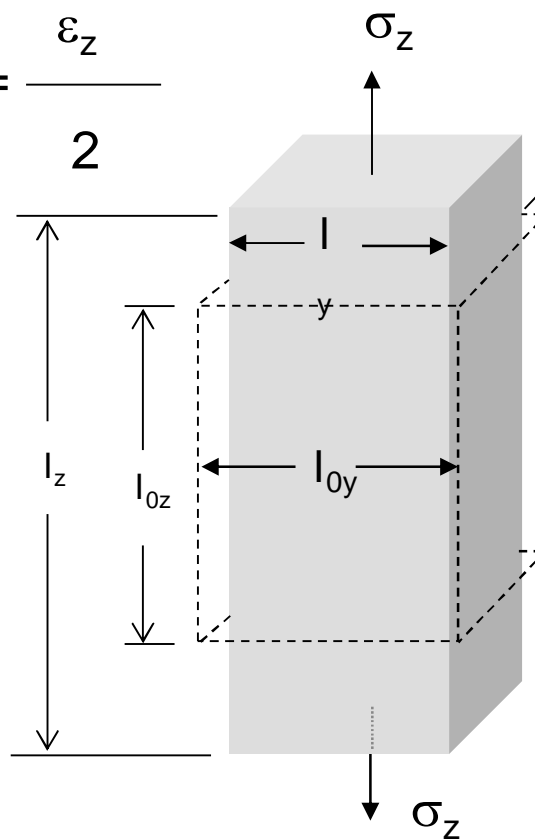


Where dashed lines indicate initial stressed state  
 $\sigma$  = uniaxial tensile or compressive stress  
 $\tau$  = shear stress  
 $\sigma_{\text{hyd}}$  = hydrostatic tensile or compressive stress  
 $\varepsilon$  = normal strain  
 $\gamma$  = shear strain  
 $\Delta V/V_0$  = fractional volume expansion or contraction

# Poisson's Ratio

- Poisson's ratio,  $\nu$ , is the ratio of transverse to axial strain

$$\frac{l_z - l_{0z}}{2} = \frac{\epsilon_z}{2}$$



$$\frac{l_y - l_{0y}}{2} = \frac{-\epsilon_y}{2}$$

Poisson's Ratio

$$\nu = \frac{-\epsilon_y}{\epsilon_z}$$

# Relationship between moduli and Poisson's ratio for an elastic isotropic materials

- Elastic Isotropic materials are materials in which properties at a point are the same in all directions. Some examples of isotropic materials are unoriented amorphous polymers and annealed glasses [1].
- If any of the two elastic constants of a homogenous (in which properties do not vary from point to point) isotropic material, the other two may be calculated [2].
- If the volume of the specimen remains constant when deformed (e.g., liquids or rubber) , then  $\nu = 0.5$ .
- In general, there is an increase in volume given by  $DV/V_0 = (1 - 2\nu)e$  where  $DV$  = increase in initial volume  $V_0$  caused by straining the sample.

$$E = 2G(1 + \nu) = 3B(1 + 2\nu)$$

1. Nielsen, Lawrence E., Mechanical Properties of Polymers and Composites, Marcel Dekker, Inc., New York, 1974, p. 1.

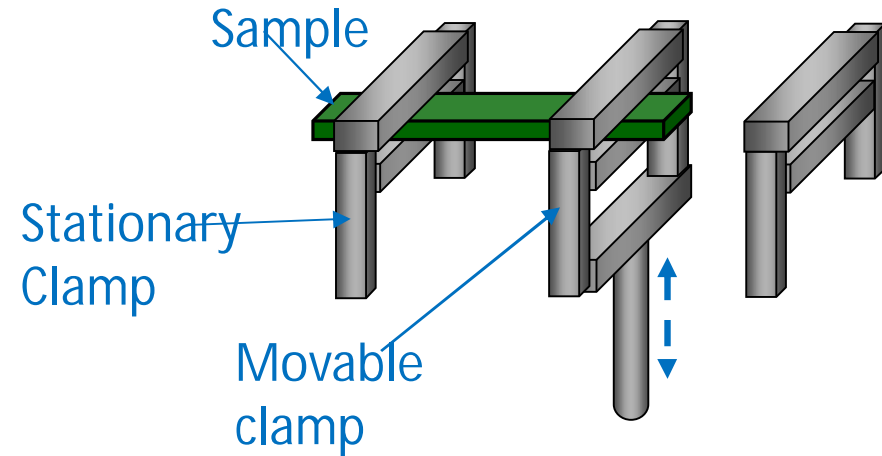
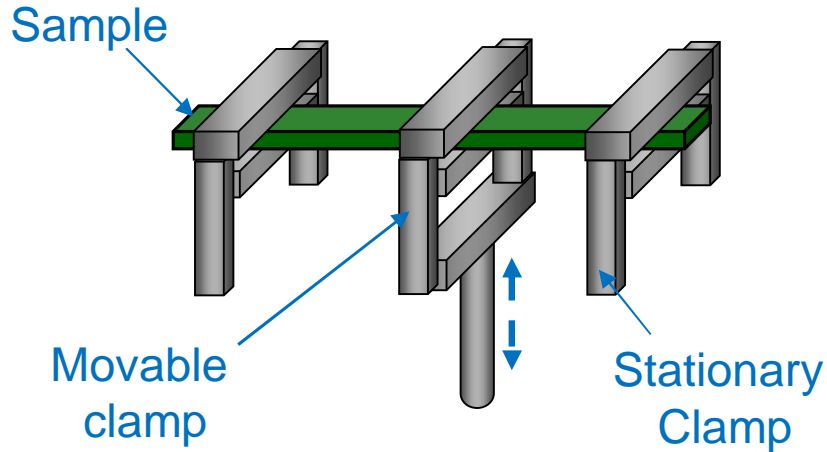
2. Hayden, H. W., Moffatt, W.G., and Wulff, J., The structure and Properties of Materials, Volume III, Mechanical Behavior, John Wiley & Sons, Inc, New York, 1965, p.26.

# Modulus calculations in DMA

DMA850 and Q800	RSA G2
<p>Stiffness (K) = Force / Displacement</p> <p>Modulus (E) = K x GF</p> <p>GF: Geometry factor. Clamp dependent Can be found in online help manual</p>	<p>Stress (<math>\sigma</math>) = Force x <math>K_{\sigma}</math></p> <p>Strain (<math>\gamma</math>) = Displacement x <math>K_{\gamma}</math></p> <p>Modulus (E) = <math>\sigma / \gamma</math></p> <p><math>K_{\sigma}</math>: Stress constant <math>K_{\gamma}</math>: Strain constant Clamp dependent Can be found in online help manual</p>

$$GF = K_{\sigma} / K_{\gamma}$$

# Cantilever clamps



Stiff samples with well-defined sample dimensions can be measured accurately.

- Soft samples (with  $T_g < RT$ ) such as elastomers may get pinched during clamping and cause errors in measurement.
- Samples with high CTE can expand between the clamp faces and buckle, causing significant errors in measurement

Tracking cure of thermosets/composites, mechanical properties, secondary transitions and  $T_g$  of polymers (thermoplastics/thermosets)

Measurement of modulus and  $\tan \delta$

# Dual cantilever clamp governing equations

Modulus = Stiffness × Geometry Factor (GF)

$$GF_{DC} = \frac{12 \cdot l^3 \left[ 1 + \frac{12}{5} (1 + \nu) \left( \frac{t}{l} \right)^2 \right]}{24wt^3}$$

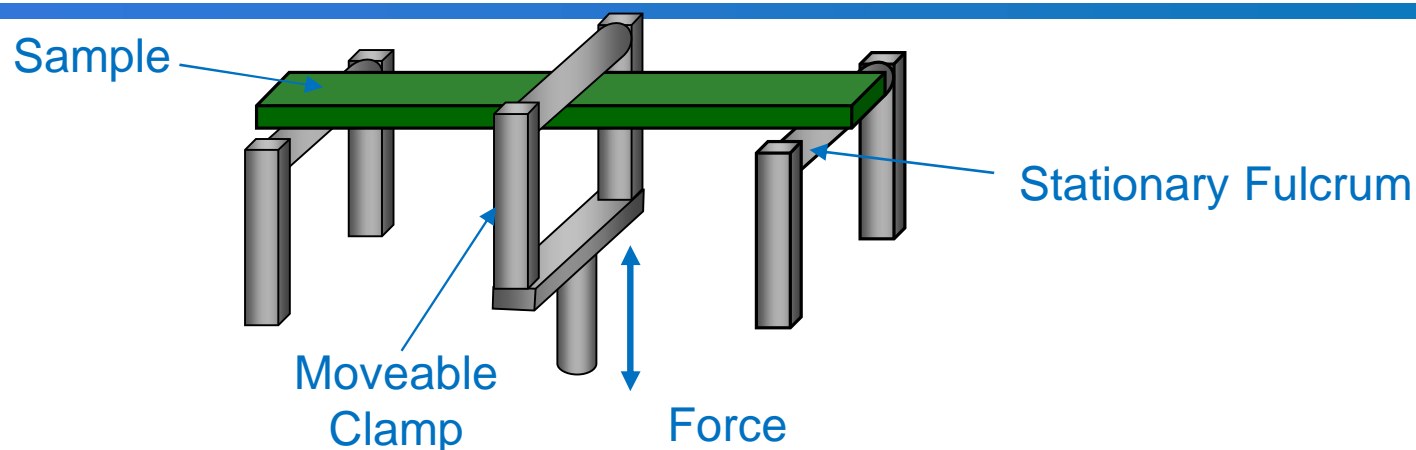
If length/thickness > 10, the contribution of the term containing the Poisson's Ratio can be approximated to be negligible

$$GF_{DC} = \frac{l^3}{2wt^3}$$

w = sample width  
l = sample length  
t = sample thickness

	To increase stiffness	To decrease stiffness
Dual cantilever	Decrease length or increase width. If possible, increase thickness. Note: L/T ≥ 10	Increase length or decrease width If possible, decrease thickness. Note: L/T ≥ 10

# 3-point bend clamp



Conforms with ASTM standard test method for bending

Purest deformation mode since clamping effects are eliminated

Stiff samples with well-defined sample dimensions can be measured accurately.

**Samples that get soft around  $T_g$  (typically unfilled thermoplastics) can sag and introduce errors in modulus measurements.**

Tracking cure of thermosets/composites, mechanical properties and  $T_g$  of polymers that are stiff past the glass transition (filled thermoplastics/thermosets/elastomers)

Measurement of modulus and  $\tan \delta$



# 3-point bend clamp governing equations

Modulus = Stiffness × Geometry Factor (GF)

$$GF_{3PB} = \frac{3l^3 \left[ 1 + \frac{6}{10}(1+\nu)\left(\frac{2t}{l}\right)^2 \right]}{12wt^3}$$

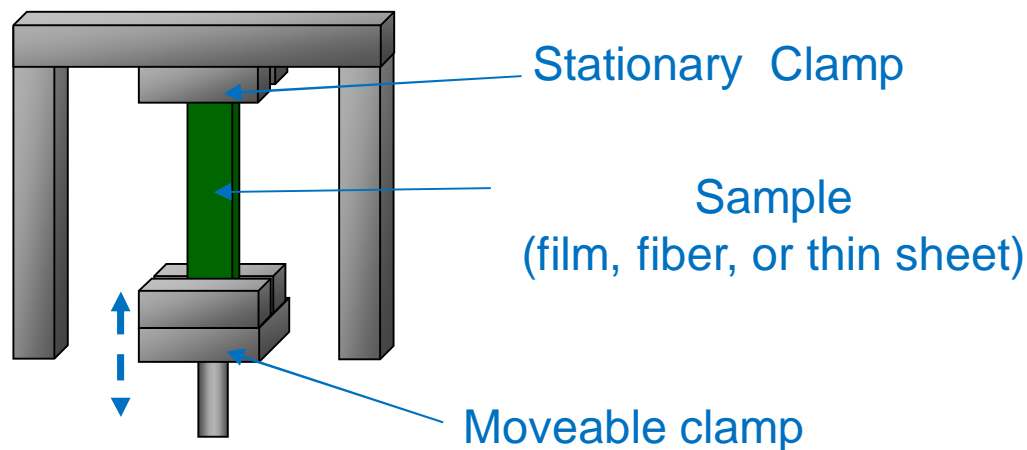
If length/thickness > 10, the contribution of the term containing the Poisson's Ratio can be approximated to be negligible

$$GF_{DC} = \frac{l^3}{4wt^3}$$

w = sample width  
l = sample length  
t = sample thickness

	To increase stiffness	To decrease stiffness
3-point bend	Decrease length or increase width. If possible, increase thickness. Note: L/T ≥ 10	Increase length or decrease width If possible, decrease thickness. Note: L/T ≥ 10

# Tension clamp



Films and fibers with well-defined sample dimensions can be measured accurately. Sample length is calculated automatically by the instrument.

## Applications

- Mechanical properties,  $T_g$ , secondary transitions (modulus and  $\tan \delta$ )
- Creep and stress relaxation
- Temperature-controlled constant force or displacement tests to understand processing effects and shrinkage
- Generation of stress-strain curves

# Tension clamp governing equations

Modulus = Stiffness × Geometry Factor (GF)

$$GF_{\text{Film}} = \frac{l}{wt}$$

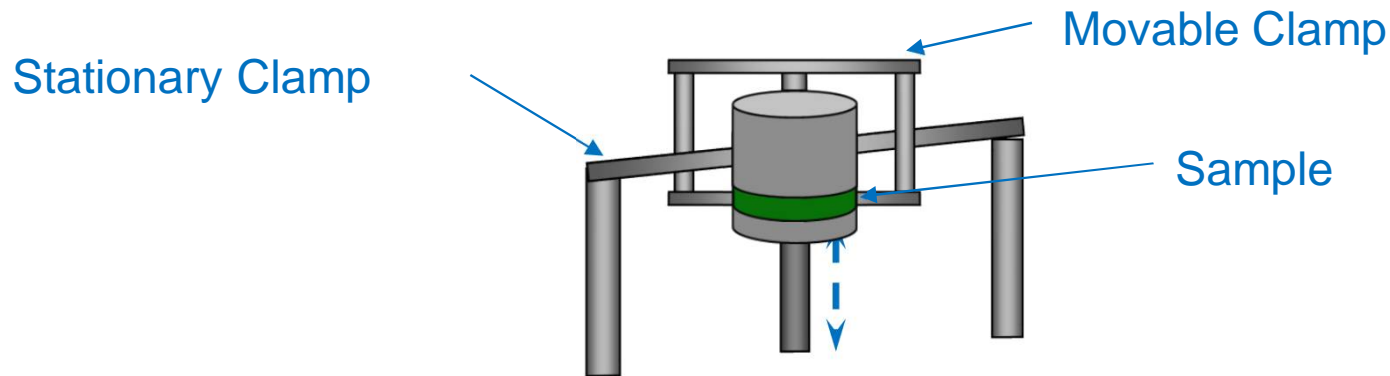
w = sample width

l = sample length

t = sample thickness

	To increase stiffness	To decrease stiffness
Tension	Decrease length or increase width. If possible, increase thickness.	Increase length or decrease width If possible, decrease thickness.

# Compression clamp



Good mode for low to medium modulus materials (gels, elastomers) which are compressible throughout the test temperature range

- Samples that are incompressible (typically below the  $T_g$ ) are difficult to test under compression
- Samples that are too soft and cannot support the load of the clamp need alterations in sample dimensions to get meaningful measurements

## Applications:

- Mechanical properties,  $T_g$ , secondary transitions (modulus and  $\tan \delta$ )
- Creep and stress relaxation
- Temperature controlled constant force or displacement tests to understand processing effects

# Compression clamp governing equations

Modulus = Stiffness × Geometry Factor (GF)

$$GF_{\text{Comp}} = \frac{\textit{thickness}}{\textit{sample surface area}} = \frac{t}{\pi r^2}$$

r = sample radius

t = sample thickness, between clamp faces

	To increase stiffness	To decrease stiffness
Compression	Decrease thickness. If possible, increase radius.	Increase thickness. If possible, decrease radius.

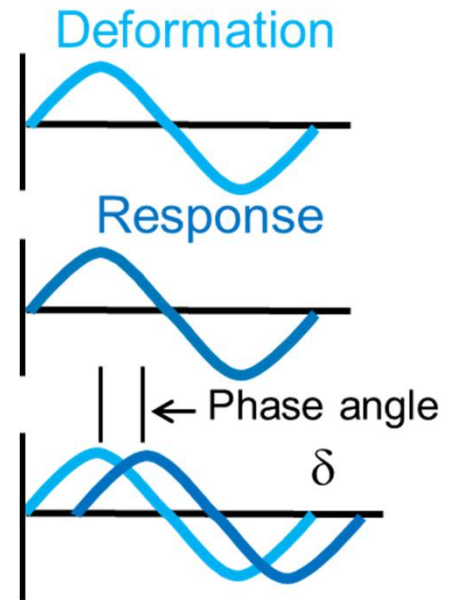
## Available oscillatory test modes

- Strain (stress) Sweep
- Time Sweep
- Frequency Sweep
- Temperature Ramp
- Temperature Step (Sweep) (TTS)

<https://www.tainstruments.com/recorded-theory-applications-training/>

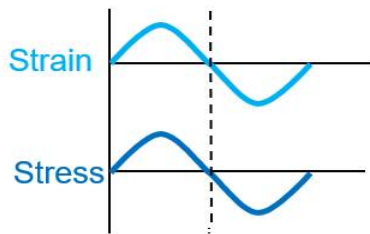
# Dynamic testing and phase angle

- An oscillatory (sinusoidal) deformation (stress or strain) is applied to a sample.
- The material response (strain or stress) is measured.
- The phase angle  $\delta$ , or phase shift, between the deformation and response is also measured.



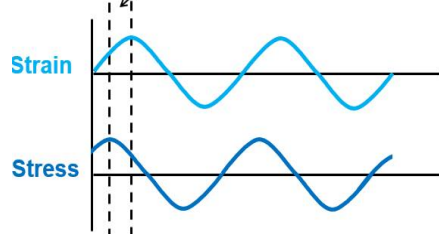
Purely Elastic Response  
(Hookean Solid)

$$\delta = 0^\circ$$



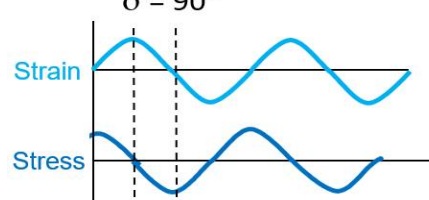
Viscoelastic Response  
(Most materials)

Phase angle  $0^\circ < \delta < 90^\circ$



Purely Viscous Response  
(Newtonian Liquid)

$$\delta = 90^\circ$$



# Viscoelastic parameters

- **Complex Modulus:**

Measure of materials overall resistance to deformation.

$$E^* = \frac{\sigma}{\gamma}$$

- **The Elastic (storage) Modulus:**

Measure of elasticity of material. The ability of the material to store energy.

$$E' = \left(\frac{\sigma}{\gamma}\right) \cos \delta$$

- **The Viscous (loss) Modulus:**

The ability of the material to dissipate energy. Energy lost as heat.

$$E'' = \left(\frac{\sigma}{\gamma}\right) \sin \delta$$

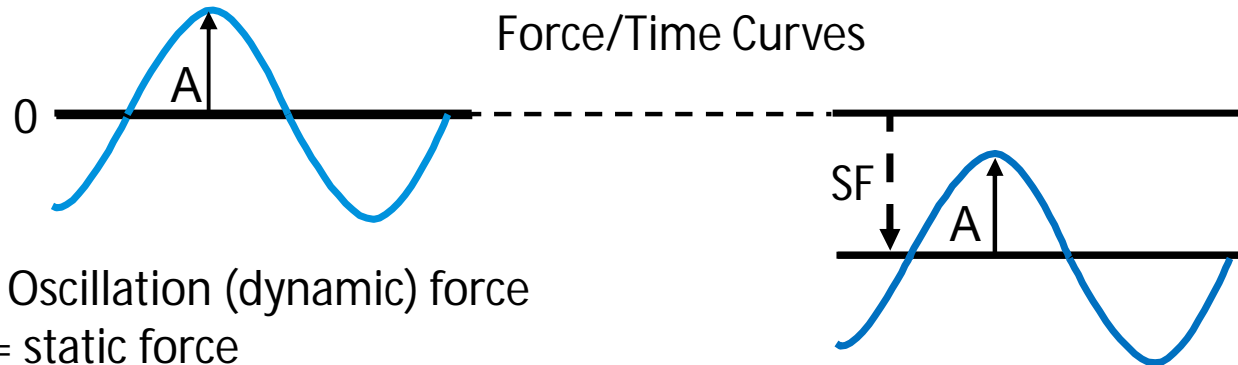
- **Tan Delta:**

Measure of material damping. Increasing tan  $\delta$  implies a greater potential for energy dissipation and lower elasticity, and vice-versa. Measure of viscous property while having the appropriate level of stiffness.

$$\tan \delta = \frac{E''}{E'}$$



# Some Clamps Require Offset (static) Force!



## Clamps **without** static force:

- Single Cantilever
- Dual Cantilever
- Shear Sandwich

## Clamps **with** static force:

- Tension Film
- Tension: Fiber
- 3-Point Bend
- Compression
- Penetration

# How to Setup Force Track?

- **Recap: Desired situation for all clamps is that  $F_{static} > F_{osc}$**
- Force track =  $\frac{F_{static}}{F_{osc}}$
- If  $\frac{F_{static}}{F_{osc}} > 1$ , then  $F_{static} > F_{osc}$
- Force track ratio is expressed as a percentage
  - On 850 and 800, Force track =  $\frac{F_{static}}{F_{osc}} \times 100\%$
  - On RSA-G2, Force track =  $(\frac{F_{static}}{F_{osc}} - 1) \times 100\%$

## DMA850

▼ Clamp: 3 Point Bending Clamp

▲ Procedure:

Initial/preload force  N

Use Force Track  %

## RSA G2 or rheometer

▼ Geometry: Tension fixture (rectangle)

▲ Procedure:

1: Conditioning Options

Axial force adjustment

Mode

Tension  Compression

Axial force  N  Set initial value

Sensitivity  N

Proportional force Mode   Compensate for modulus

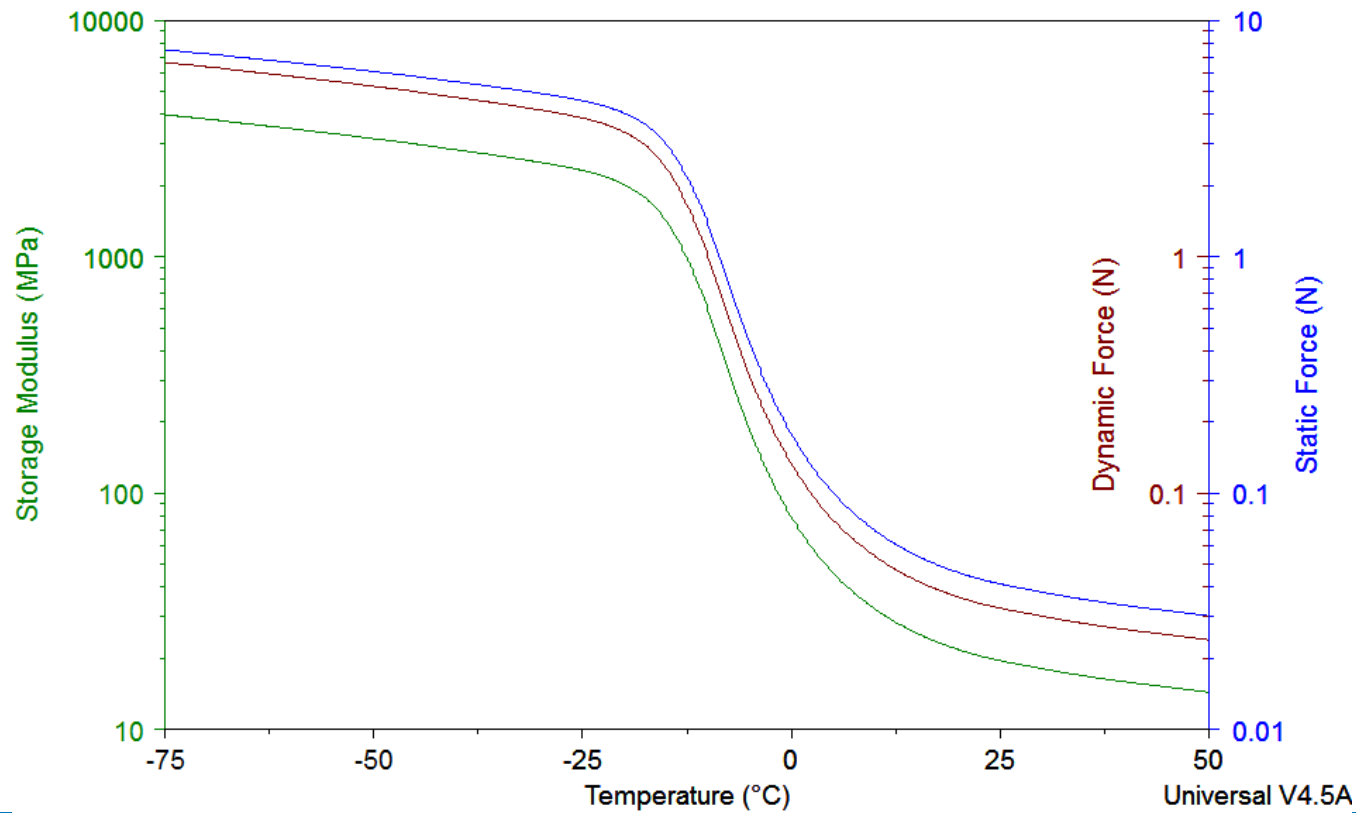
Axial Force > Dynamic Force  %

Minimum axial force  N

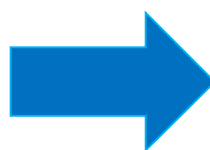
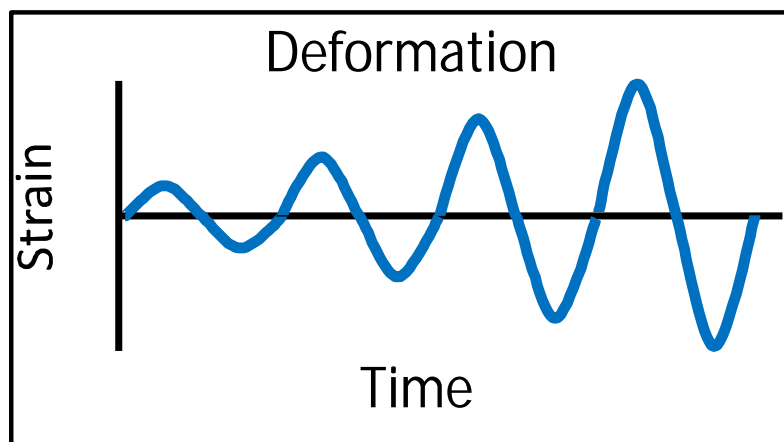
Programmed Extension Below  Pa

# Temperature Ramp with Force Track

- Static Force tracks Dynamic Force throughout Temperature Ramp to prevent over-stretching



# Dynamic Strain (Stress) Sweep

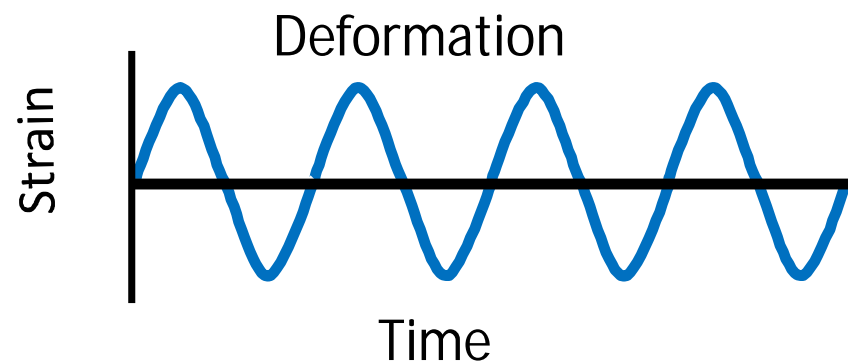


The material response to increasing deformation amplitude is monitored at a constant frequency and temperature.

## USES

- Identify Linear Viscoelastic Region
- Payne effect analysis for elastomers

# Dynamic Time Sweep

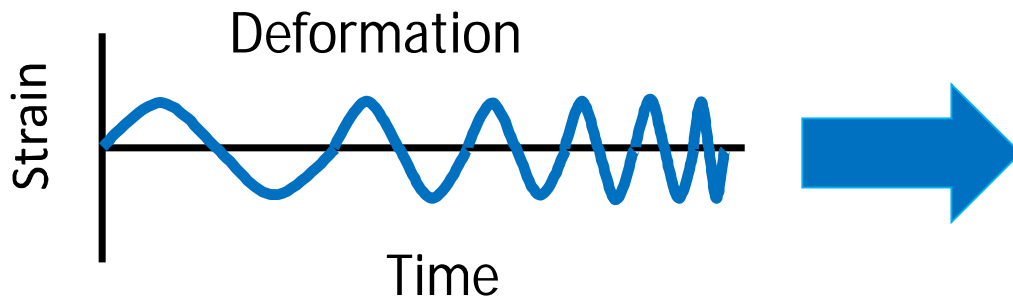


The material response is monitored at a constant frequency, amplitude and temperature.

## USES

- Curing studies
- Fatigue tests
- Stability against thermal degradation

# Frequency Sweep



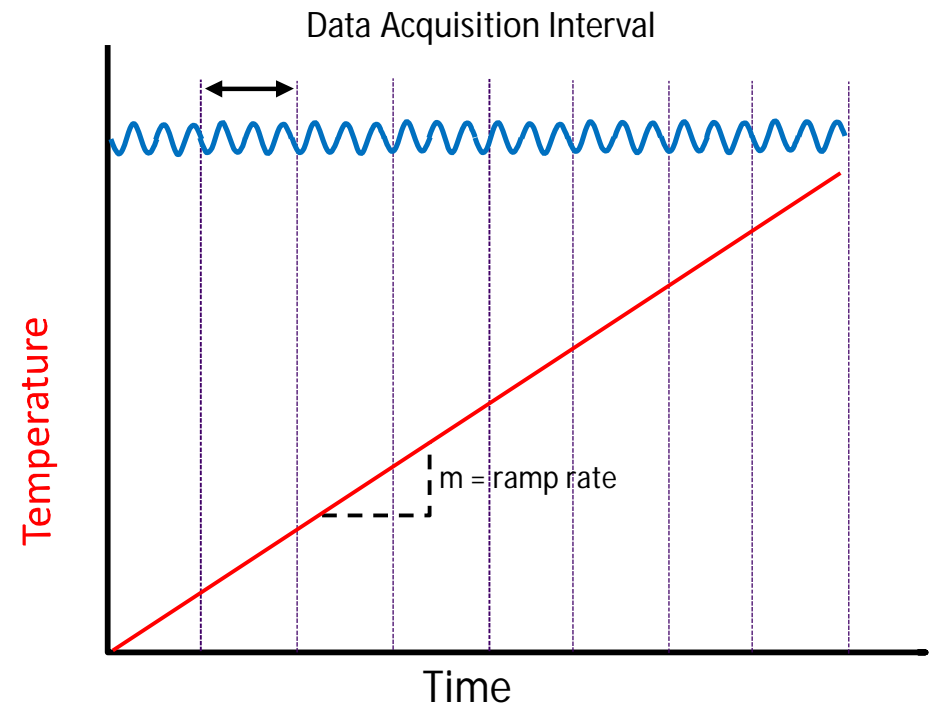
- The material response to increasing frequency (rate of deformation) is monitored at a constant amplitude and temperature.

## USES

- Quick comparison on modulus and elasticity on solids
- Study polymer melt processing (shear sandwich).
- Estimate long term properties with extended frequency (time) range using TTS

# Dynamic Temperature Ramp

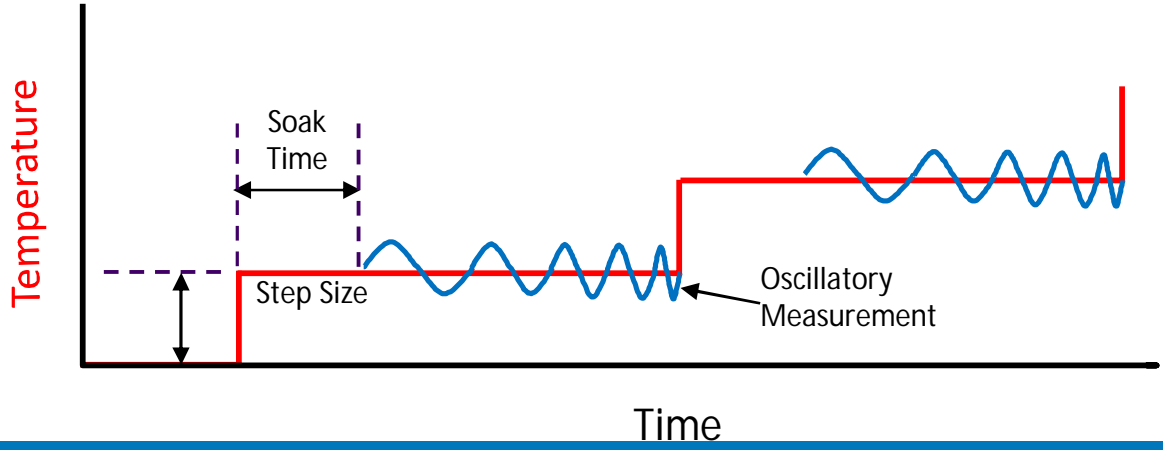
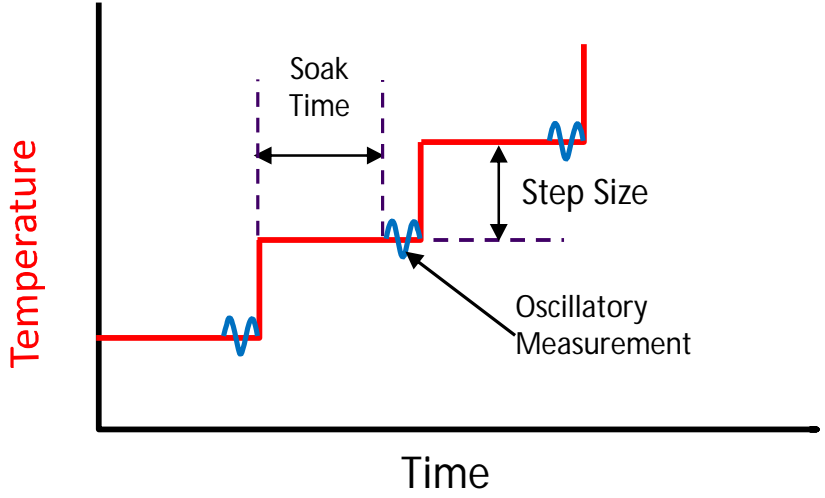
- A linear heating rate is applied. The material response is monitored at a constant frequency and constant amplitude of deformation. Data is taken at user defined time intervals.



Recommend ramp rate for polymer testing: 1-5°C/min.

# Temperature Step & Hold- Single /Multi-Frequency

- A step and hold temperature profile is applied. The material response is monitored at one, or over a range of frequencies, at constant amplitude of deformation





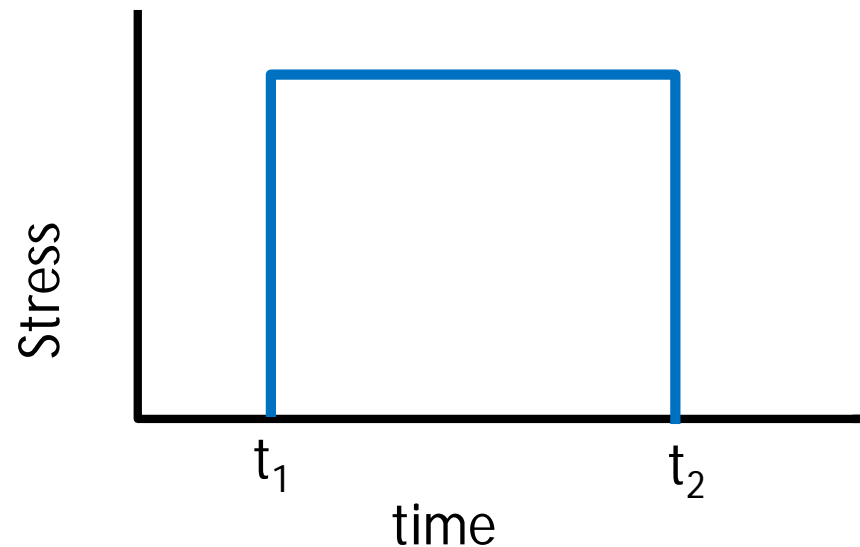
## Available transient test modes

- Creep-Recovery
- Stress Relaxation
- Iso-strain Temperature Ramp
- Iso-force Temperature Ramp
- Stress-Strain Rate Tests

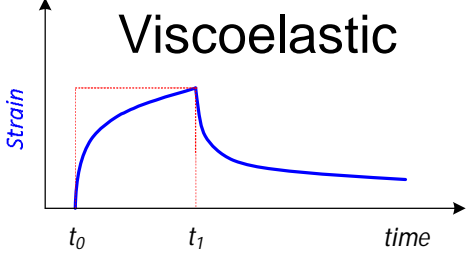
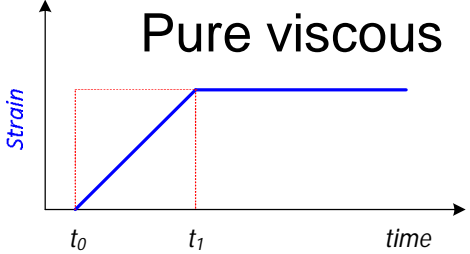
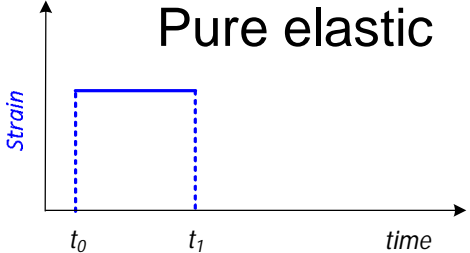
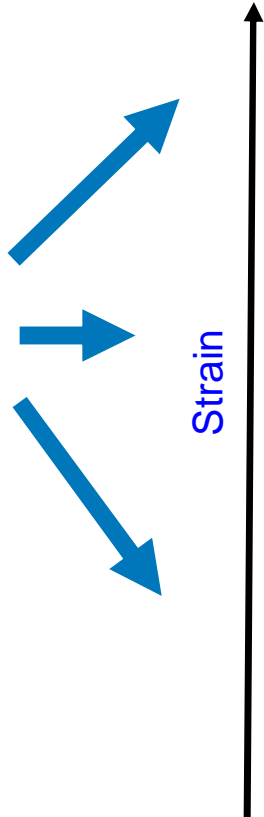
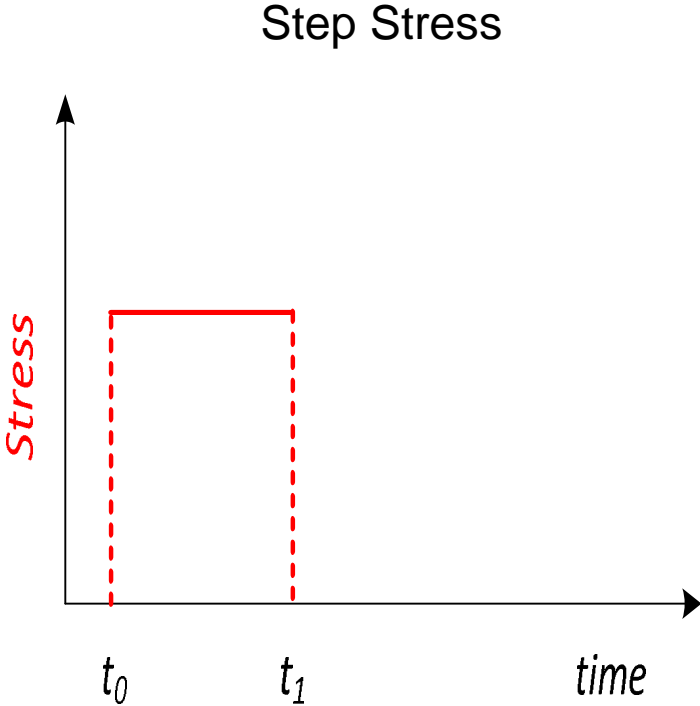
<https://www.tainstruments.com/recorded-theory-applications-training/>

# Creep Recovery Experiment

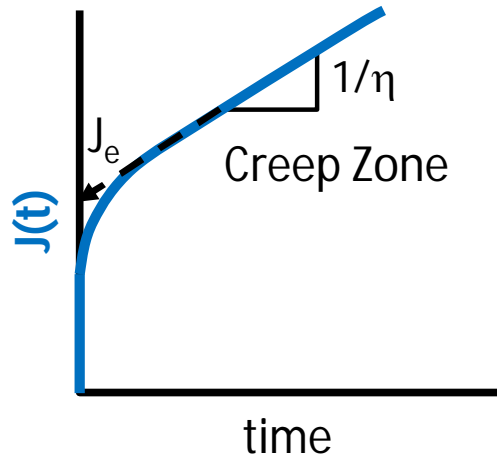
- A stress is applied to sample instantaneously at  $t_1$  and held constant for a specific period of time. The strain is monitored as a function of time ( $\gamma(t)$  or  $\varepsilon(t)$ ).
- The stress is reduced to zero at  $t_2$  and the strain is monitored as a function of time ( $\gamma(t)$  or  $\varepsilon(t)$ ).



# Creep-recovery: Material response



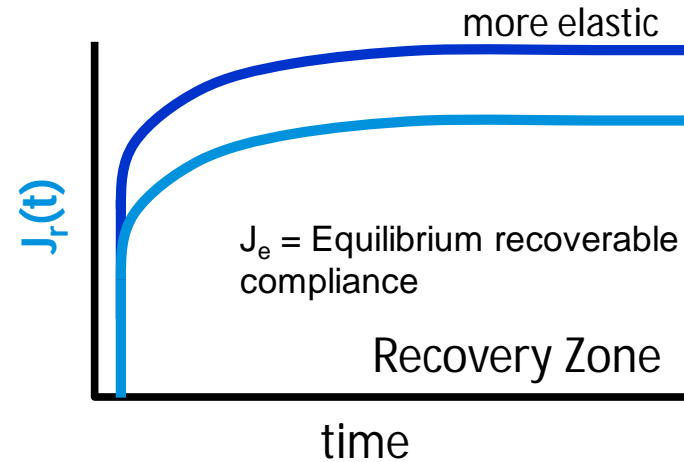
# Creep and Recoverable Compliance



Creep Compliance

$$J(t) = \frac{\gamma(t)}{\sigma}$$

Creep experiments report the material property *Compliance* which is in a sense the inverse of Modulus



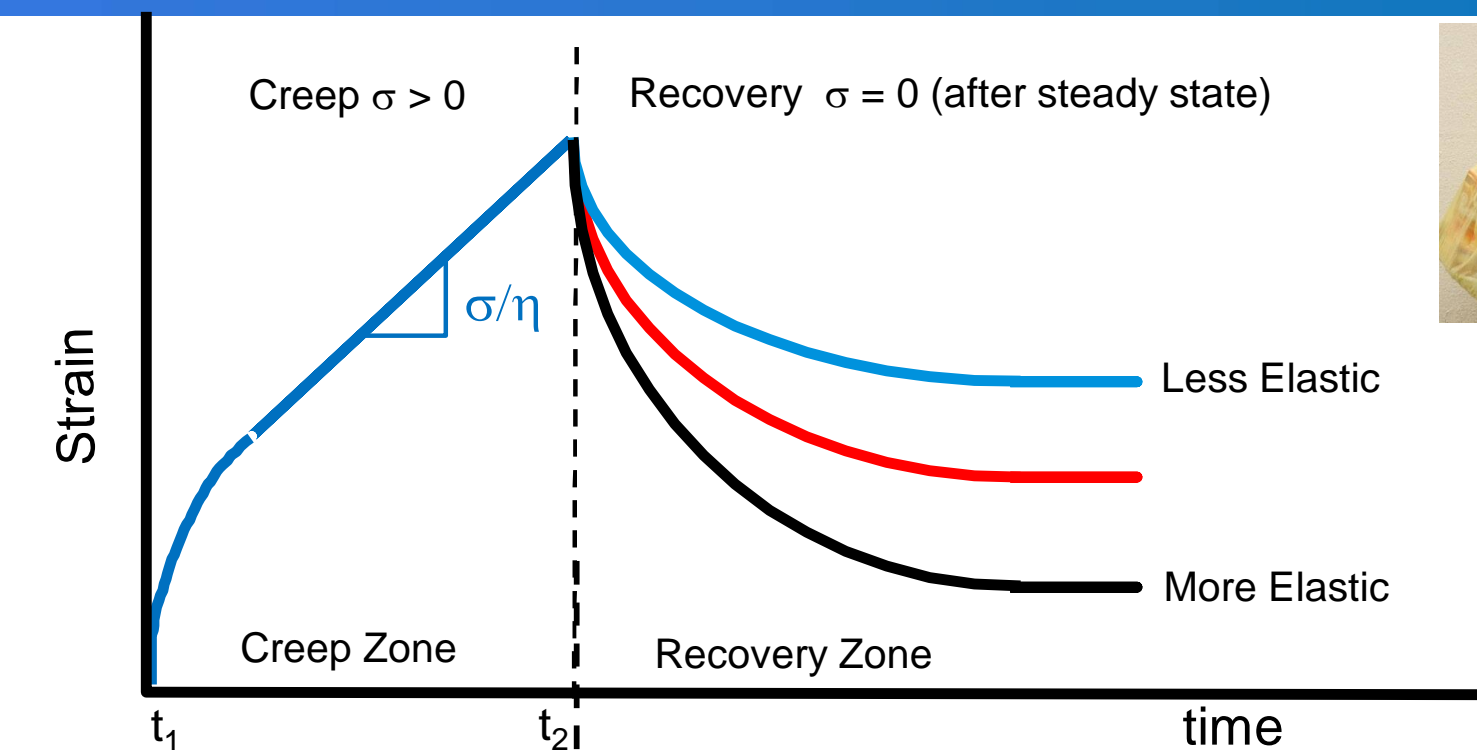
Recoverable Compliance

$$J_r(t) = \frac{[\gamma_u - \gamma(t)]}{\sigma}$$

Where  $\gamma_u = \text{Strain at unloading}$   
 $\gamma(t) = \text{time dependent recoverable strain}$

Mark, J., et. al., Physical Properties of Polymers, American Chemical Society, 1984, p. 102.

# Creep-recovery: Viscoelastic fingerprint



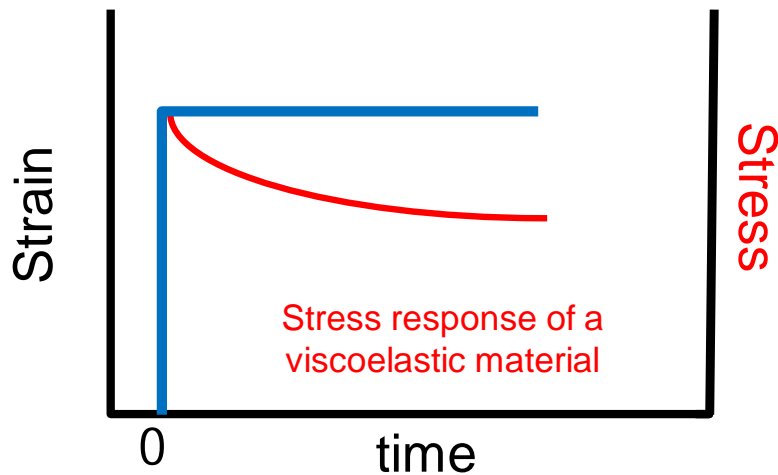
Strain rate decreases with time in the creep zone until finally reaching a steady state

In the recovery zone, the viscoelastic fluid recoils, eventually reaching an equilibrium at some small total strain relative to the strain at unloading.

Mark, J., et. al., *Physical Properties of Polymers*, American Chemical Society, 1984, p. 102.

# Stress relaxation

Strain is applied to the sample instantaneously (in principle) and held constant with time  
Stress is monitored as a function of time  $\sigma(t)$



$$\text{Relaxation modulus} = \frac{\text{stress}}{\text{strain}}$$

Strain Control ▾ Stress Relaxation ▾

Temperature	<input type="text" value="50"/>	°C
Soak time	<input type="text" value="120.0"/>	s
Preload force	<input type="text" value="0.01"/>	N
Strain	<input type="text" value="1.0"/>	%
Relaxation time	<input type="text" value="600.0"/>	s
Recovery time	<input type="text" value="0.0"/>	s

Data sampling mode

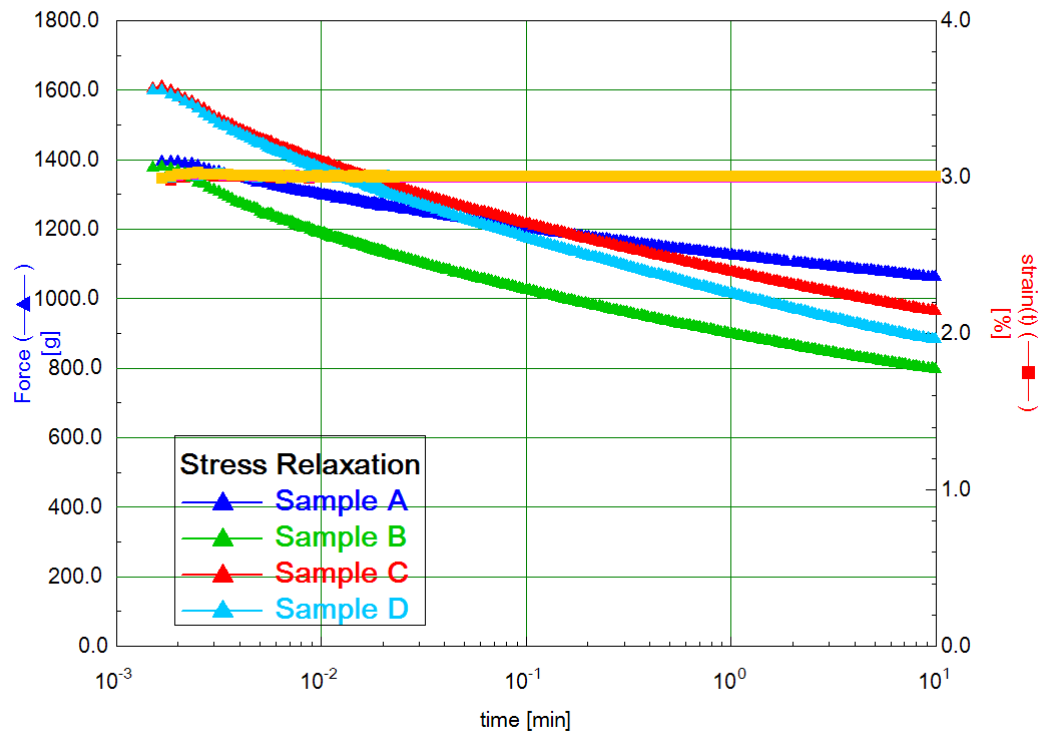
Linear  Log

Sampling rate  pts/s

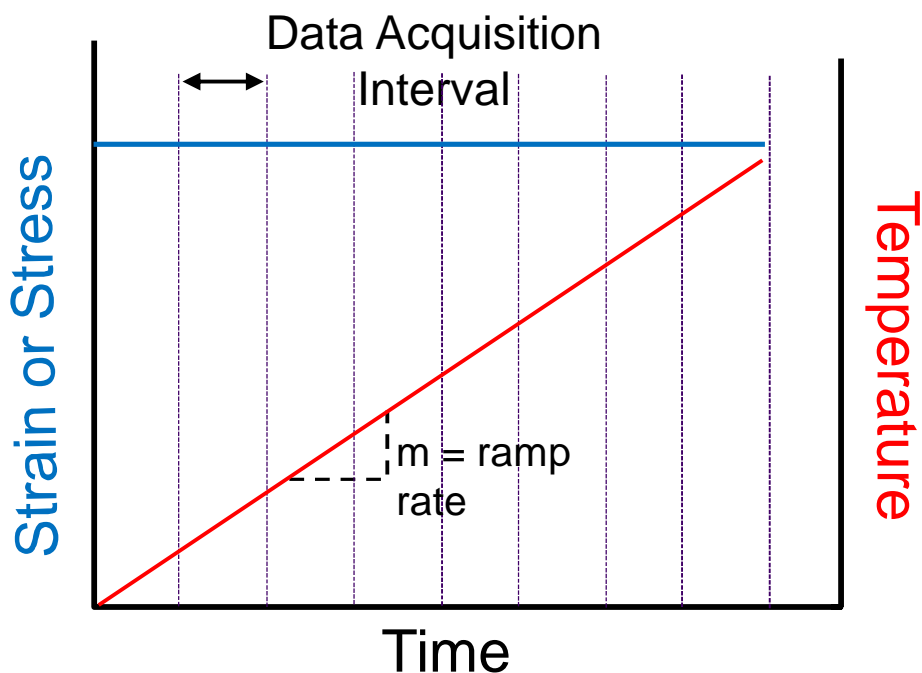
# O-rings: Stress Relaxation

- Squeeze the O-ring to a certain strain. Hold it constant, then measure how long it takes for the force to relax

O-ring Stress Relaxation



# Iso strain/stress temperature ramp



Temperature

## Iso strain

Sample: [ ]  
Clamp: Film Clamp  
Strain Control ▾ IsoStrain ▾

Preload force [ 0.01 ] N  
Displacement [ 20.0 ] μm  
Sampling rate [ 1.0 ] pts/s

Use current temperature

Ramp from [ 25 ] °C to [ 150 ] °C  
Ramp rate [ 3.0 ] °C/min

Soak times  
at Start temperature [ 300.0 ] s  
at End temperature [ 0.0 ] s

Estimated time to complete 00:41:40 hh:mm:ss

Test Settings Post Test Conditions

## Iso stress

Sample: [ ]  
Clamp: Film Clamp  
Stress Control ▾ IsoStress ▾

Preload force [ 0.01 ] N  
Stress [ 500.0 ] Pa  
Sampling rate [ 1.0 ] pts/s

Use current temperature

Ramp from [ 25 ] °C to [ 150 ] °C  
Ramp rate [ 3.0 ] °C/min

Soak times  
at Start temperature [ 300.0 ] s  
at End temperature [ 0.0 ] s

Estimated time to complete 00:41:40 hh:mm:ss

Test Settings Post Test Conditions

The strain or stress is held at a constant value and a linear heating rate is applied.

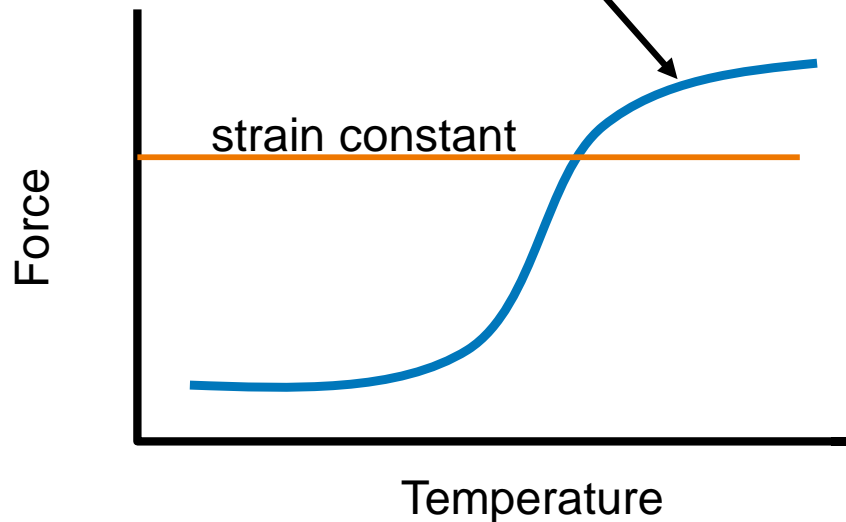
Assessing mechanical behavior under conditions of confined or fixed load (stress) or deformation (strain).

Example: Measure sample shrinkage

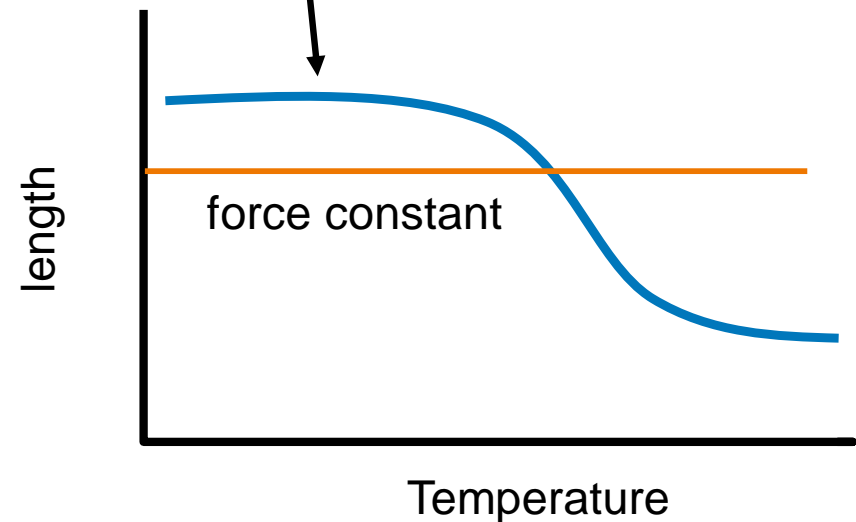


# Iso strain/stress temperature ramp

Sample is held at a constant length;  
shrinkage force is measured



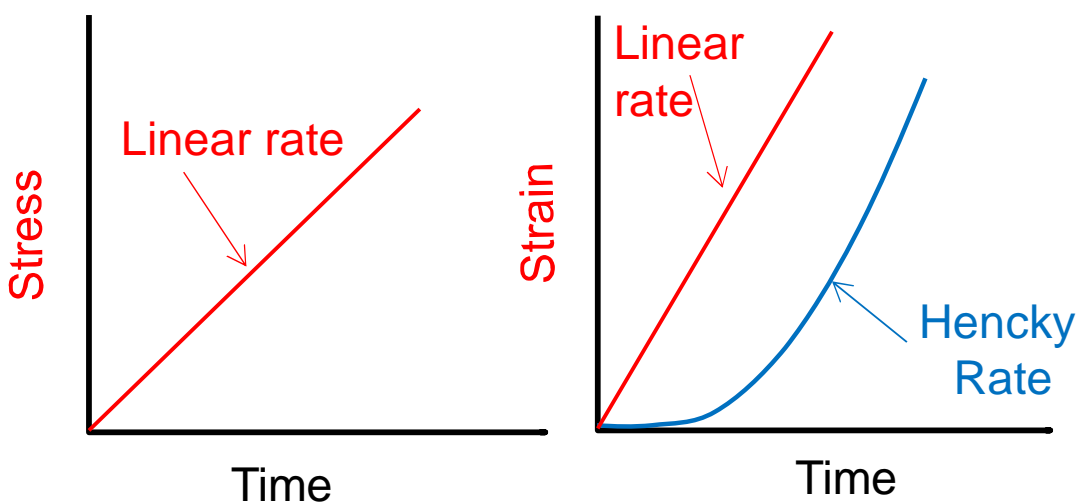
Sample is held at a constant  
force; shrinkage is measured



# Stress-strain test

Sample is deformed under a constant linear strain rate, Hencky strain rate, force, or stress for generating more traditional stress-strain curves.

Measure sample's Young's modulus, yield stress, strain hardening effect and sample fracture



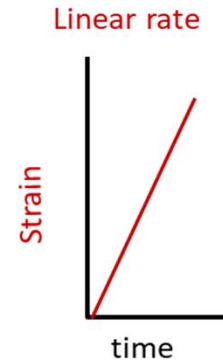
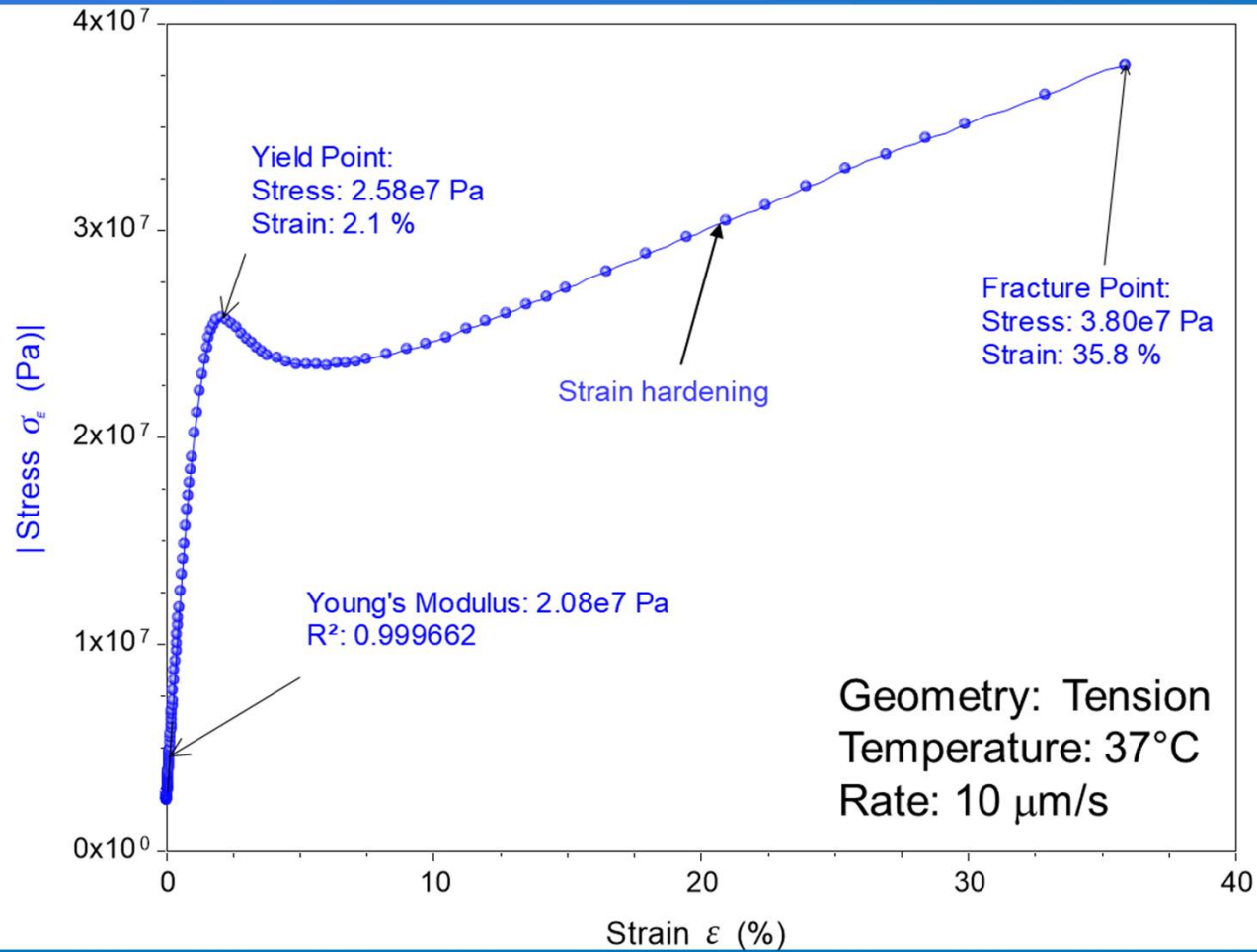
## Strain Ramp

Sample:	
Clamp:	Film Clamp
Rate Control:	Strain Ramp
Temperature:	25 °C
Soak time:	300.0 s
Preload force:	0.01 N
<input checked="" type="checkbox"/> Inherit starting displacement	
Ramp from:	Inherited μm to 100.0 μm
Ramp rate:	20.0 μm/min
Data sampling mode	
<input checked="" type="radio"/> Linear <input type="radio"/> Log	
Sampling rate:	1.0 pts/s
Test Settings	
Post Test Conditions	

## Stress Ramp

Sample:	
Clamp:	Film Clamp
Rate Control:	Stress Ramp
Temperature:	25 °C
Soak time:	300.0 s
Preload force:	0.01 N
<input checked="" type="checkbox"/> Inherit starting force	
Ramp from:	Inherited N to 5.0 N
Ramp rate:	1.0 N/min
Data sampling mode	
<input checked="" type="radio"/> Linear <input type="radio"/> Log	
Sampling rate:	1.0 pts/s
Test Settings	
Post Test Conditions	

# A typical stress-strain curve



# Summary

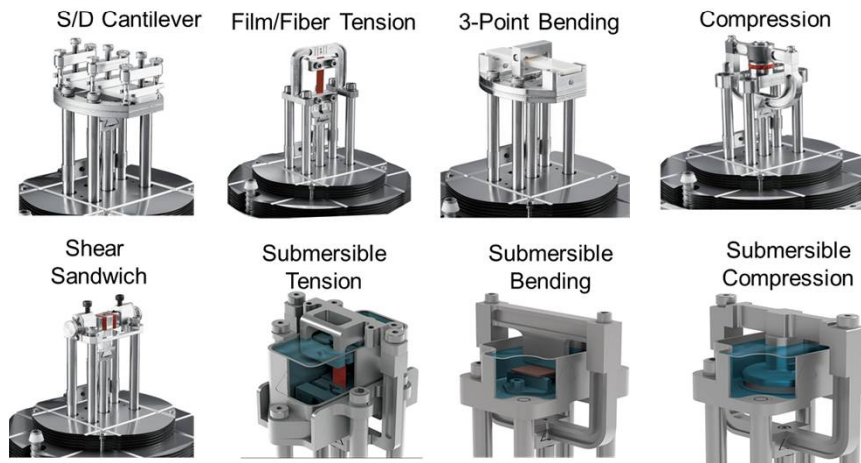


## Dynamic tests

- Strain/amplitude sweep
- Time sweep
- Frequency sweep
- Temperature ramp
- Temperature sweep

## Transient tests

- Creep-recovery
- Stress-relaxation
- Iso-strain temperature ramp
- Iso-stress temperature ramp
- Stress-strain tests



Waters™



Philadelphia Short Course: Day II

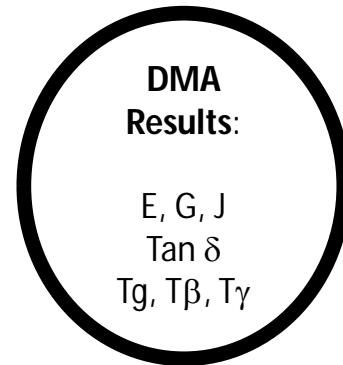
## Section V: DMA Applications

***Terri Chen, PhD***

***Principal Application Scientist***

***TA Instruments – Waters LLC***

# The DMA Results Can Correlate To...



## Molecular structures

- MW and MWD
- Branching
- Crystallinity
- Crosslinking
- Phase
- Relaxation

## Processing:

- Heat history
- Residual stress
- Shear or orientation
- Temperature
- Fillers

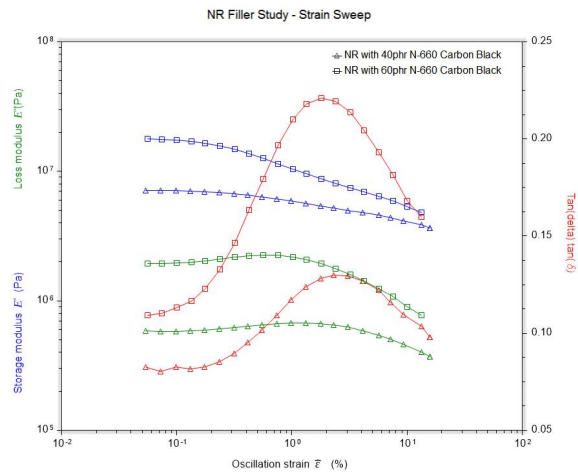
## Product properties

- Transition temperatures (T<sub>g</sub>, T <sub>$\beta$</sub> , T <sub>$\gamma$</sub> )
- Environmental resistance
- Impact strength
- Long term behavior, aging
- Adhesion

# Most common DMA methods

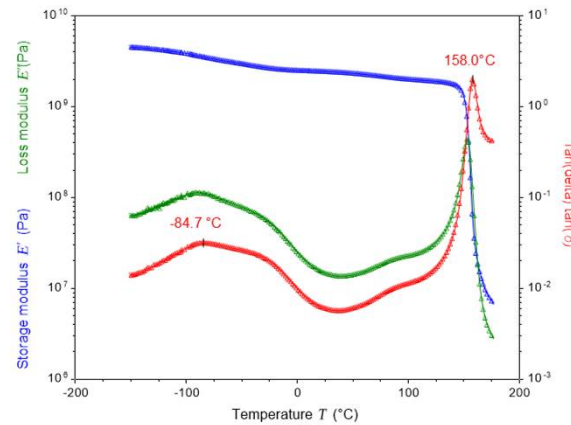
## Most common DMA methods

- Amplitude sweep



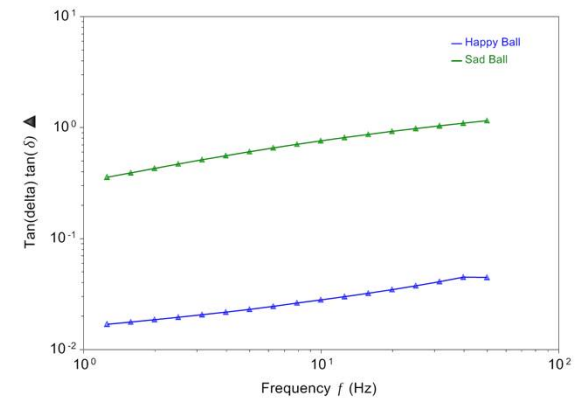
Amplitude Sweeps  
(Linear viscoelastic Region)

- Temperature ramp



Temperature Ramp  
(Transitions and viscoelasticity across temperature)

- Frequency Sweep and TTS



Frequency Sweep  
(viscoelasticity across time scales of deformation)

# Amplitude sweep: identify LVR

## Common DMA methods

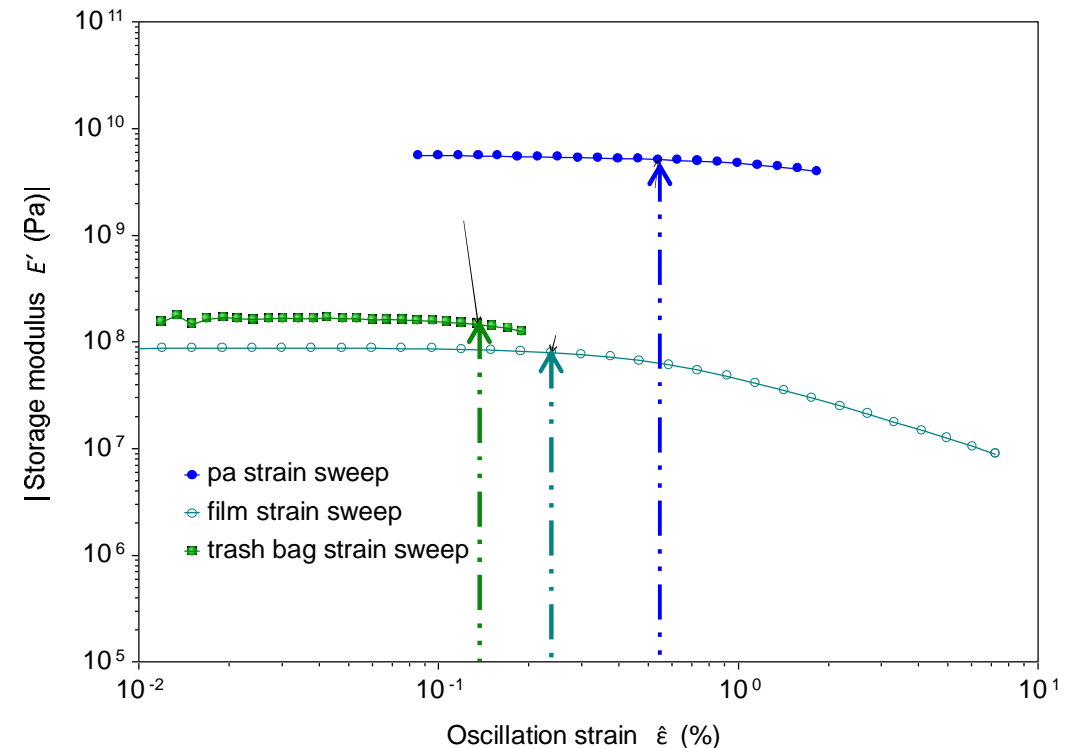
### ○ Amplitude Sweep

From an amplitude sweep:

Obtain the Linear Viscoelastic Region (range of strain values where modulus is independent) at a given frequency

**When performing nondestructive experiments ( frequency sweep, temperature ramp, time sweep) a strain within the LVR must be chosen**

Solid samples typically have an LVR that ends  $\leq 1\%$





# LVR dependence on frequency

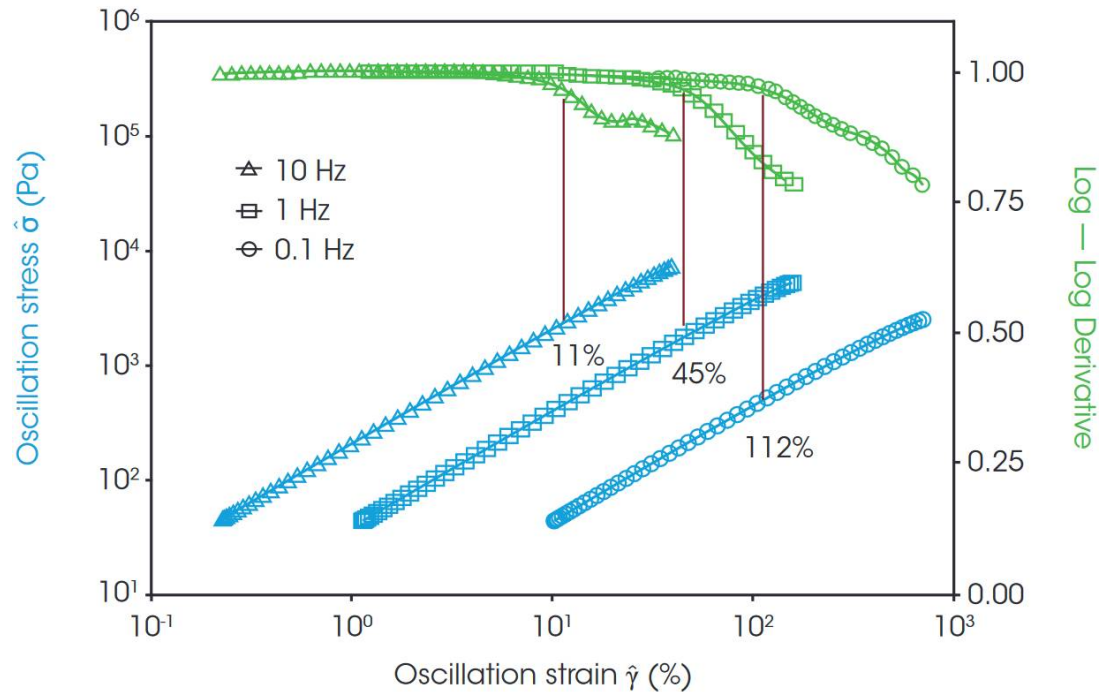
## Common DMA methods

- Amplitude Sweep

From an amplitude sweep:

Obtain the Linear viscoelastic region (LVR - range of strain values where modulus is independent) at a given frequency

**Frequency dependence of LVR – LVR is shorter at higher frequencies, molecules are more stiff**



# LVR dependence on temperature

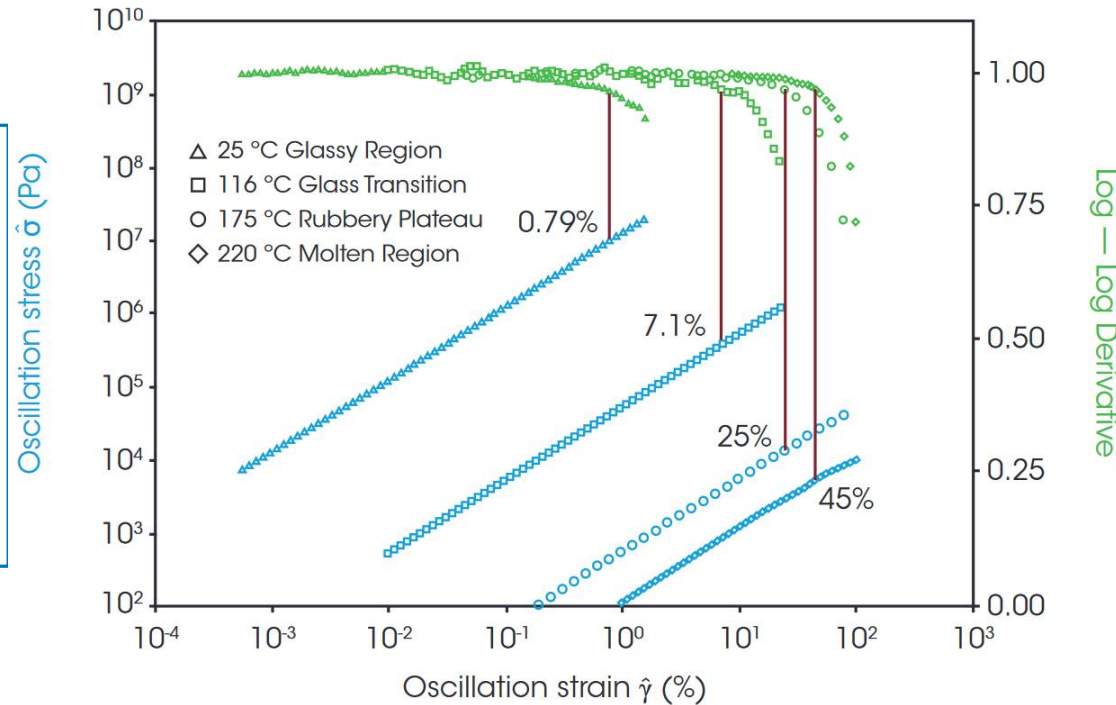
## Common DMA methods

- Amplitude Sweep

From an amplitude sweep:

Obtain the Linear viscoelastic region (LVR - range of strain values where modulus is independent) at a given frequency

**Temperature dependence of LVR – LVR is shorter at lower temperatures, molecules are more stiff**

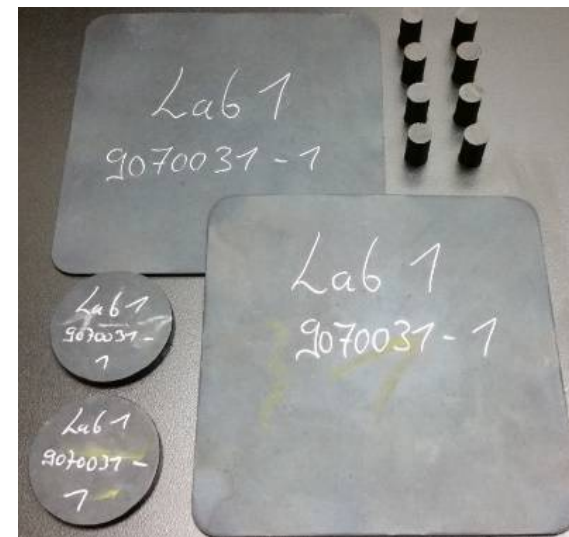
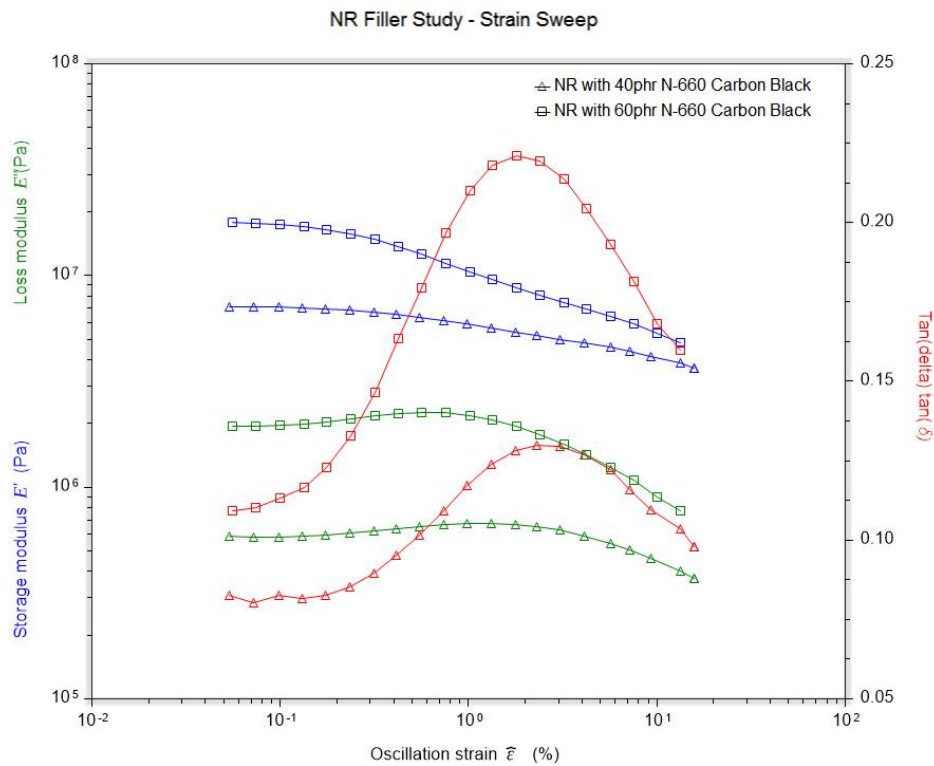


# Rubber: Effect of Filler Content in Tire Rubber (NR)

Study on DMA3200

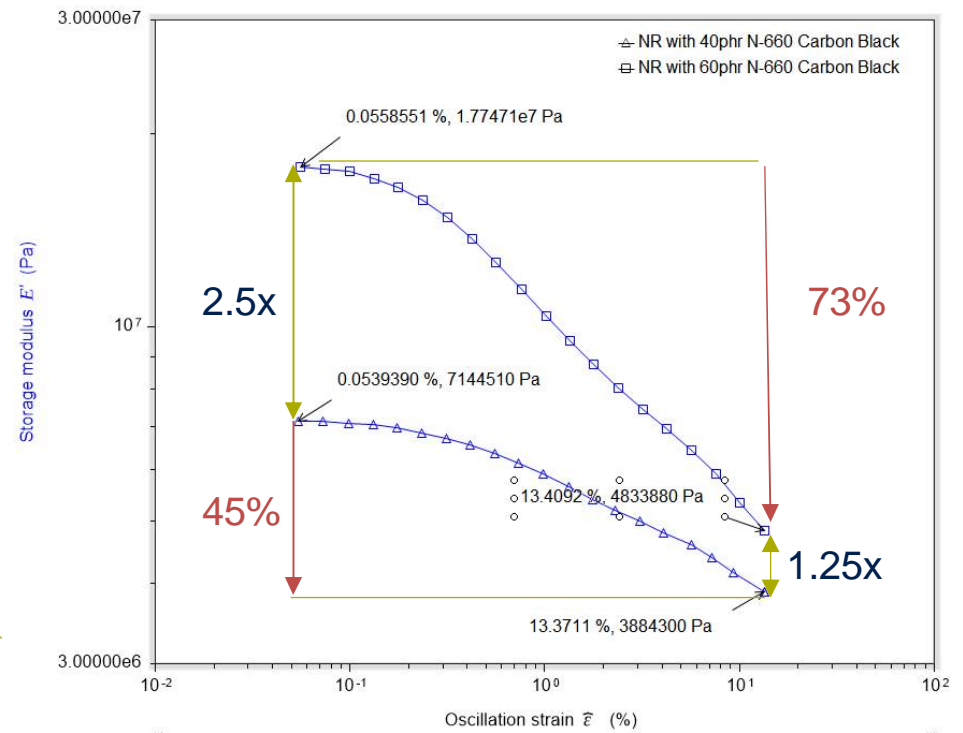
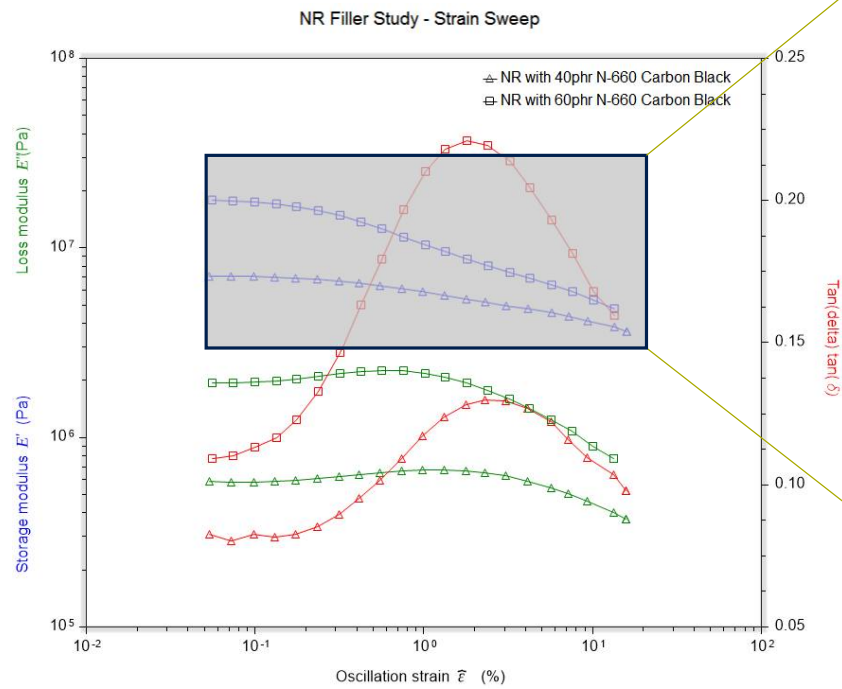
High Force DMA example:

Larger rubber samples where rubber samples are difficult to cut small and precisely enough for conventional DMA tests



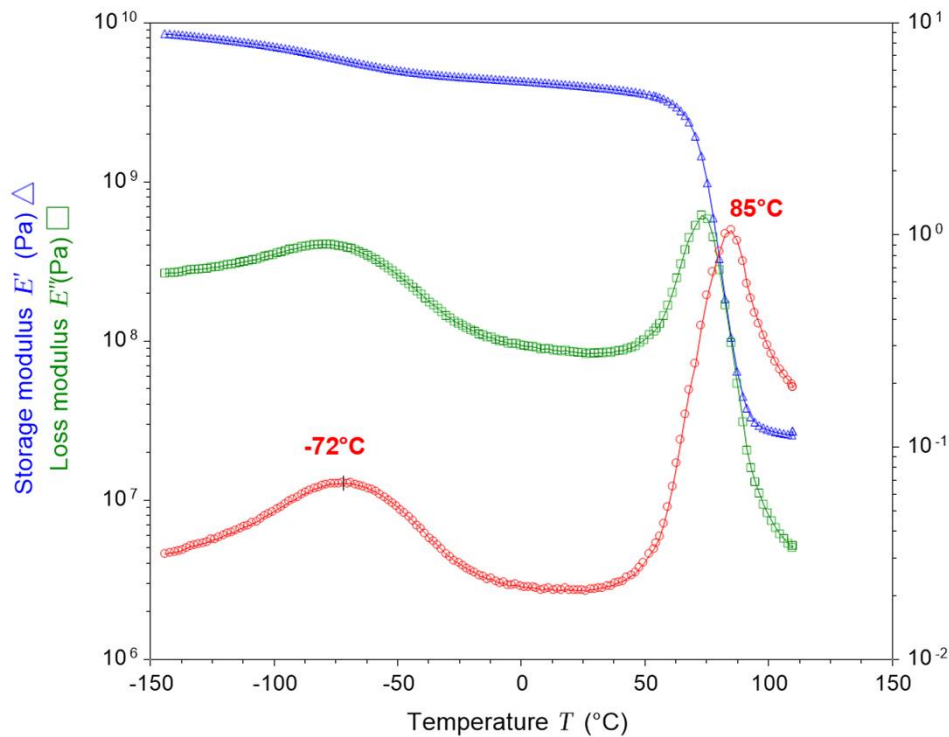
# Rubber: Effect of Filler Content in Tire Rubber (NR)

NR Filler Study - Strain Sweep



# DMA temperature ramp

PET film: Tested in tension



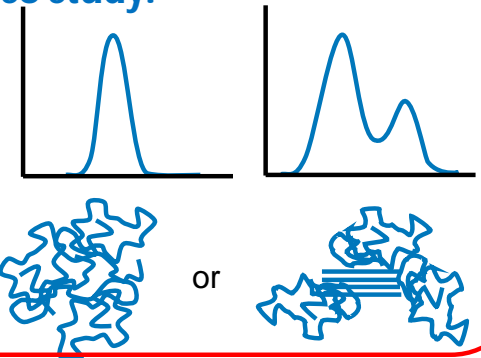
**Glass Transition ( $T_g$ ):** Cooperative motion among a **large number** of chain segments

**Secondary Transitions ( $T_\beta, T_\gamma$ ):** Local or side group motion

Rheology/DMA is 100-1000× more sensitive than DSC for identifying weak amorphous transitions

**DMA temp ramp can also study:**

- Crystallinity
- Crosslinking density
- Blend Miscibility



<https://www.tainstruments.com/recorded-theory-applications-training/>

# Primary and secondary transitions in PC

## Common DMA methods

- Temperature Ramp

From temperature ramp:

Material glass transition

Local Main-Chain Motion – intra-molecular rotational motion of main chain segments four to six atoms in length

Secondary transitions

Side group motion with some cooperative motion from the main chain

Instrument: DMA850

Temperature:

-150°C to 180°C

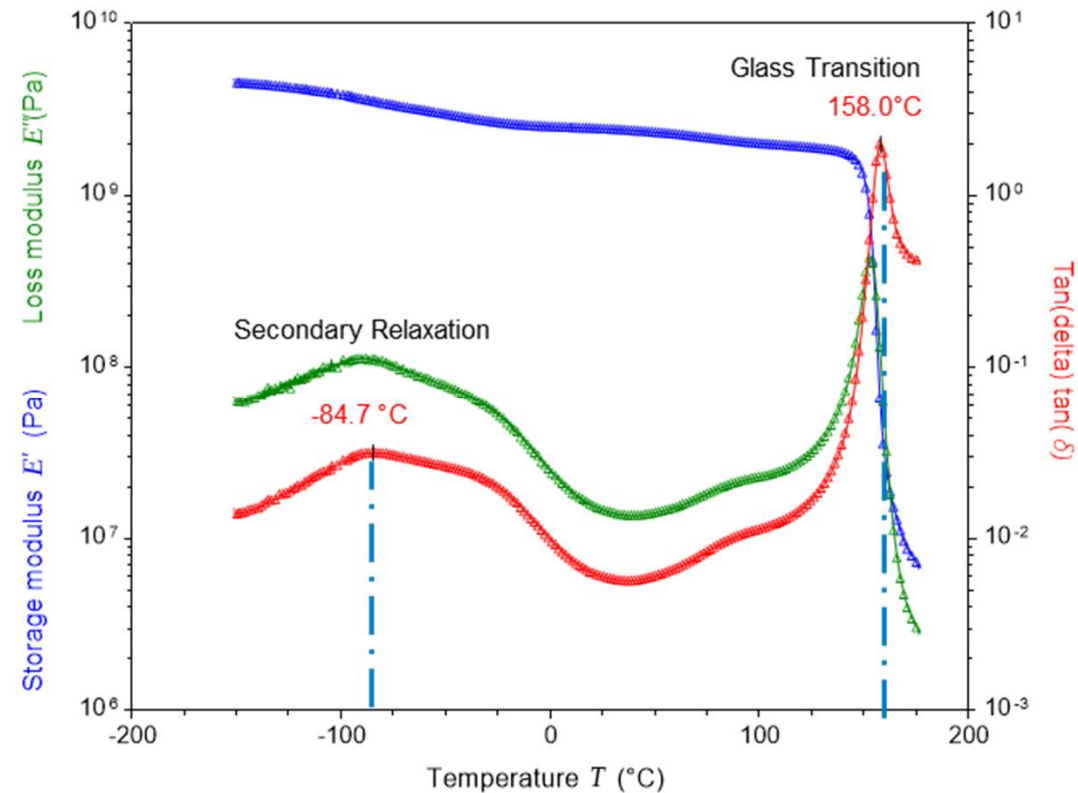
Heating rate: 3°C/min

Frequency: 1Hz

Amplitude: 15  $\mu\text{m}$



## ■ Polycarbonate



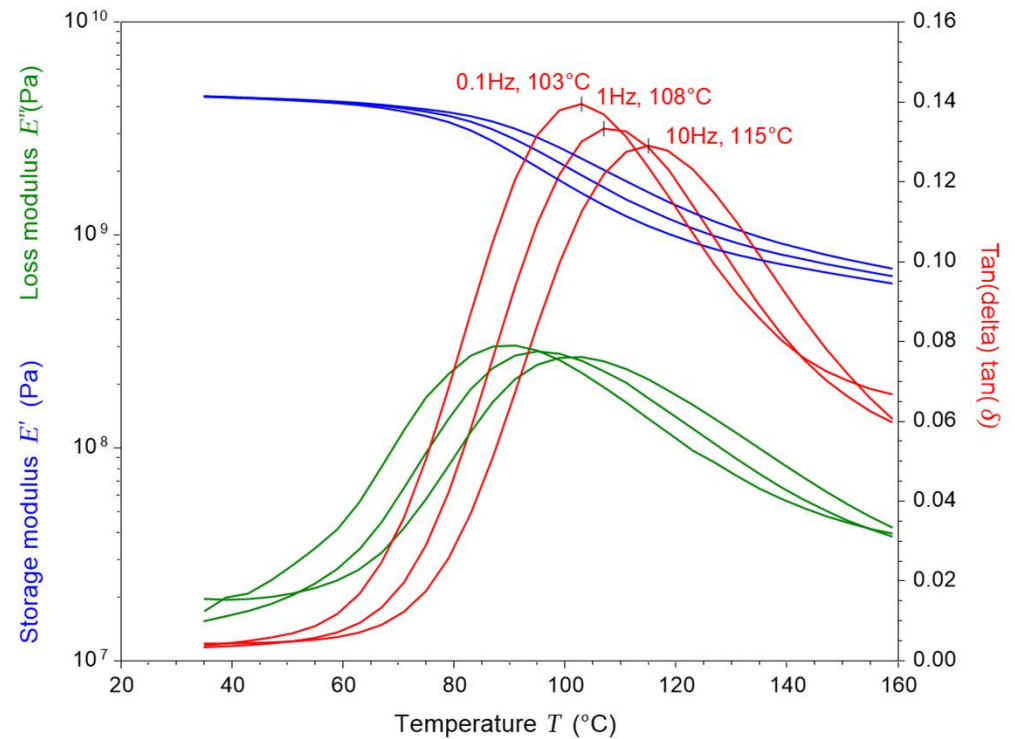
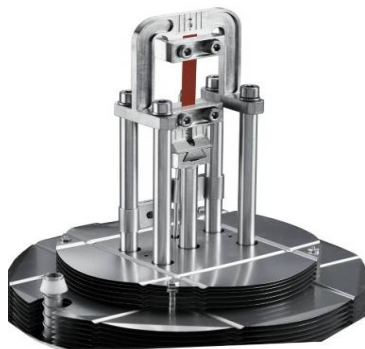
# Effect of frequency on Tg: PET film

## Common DMA methods

- Temperature Ramp

From temperature ramp:

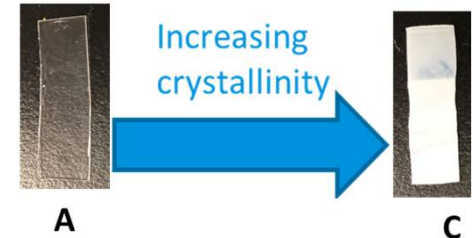
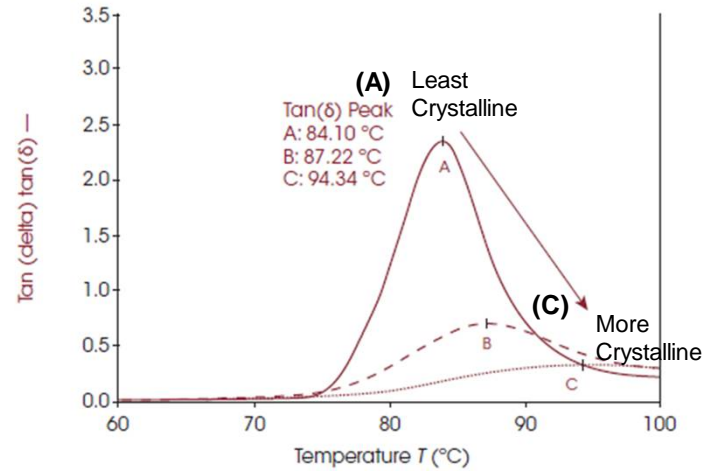
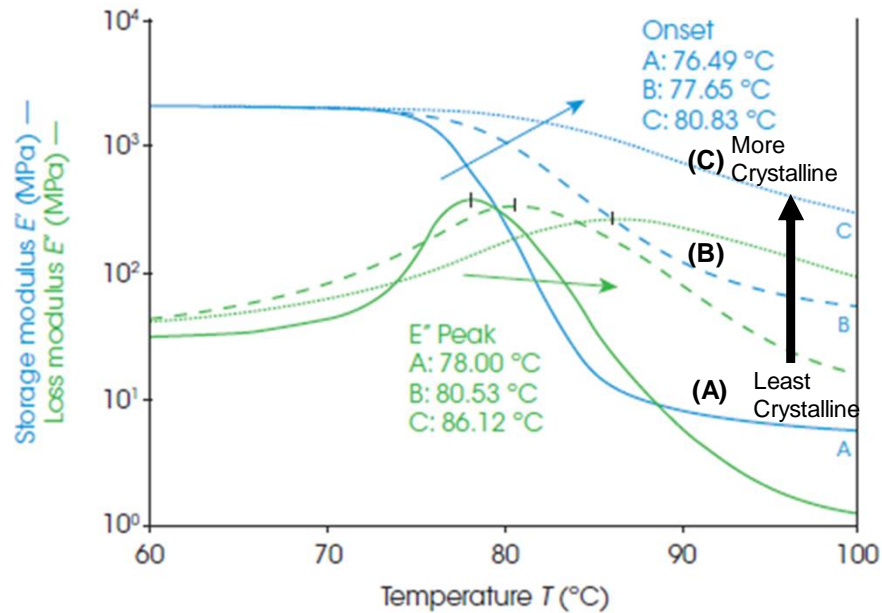
**Observe effect of frequency on the glass transition – higher frequency generally increases Tg, the molecules become more stiff**



# Effect of crystallinity on $E'$ and $\tan\delta$ : PET

## Common DMA methods

### ○ Temperature Ramp



From temperature ramp:

**Observe effect of crystallinity on the storage modulus (Left) and the glass transition temperature (Right)**



# Effect of crosslinking on E' and Tg

## Common DMA methods

### ○ Temperature Ramp

From temperature ramp:

**Observe effect of crosslinking on the storage modulus and the glass transition temperature**

### Increasing crosslinking :

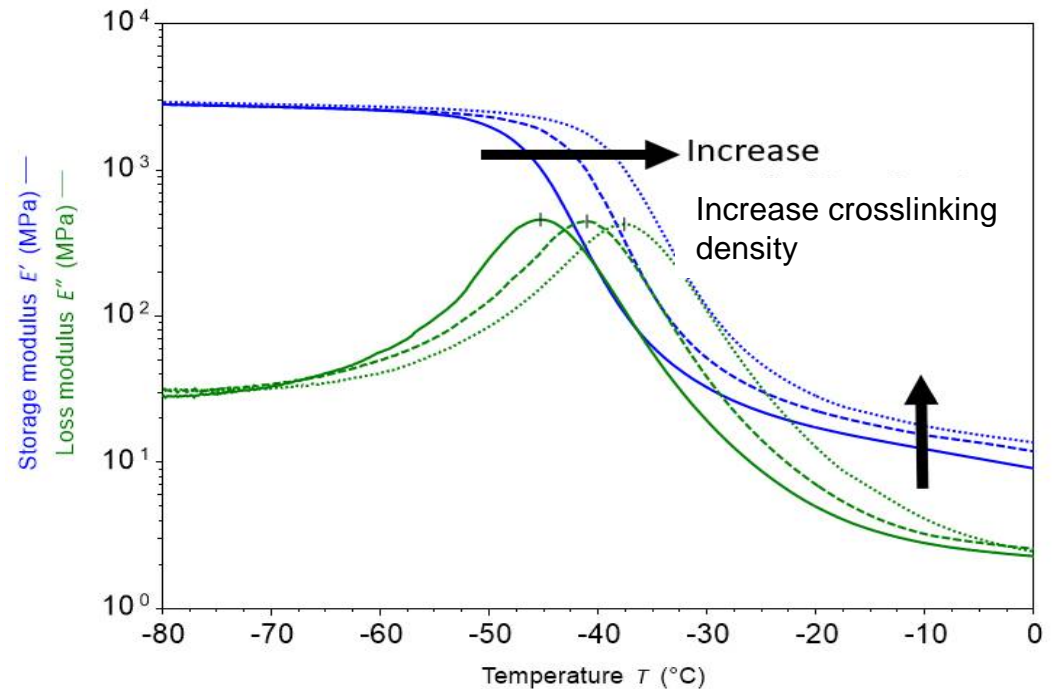
Tg shifted to higher temperatures

Transition becomes broader and weaker (tan δ decreases)

Rubbery plateau modulus increases

Calculating crosslinking density:

$$M_c = \frac{3RTd}{E'_{rubbery}} \quad q = \frac{Mw}{Mc}$$



TA Applications note: RH100 Measurement of Glass Transition Temperatures by Dynamic Mechanical Analysis and Rheology, <https://www.tainstruments.com/pdf/literature/RH100.pdf>

# Effect of aging over time: O-ring

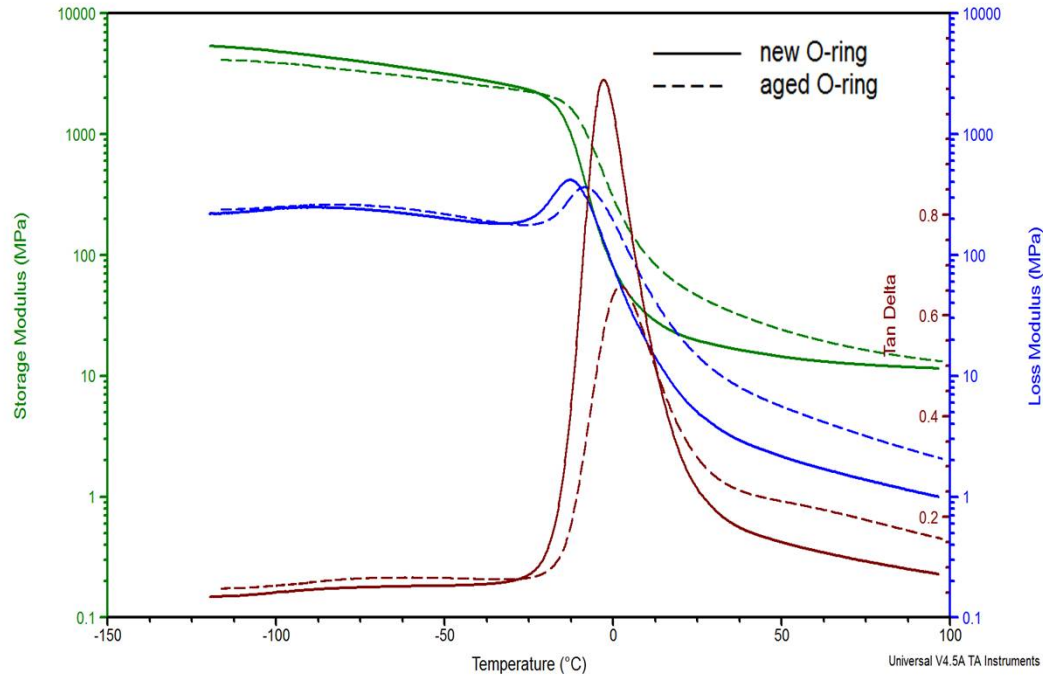
## Common DMA methods

- Temperature Ramp



From temperature ramp:

**Observe effect of aging on a rubber sample - aged O-ring has higher Tg and increased storage modulus at rubbery plateau**



# Effect of plasticizer on vinyl flooring Tg

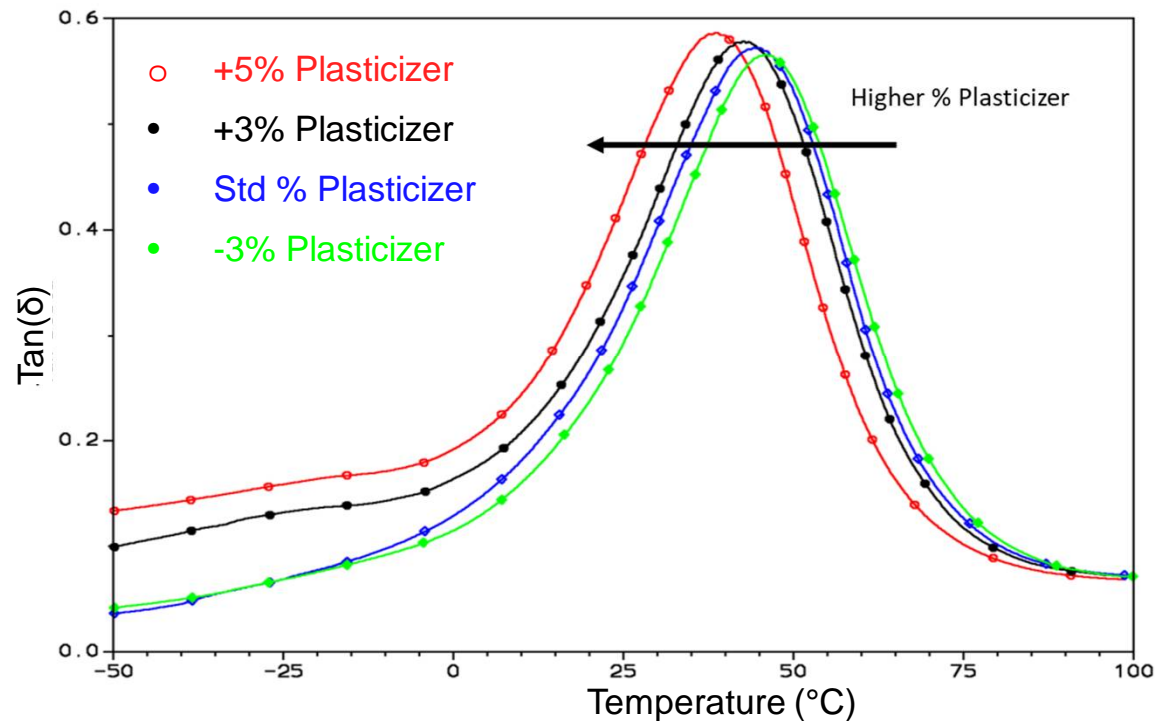
## Common DMA methods

- Temperature Ramp

From temperature ramp:

### Observe effect of increased plasticizer loading

Plasticizers shield molecular interactions of matrix, thereby decreasing the glass transition, and softening the material



# Effect of orientation on mechanical properties

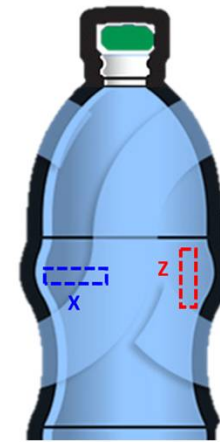
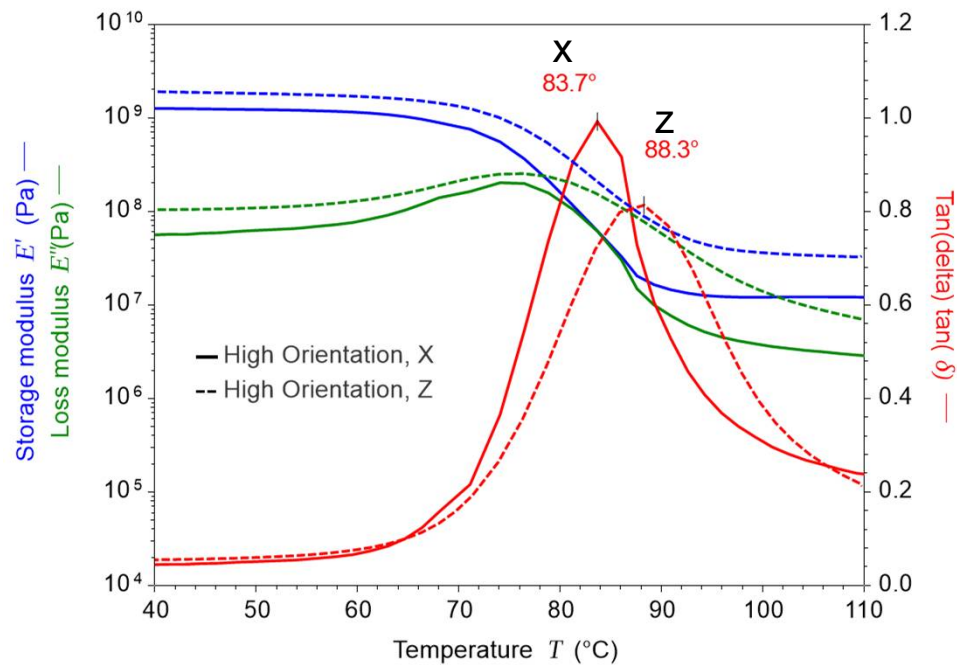
## Common DMA methods

- Temperature Ramp

From temperature ramp:

**Observe effect of orientation on storage modulus and glass transition temperature**

Bottle is stronger in “Z” direction, and this makes sense considering the application



# Polymer blends - miscibility

## Common DMA methods

- Temperature Ramp

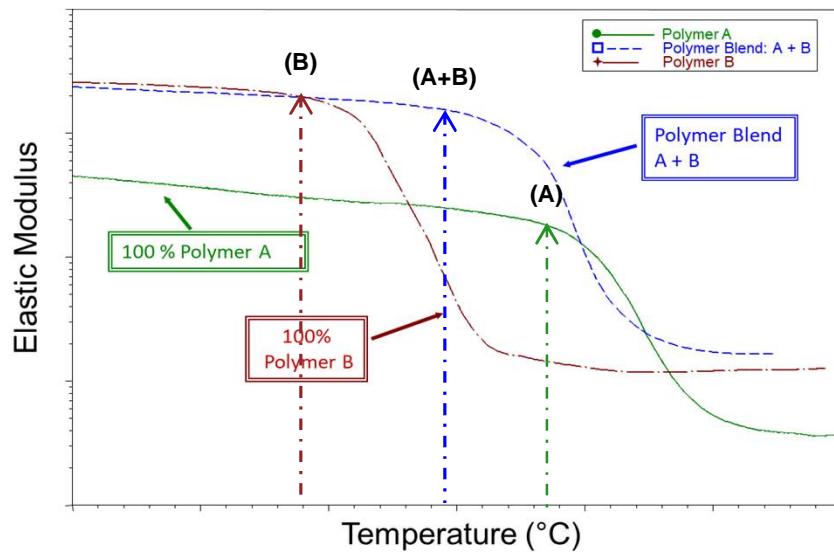
From temperature ramp:

**Observe blend compatibility**

### Miscible Blend

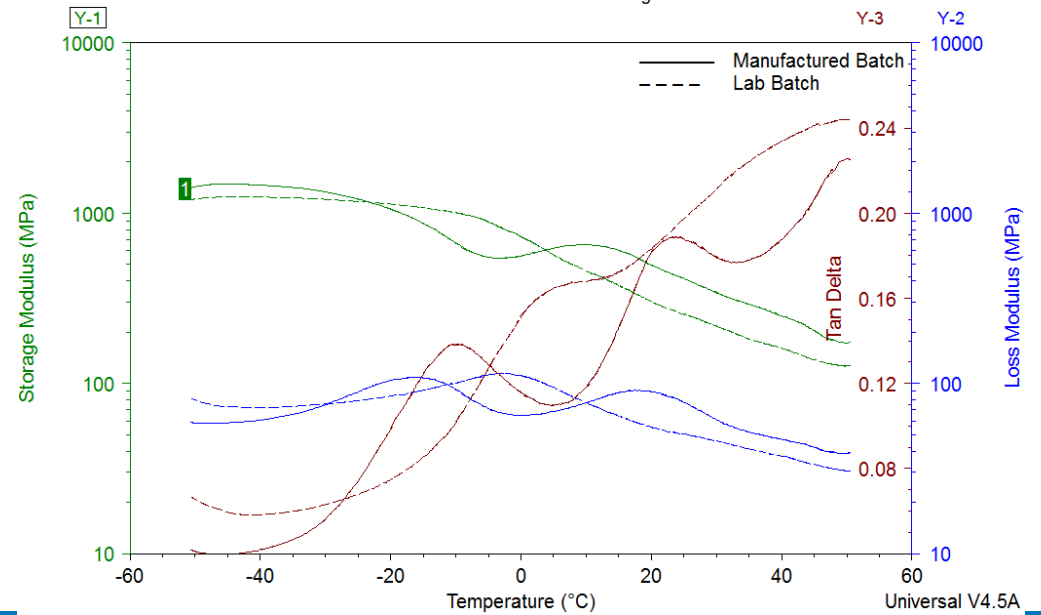
Pure components have unique  $T_g$ 's

Blend has one  $T_g$

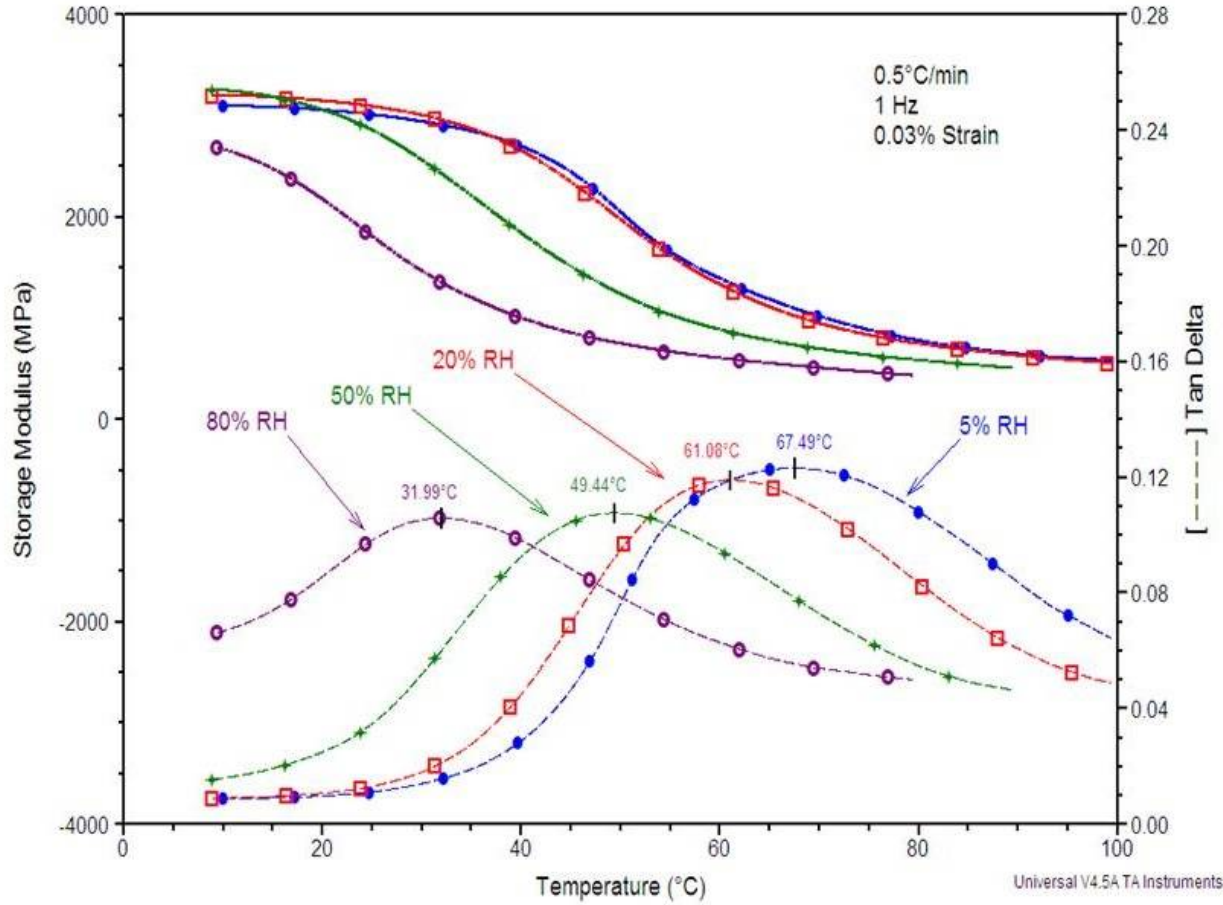


### Immiscible Blend

Blend has two  $T_g$ 's



# Humidity Influence: Nylon Film



# DMA mechanical stress-strain test

- Pull sample at one rate
- Generate Stress vs Strain plot

1: Other Axial

Environmental Control

Temperature  °C  Inherit Set Point

Soak Time  s  Wait For Temperature

Test Parameters

Duration  s

Motor direction  Tension  Compression

Constant linear rate  mm/s

Angular Velocity  rad/s

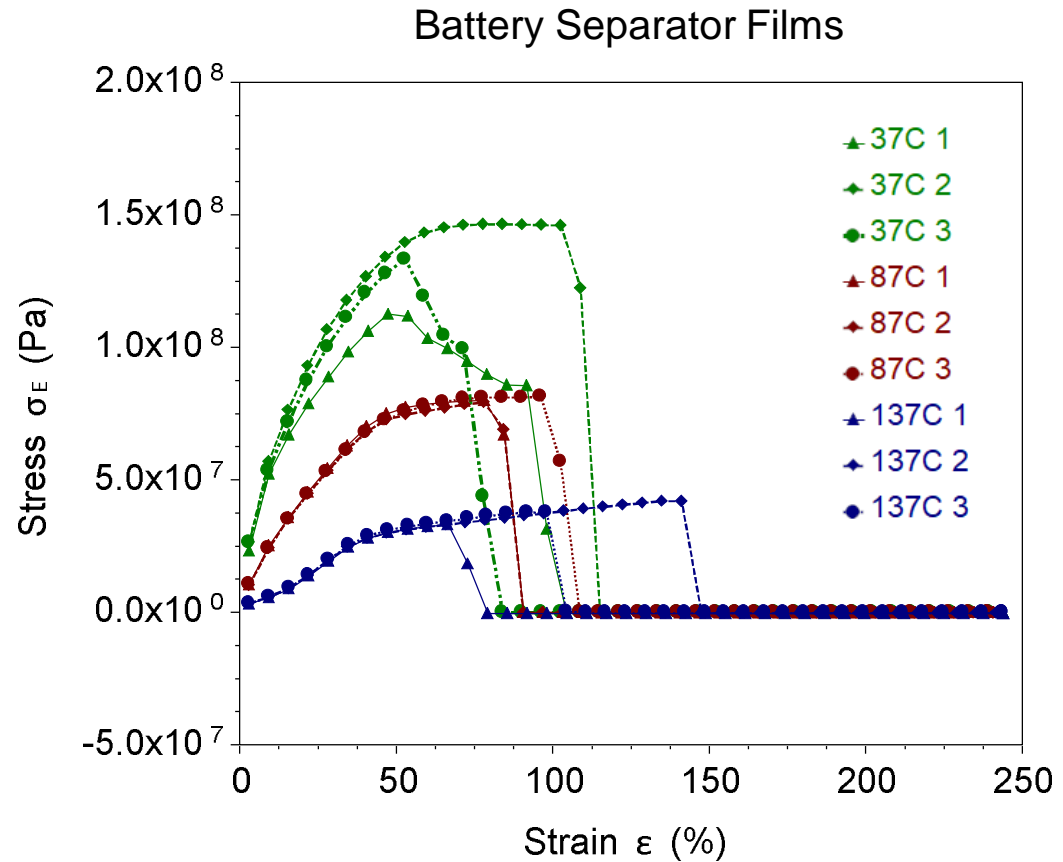
Sampling  Linear  Fast

Initial time between samples  s

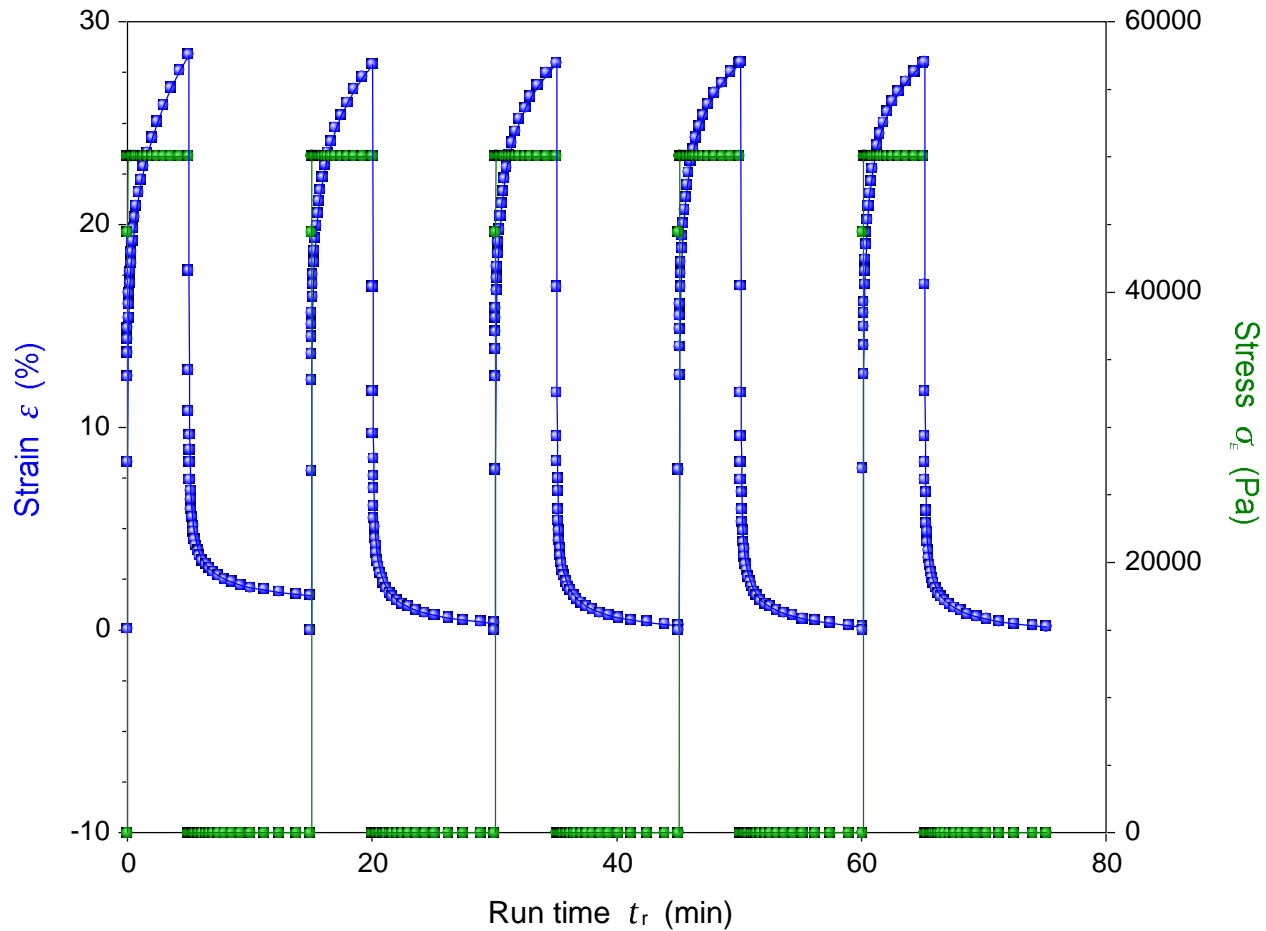
Adjust time between points

Data acquisition

Step termination



# Multi-step creep recovery: memory foam

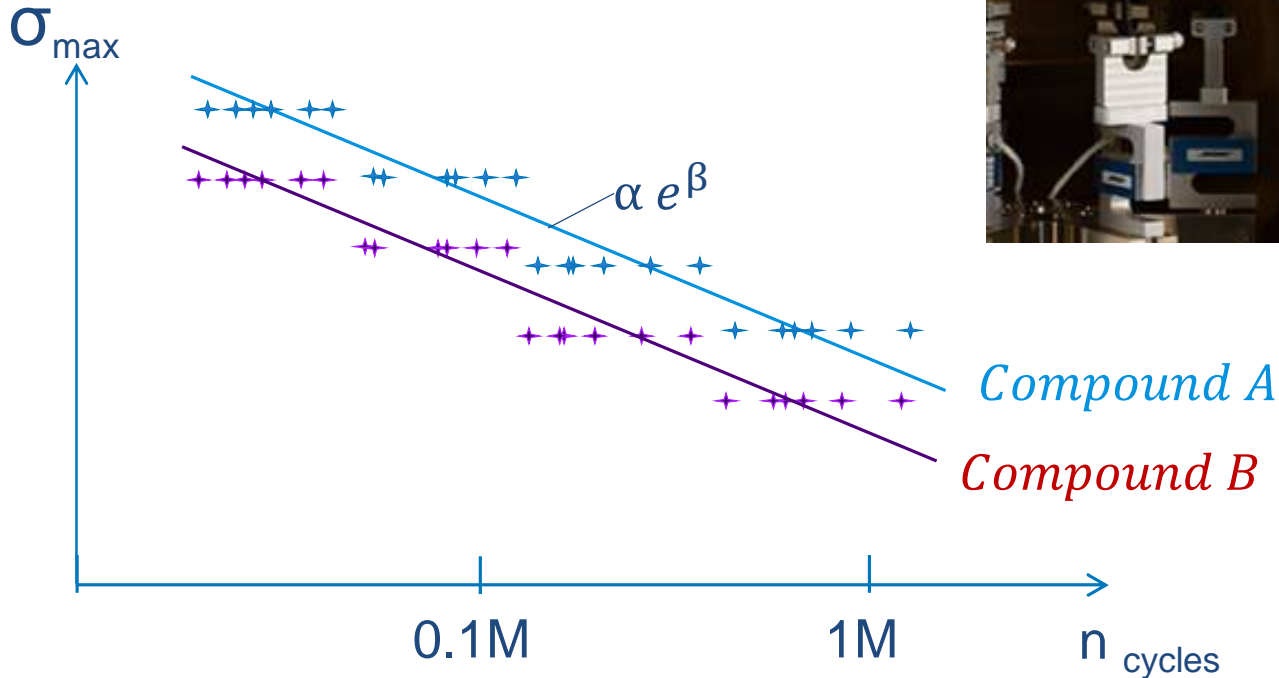




# Tensile fatigue test – Time sweep BR Rubber (Tire Rubber) Example

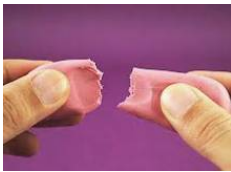
- High force DMA for rubber tire fatigue test
- Compound B has a lower life than A because it typically fails at less number of cycles when subjected to the same stress.

- Time sweep to obtain Stress-Number of cycle (SN) points
- Data is fit to exponential equation (line on plot)
- Data and exponential fit is used to compare materials

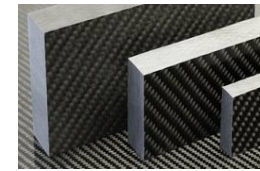
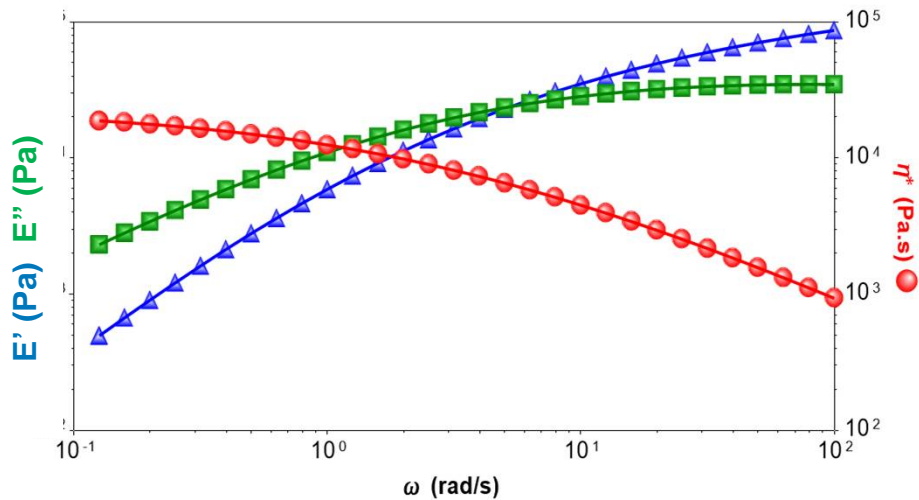


# DMA frequency sweep test

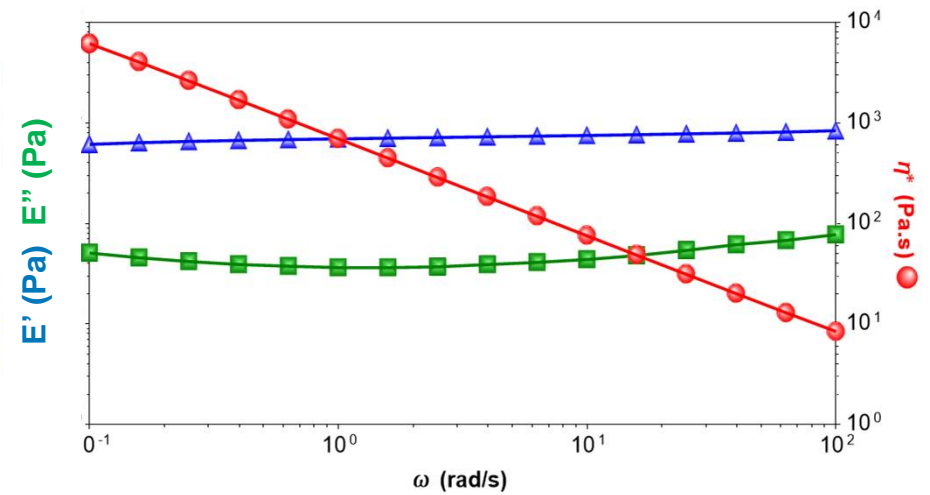
- Maximum frequency in a single test: 100-200Hz



Viscoelastic solids

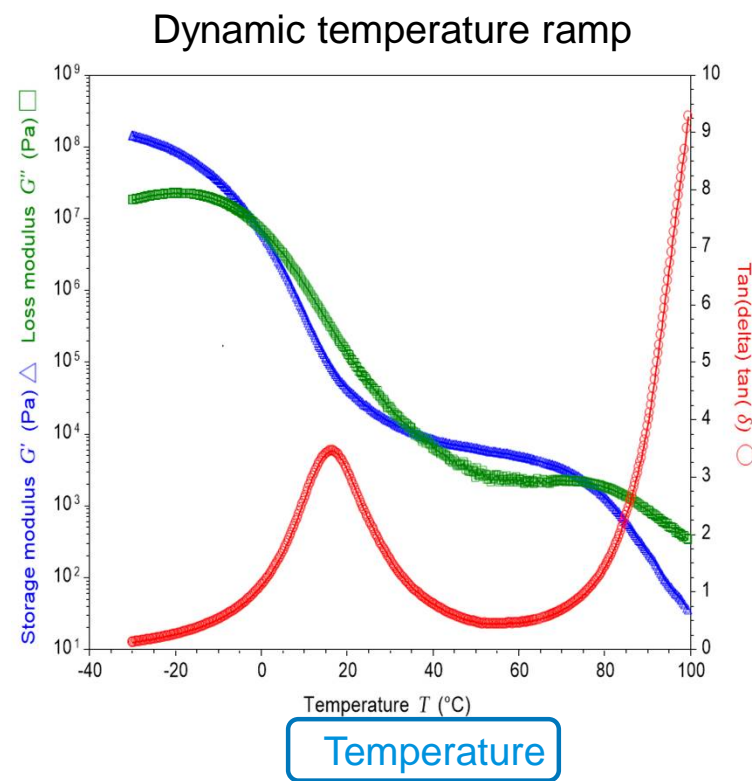
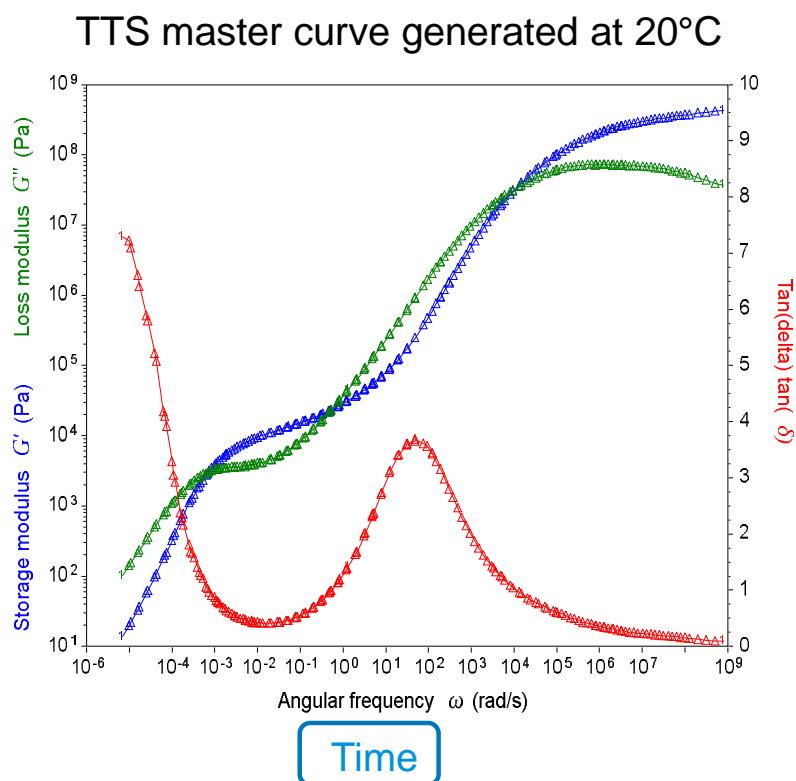


Elastic solids



# Time-Temperature Superposition (TTS)

- The viscoelastic properties of an amorphous polymer as a function of temperature is mirrored as its properties as a function of time (frequency)



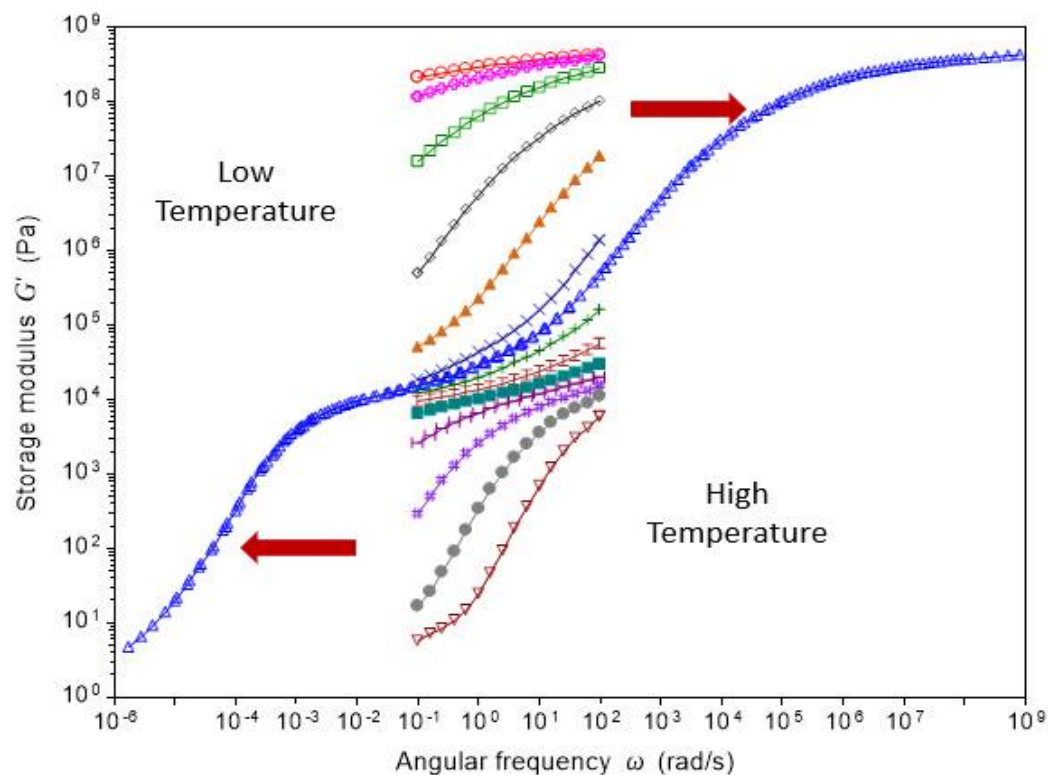
# Benefit of TTS

- TTS can be used to extend the frequency beyond the instrument's range.
- Low frequency data predicts material behavior over longer timescales that cannot be practically measured on a laboratory instrument.
- High frequency data predicts material behavior at short timescales (high-speed impact, mechanical vibrations, acoustics) that are challenging to measure accurately using an analytical instrument.
- Creep or Stress Relaxation TTS can predict behavior over longer times under static load/deformation.

- Dealy J, Plazek D. *Time-Temperature Superposition – A Users Guide*. Rheology Bulletin 2009; 78: 16
- van Gurp M, Palmen J. *Time-temperature superposition for polymeric blends*. Rheology Bulletin 1998; 67: 5.
- Cox WP and Merz EH. *Correlation of dynamic and steady flow viscosities*. Journal of Polymer Science 1958; 28: 619

# How to perform TTS analysis

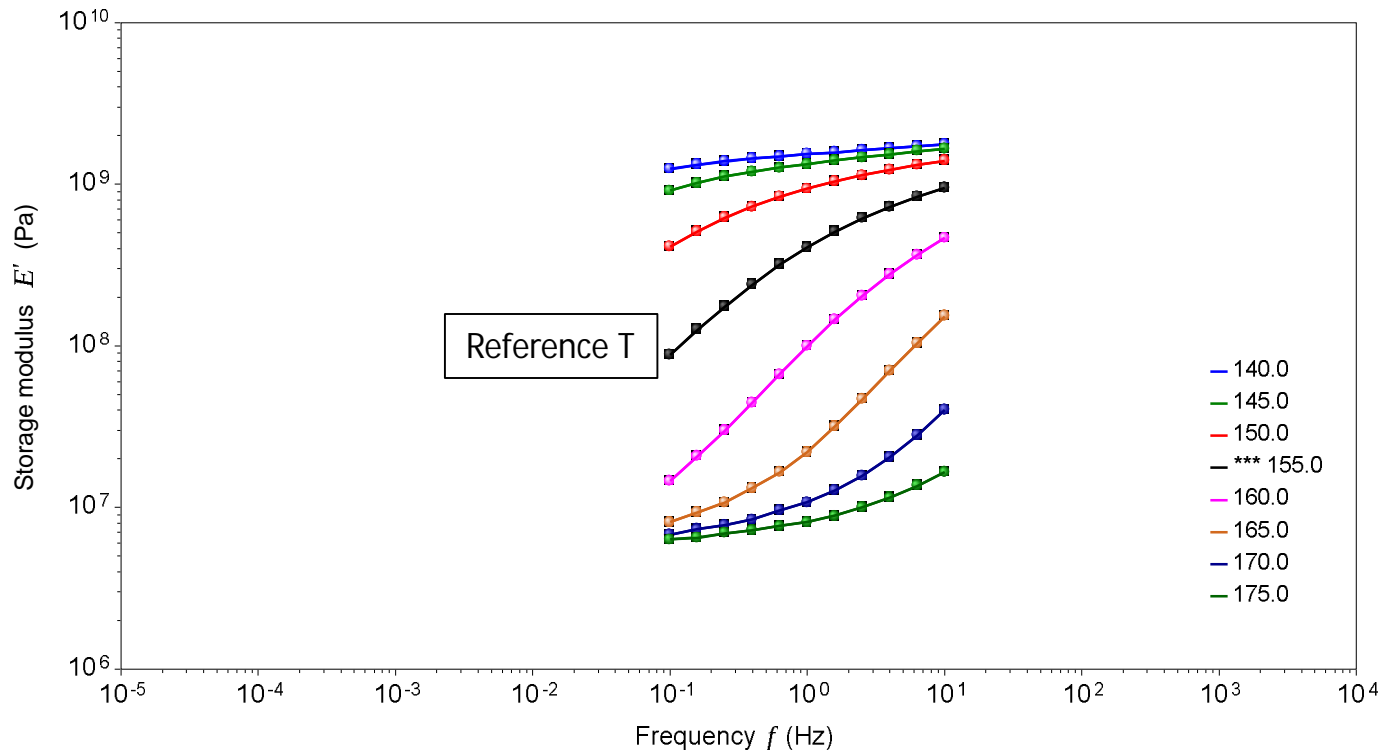
- Perform frequency sweeps at different temperature
- Extrapolates properties to time scales outside the instrumental range



- Frequency sweep data collected under different temperature steps can be shifted along the x-axis.
- Access to a wide range of frequency or time scales
- Predict properties outside of instrument capability
- TTS can be applied to both dynamic and transient measurements

# TTS example: shifting of individual curves

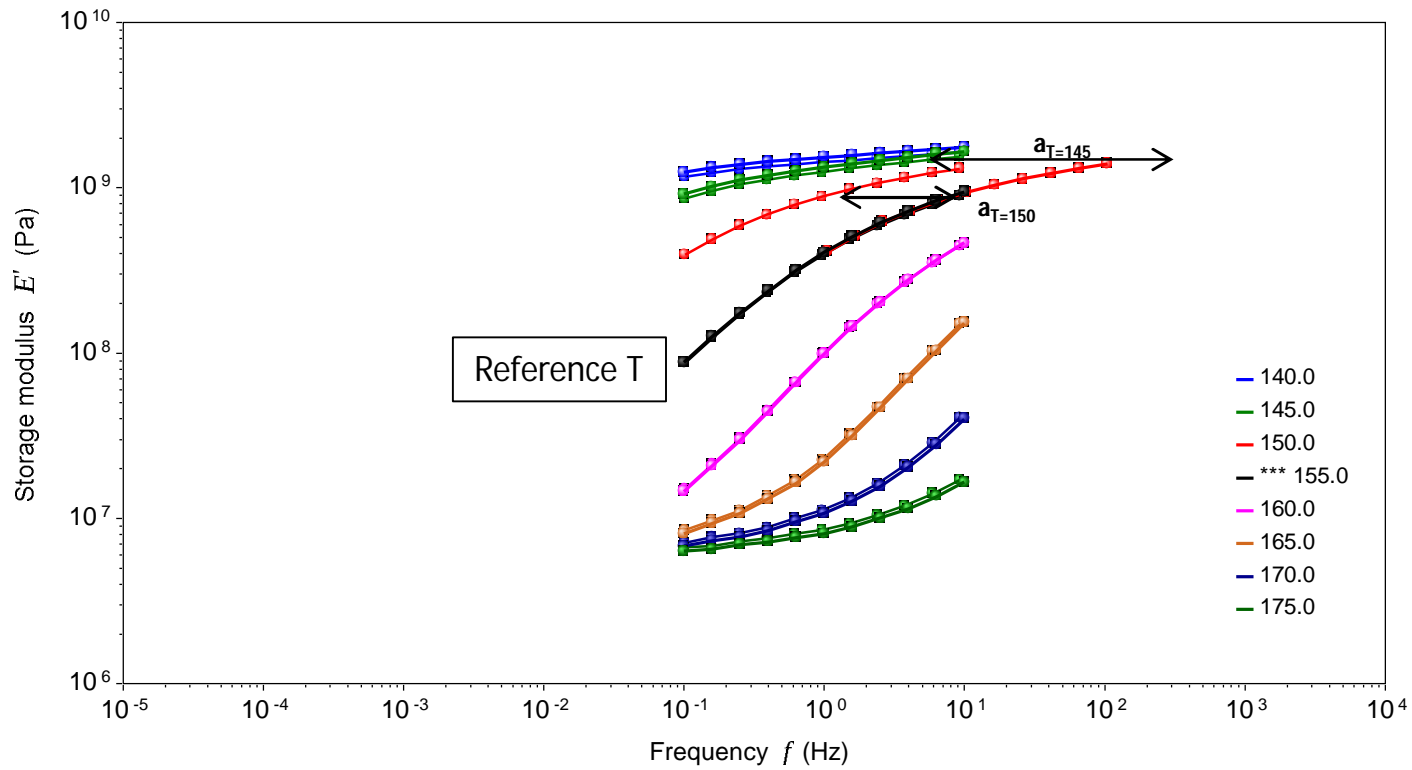
- Generating frequency sweep data at different temperature steps
- Select your reference temperature (e.g. 155°C)



- Shifts can be performed automatically in TRIOS.  
Refer to <http://www.tainstruments.com/tts-and-trios-software/>

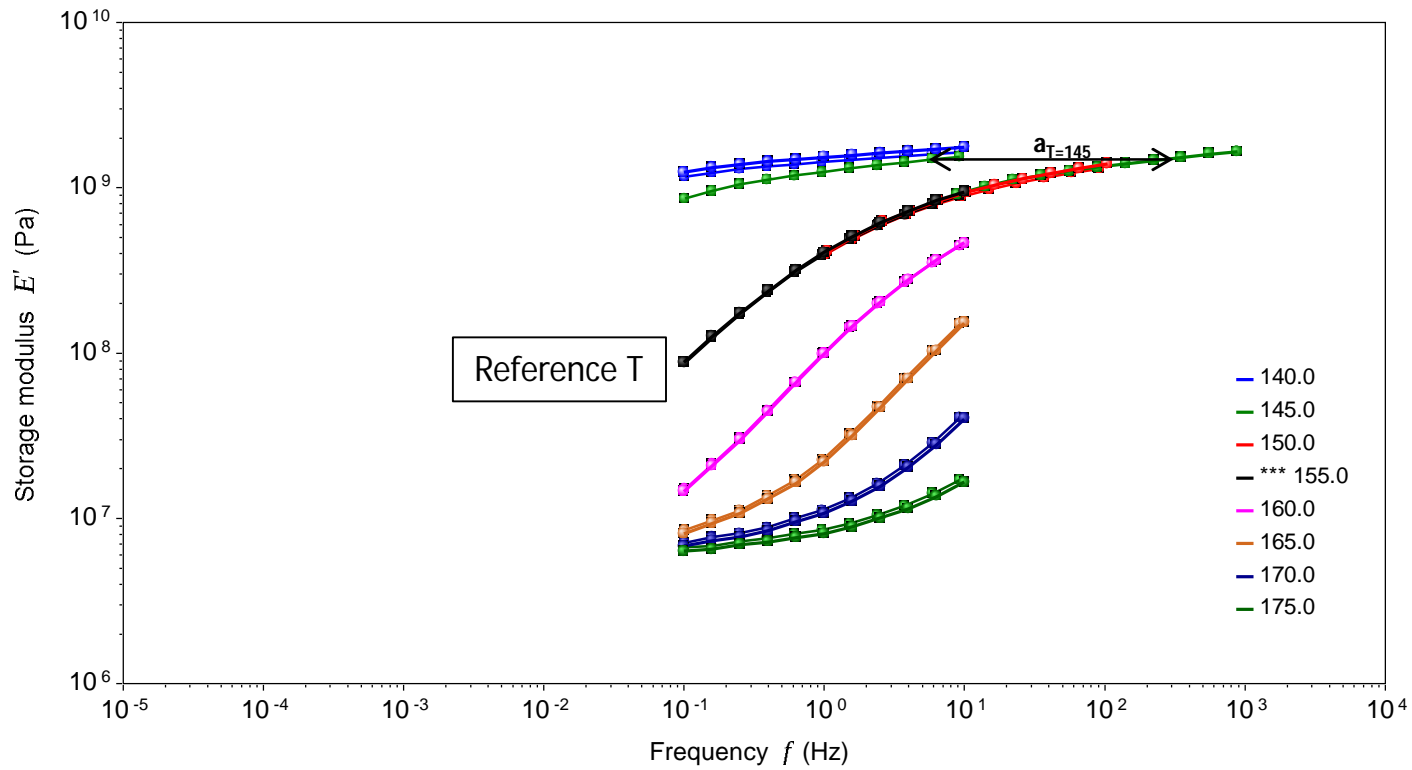
# TTS example: shifting of individual curves

- Low temperature data shift to higher frequencies



# TTS example: shifting of individual curves

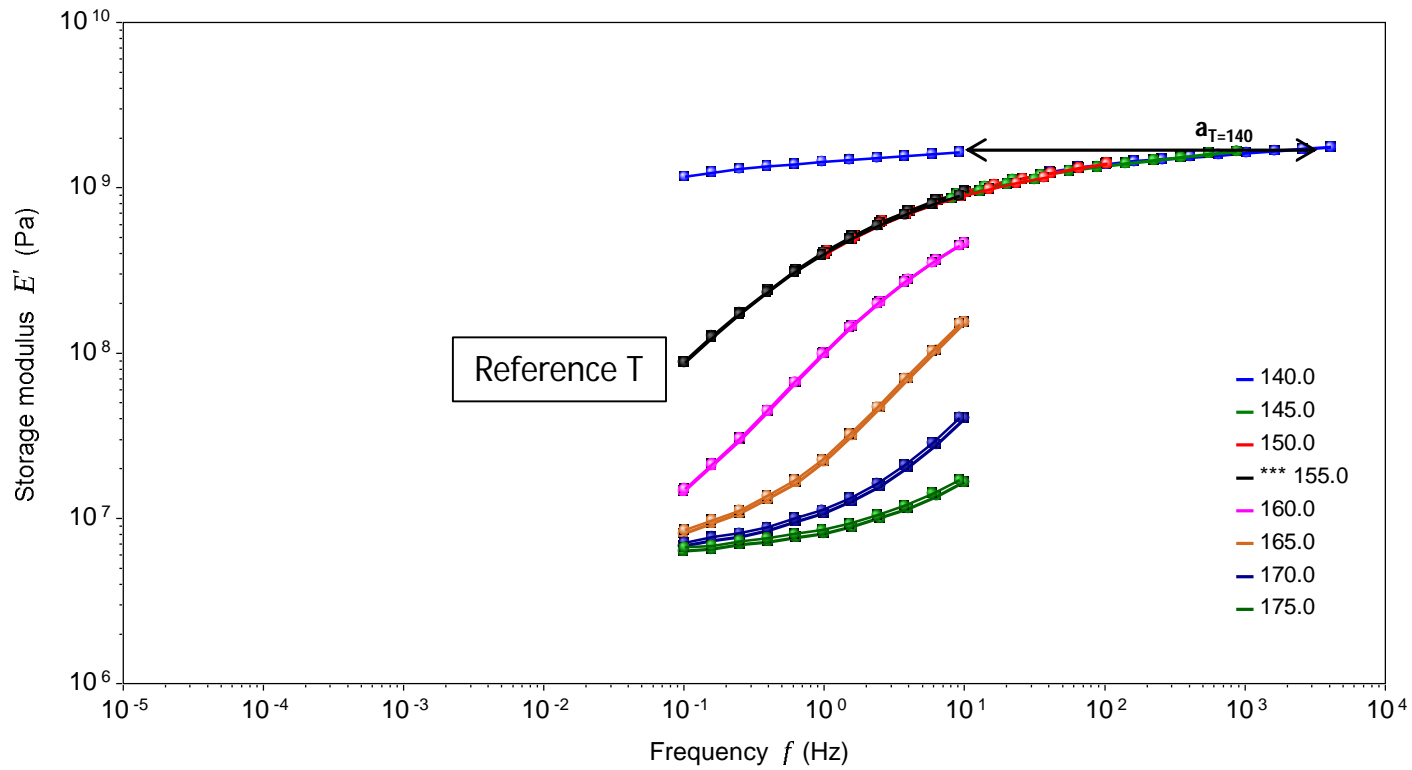
- Low temperature data shift to higher frequencies





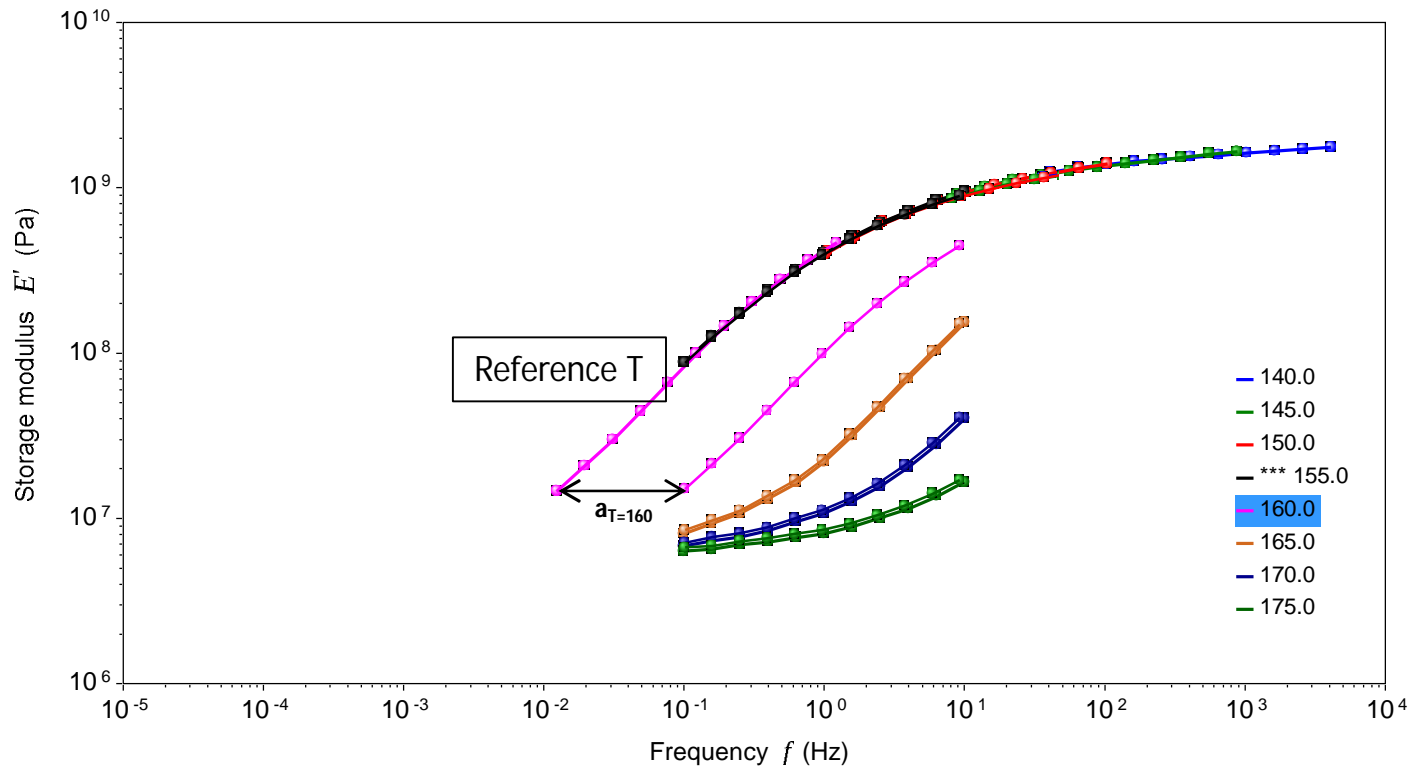
# TTS example: shifting of individual curves

- Low temperature data shift to higher frequencies



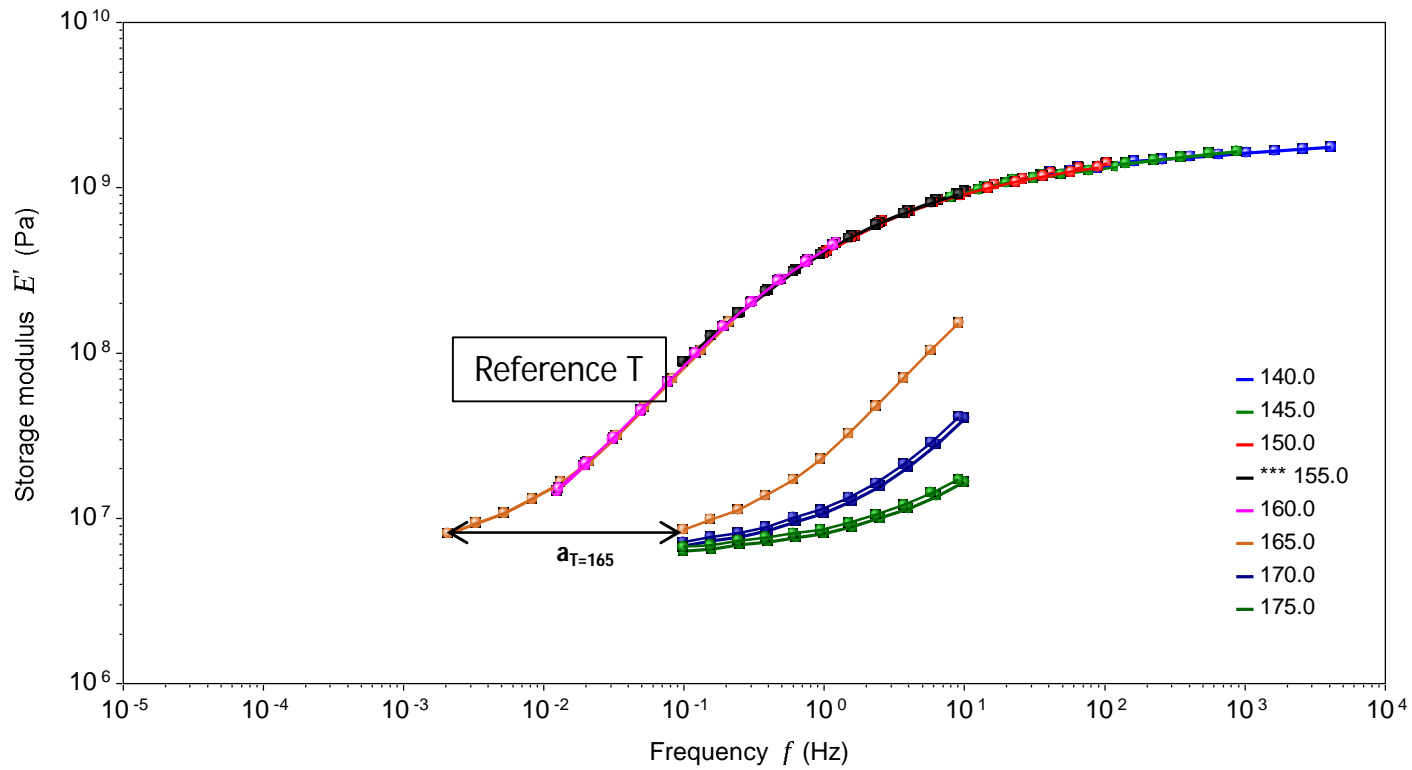
# TTS example: shifting of individual curves

- High temperature data shift to lower frequencies



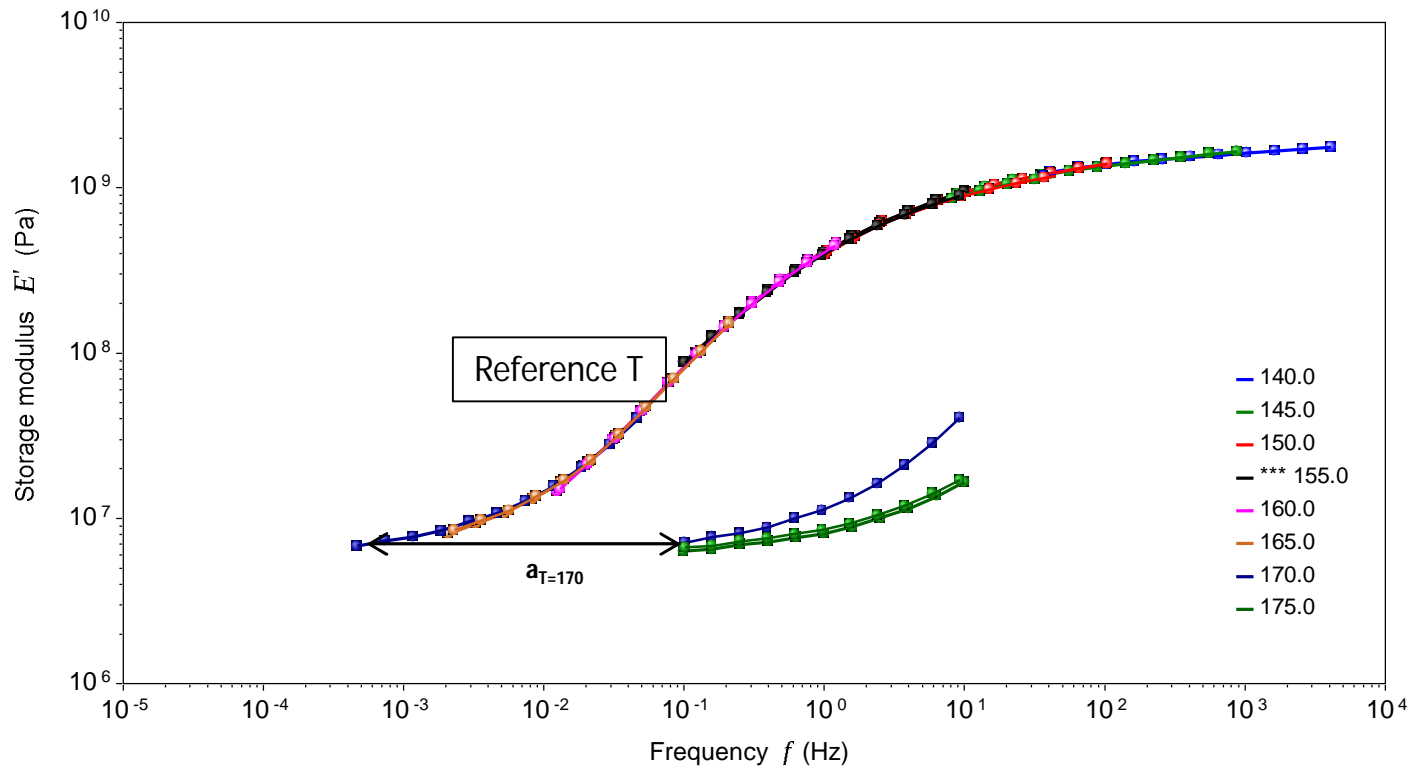
# TTS example: shifting of individual curves

- High temperature data shift to lower frequencies



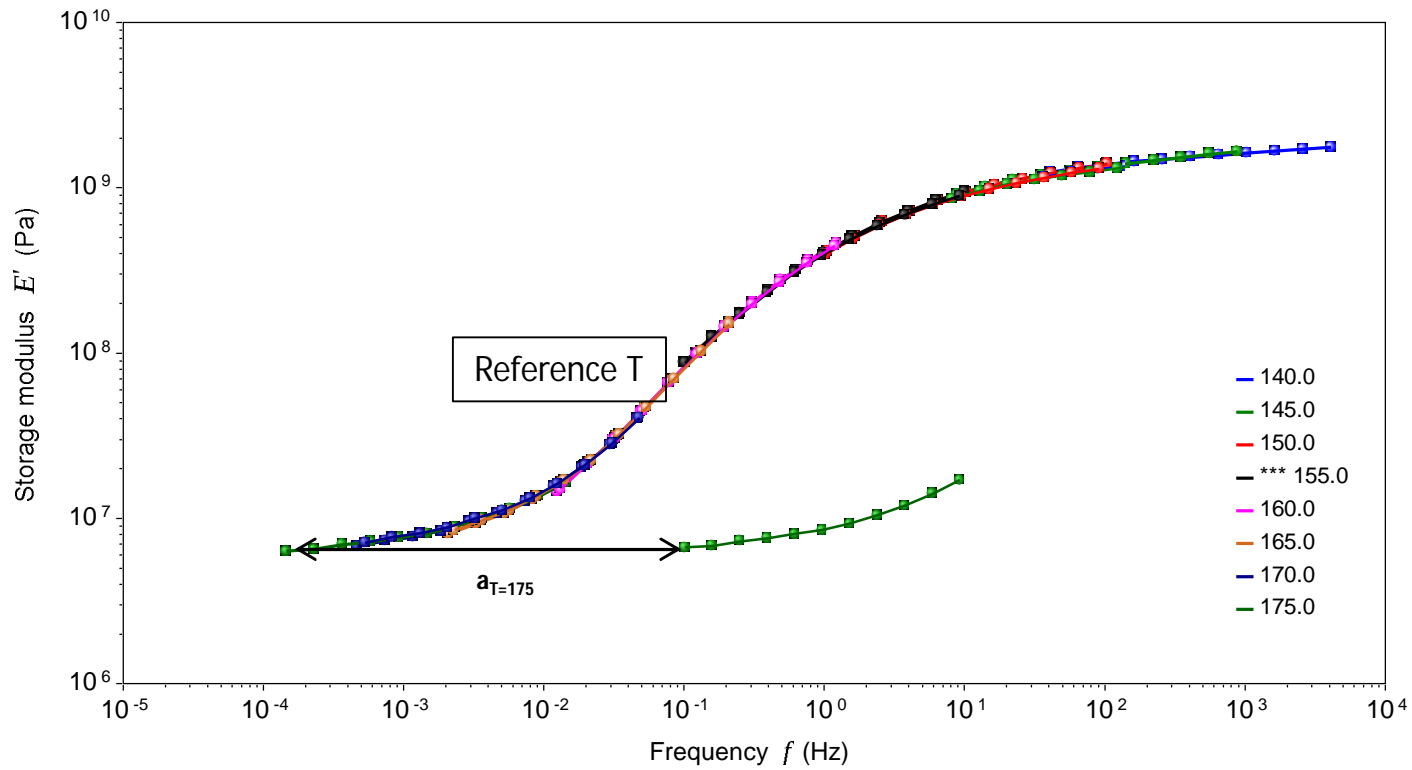
# TTS example: shifting of individual curves

- High temperature data shift to lower frequencies



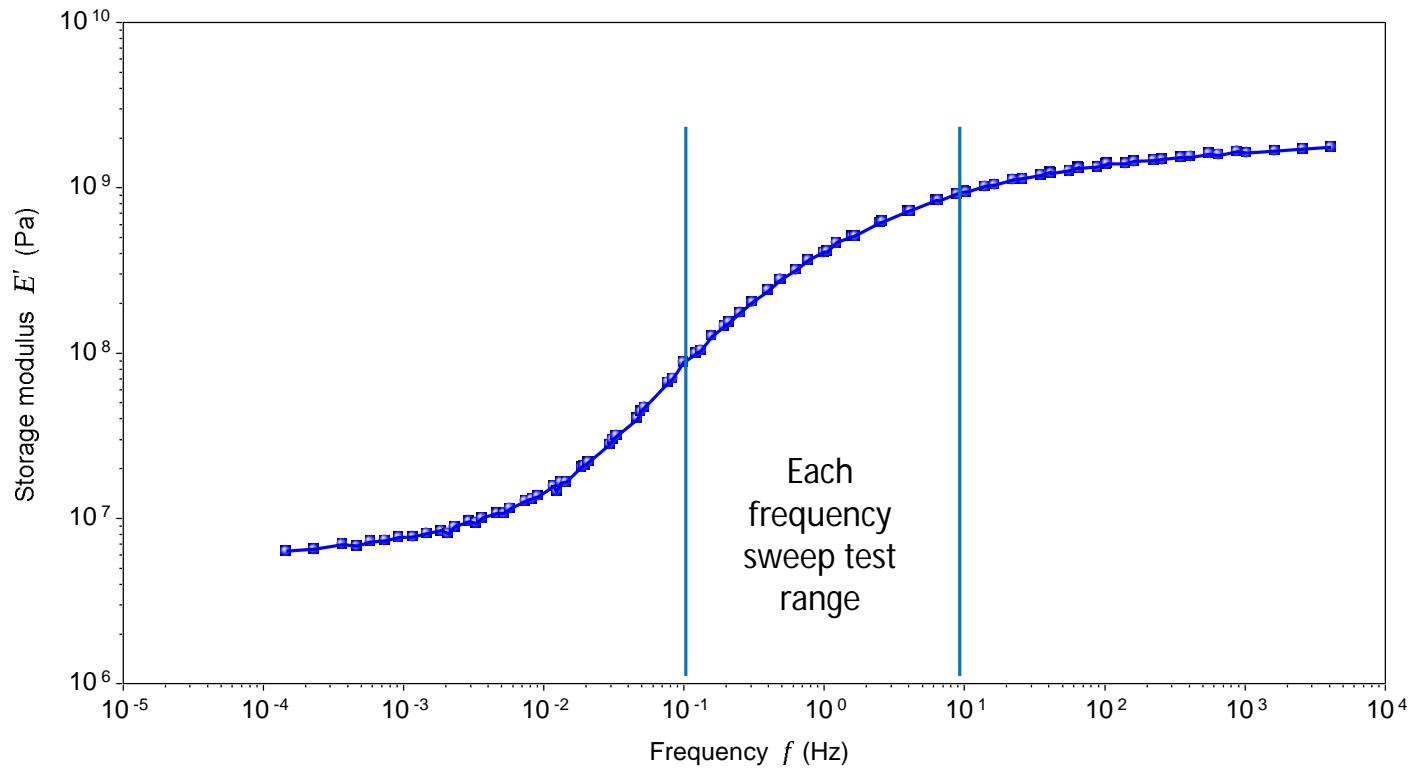
# TTS example: shifting of individual curves

- High temperature data shift to lower frequencies

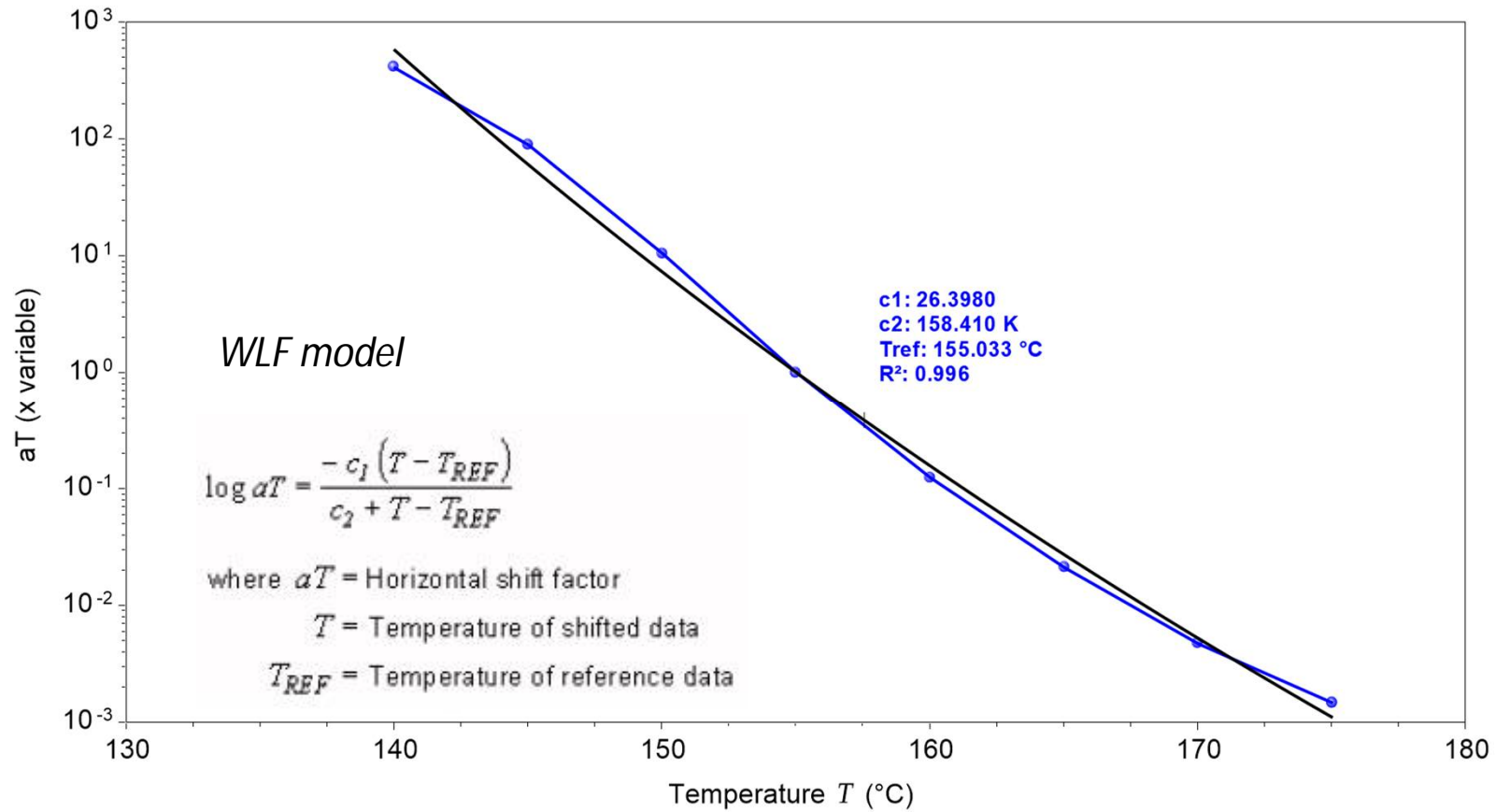


# TTS example: shifting of individual curves

- TTS Master Curve using 155°C as reference



# Shift Factors $aT$ vs. Temperature



# WLF or Arrhenius Equations

- Master Curves can be generated using shift factors derived from the Williams, Landel, Ferry (WLF) model

$$\log a_T = -c_1(T-T_0)/(c_2+(T-T_0))$$

$a_T$  = temperature shift factor       $T_0$  = reference temperature

$c_1$  &  $c_2$  = constants from curve fitting

Generally,  $c_1=17.44$  &  $c_2=51.6$  when  $T_0 = T_g$

- The Arrhenius model works better if
  - $T > T_g+100^\circ\text{C}$ ; or  $T < T_g$  and polymer is not elastomeric
  - temperature range is small, then  $c_1$  &  $c_2$  cannot be calculated precisely

$$\ln a_T = (E_a/R)(1/T-1/T_0)$$

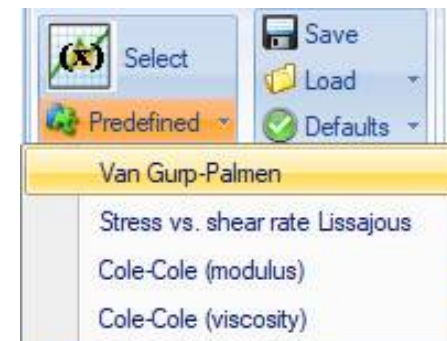
$a_T$  = temperature shift factor       $E_a$  = Apparent activation energy

$T_0$  = reference temperature       $R$  = gas constant



# How do I know if TTS works for my sample?

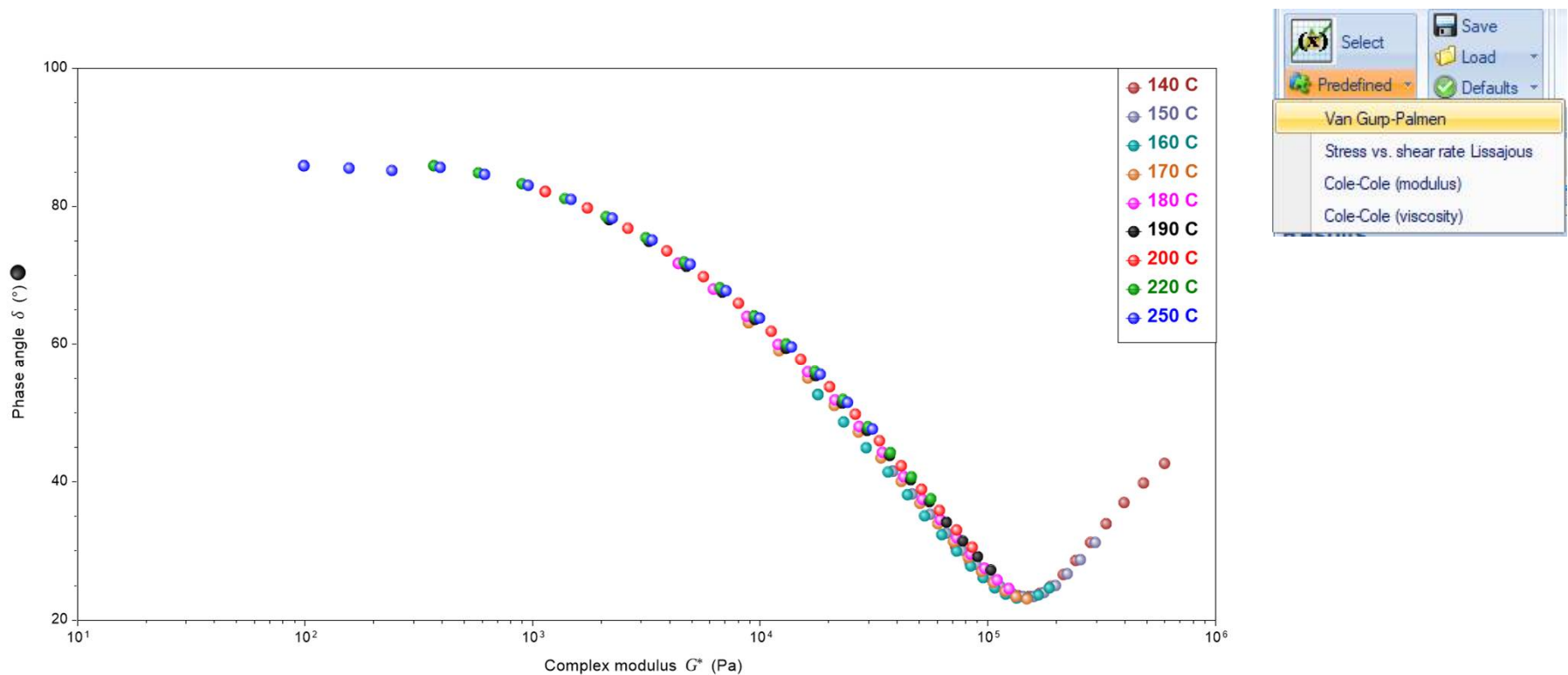
- TTS does not apply for any materials.
- Check validity of TTS
  - ✓ Van-Gurp Palmen plot should be a smooth curve
  - ✓ Cole-Cole plot should be a smooth curve
  - ✓ Shift factor ( $a_T$ ) should fit either WLF or Arrhenius equation



If any one of the above criteria are not met, TTS may not be applicable for your material.

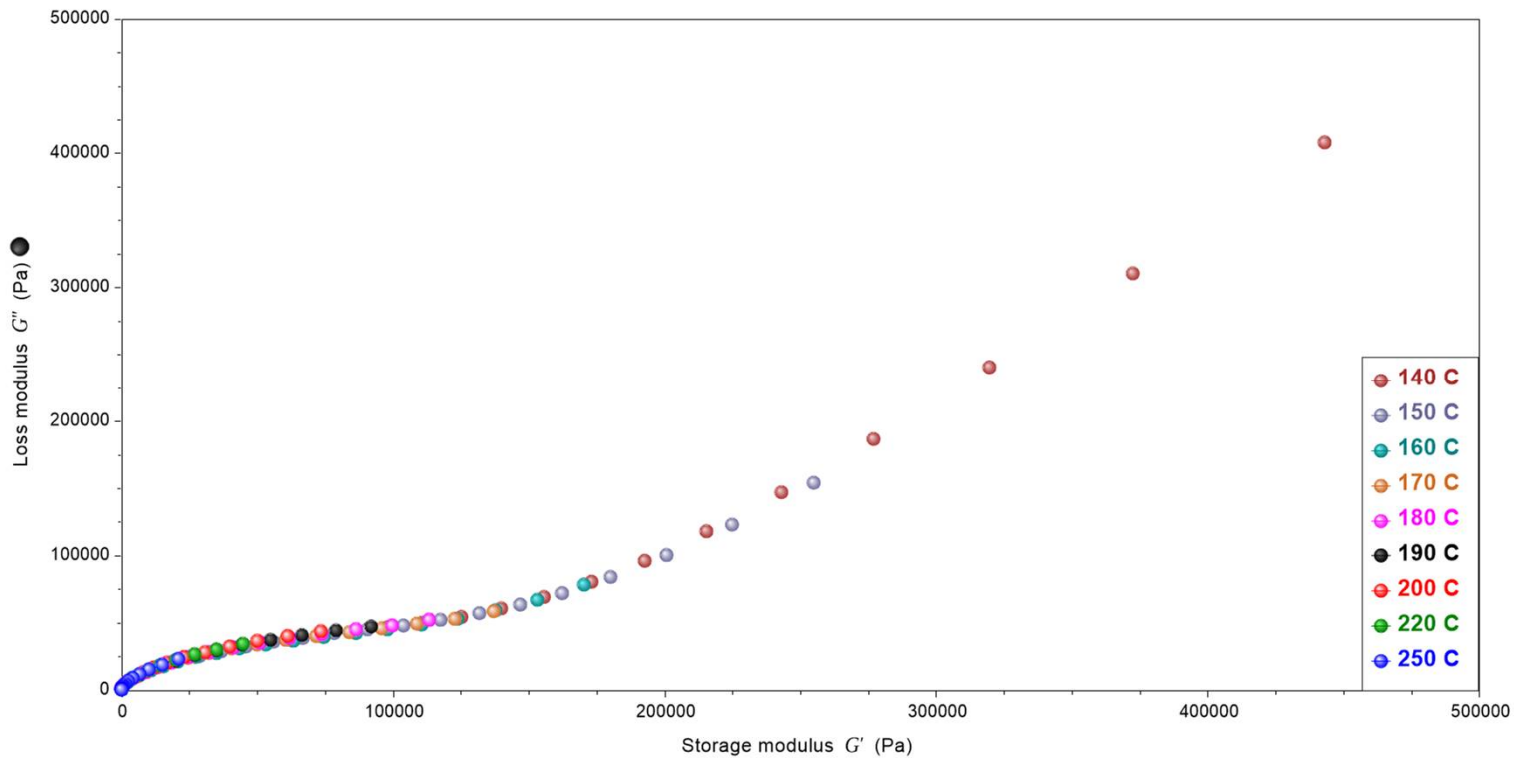
# 1. van Gorp-Palmen plot to Validate TTS

- The van Gorp-Palmen plot can be directly plotted in TRIOS to validate the application of (TTS).



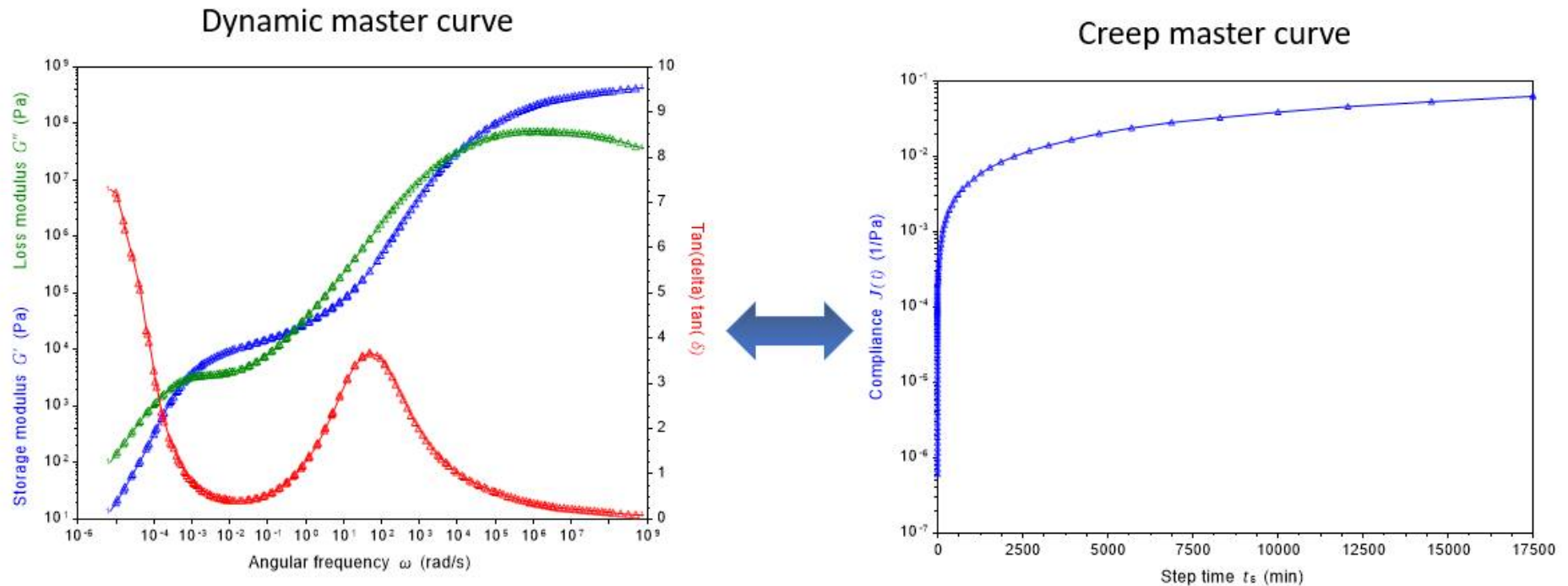
## 2. Cole-Cole plot to Validate TTS

- The Cole-Cole plot can be directly plotted in TRIOS to validate the application of (TTS).



# Transformation within Linear Viscoelastic Region Waters™ | TA Instruments

- TTS analysis can be applied to both dynamic and transient (creep and stress relaxation) measurements
- Within the linear viscoelastic region, the dynamic and transient data are inter-convertible



Waters™



Philadelphia Short Course: Day II

## Section VI: DMA Troubleshooting

***Terri Chen, PhD***  
***Principal Application Scientist***  
***TA Instruments – Waters LLC***

# Factors that influence measurement results

## Primary measurements

- Force
- Displacement
- Temperature

### Check list

- Instrument calibrations
- Thermocouple position

## Geometry

- Clamp
- Sample size
- Sample loading
- Sample integrity

### Check list

- Clamp calibrations
- Proper loading torque/force
- Sample uniformity and thermal stability
- Bad contact or sample bending and twisting

## Test Parameters

### Check list

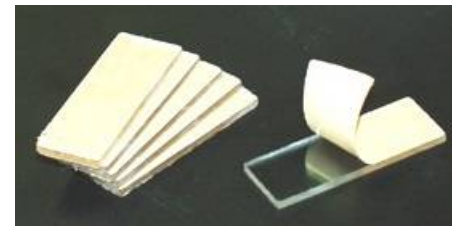
- Loading force
- Proper force track
- Equilibration time
- Heating rates
- Amplitude
- Frequency

# Instrument and clamp

- Periodically calibrate the instrument following the online help manual
- Perform clamp calibration every time when attaching a new clamp on the instrument
  - <http://www.youtube.com/user/TATechTips>
- Perform confidence verification check using polycarbonate provided by TA Instruments



p/n: 984309.901

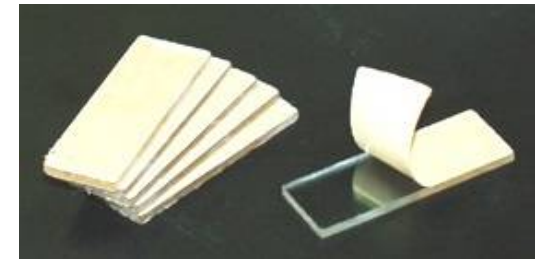


p/n: 982165.903

# DMA confidence check - polycarbonate

- Load Polycarbonate (L  $\approx$  17.5, w  $\approx$  12.85, t  $\approx$  1.6mm)
- Use Single Cantilever Clamp
  - 20-30 micrometer amplitude
  - 1 Hz frequency
- Storage Modulus at Room Temperature  
E' = 2.35 GPa (2350 MPa) +/- 5%
- Tan Delta at Room Temperature  
Tan  $\delta$  < 0.01
  
- Transition Temperature  
Tan  $\delta$  peak between 155-160°C @ 1Hz, 3-5°C/min  
E'' peak will be about 5°C lower

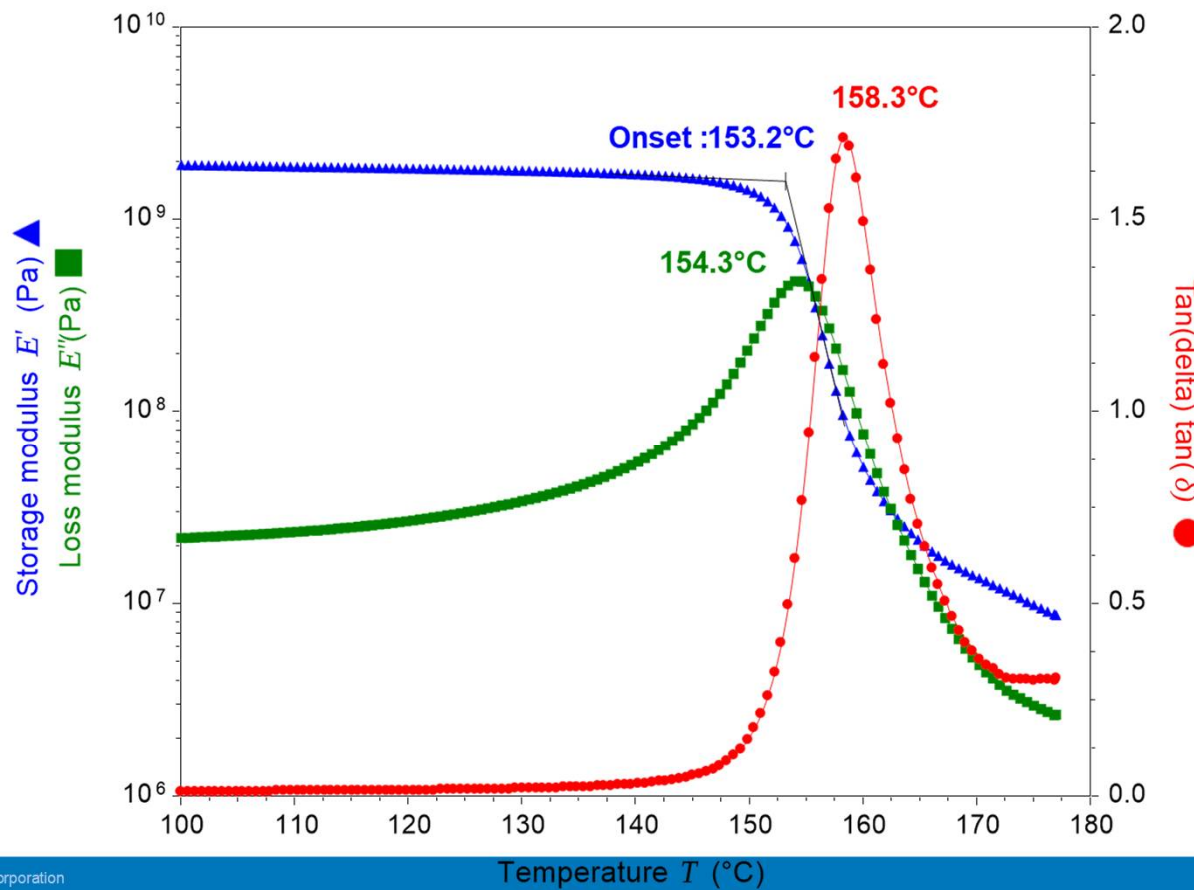
p/n: 982165.903



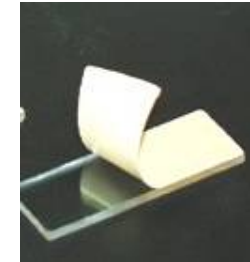


# Temp ramp on polycarbonate

- Available from TA for Instrument verification



PC sample

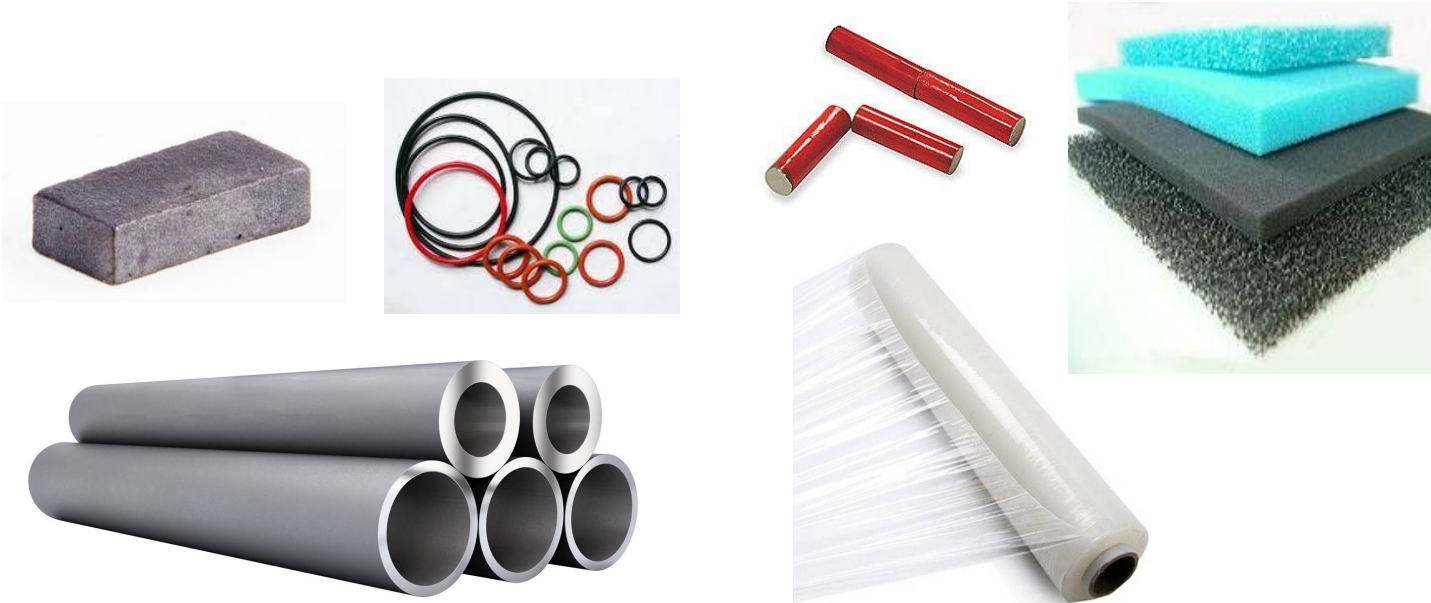


p/n: 982165.903

Clamp:  
single cantilever  
Temperature:  
ambient to 180°C  
Heating rate: 3°C/min  
Frequency: 1 Hz  
Amplitude: 20  $\mu$ m

# Sample preparation – the key to get good data

- DMA measurement results are highly depending on the quality of sample preparation
- Sample flatness and uniformity have big influence on the accuracy of the test results



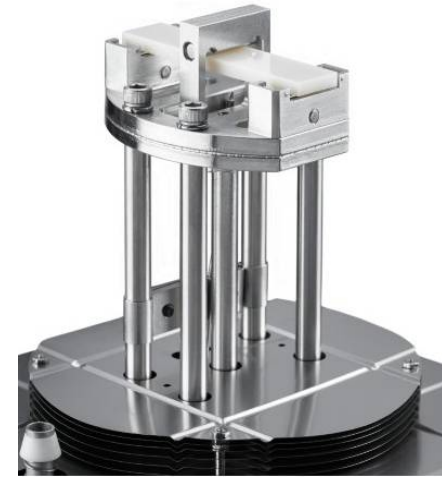
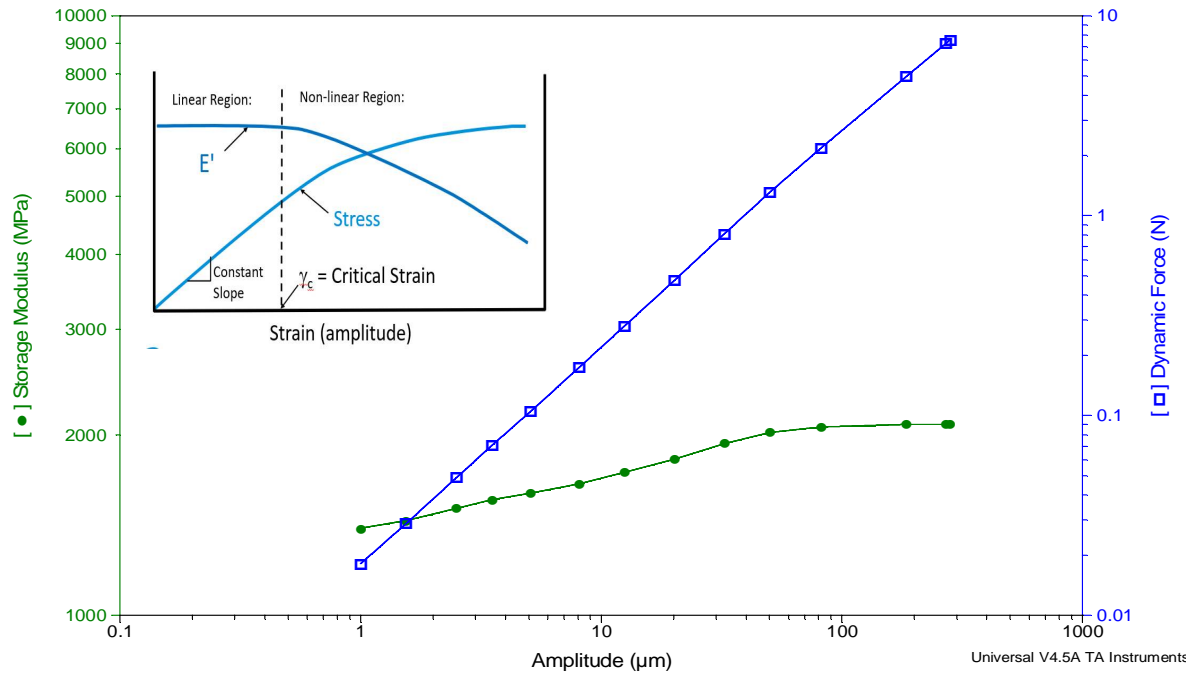
# E' Increase in a strain sweep

Why does E' increase with increasing amplitude?  
How to verify linear viscoelastic region?

Sample: ABS strain sweep  
Size: 50.0000 x 12.9100 x 3.1700 mm  
Method: Strain Sweep

DMA

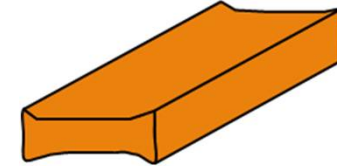
File: T:\...ABS STRAIN SWEEP.003  
Operator: TC  
Run Date: 23-Jan-2018 14:17  
Instrument: DMA Q800 V21.3 Build 96



Instrument: DMA  
Clamp: 3-p bending  
Temperature: ambient  
Amplitude: 1-500 μm  
Frequency: 1Hz

# E' Increase in a strain sweep

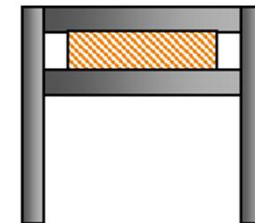
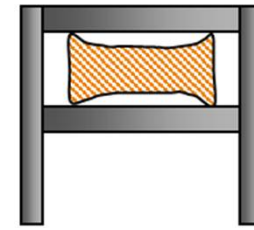
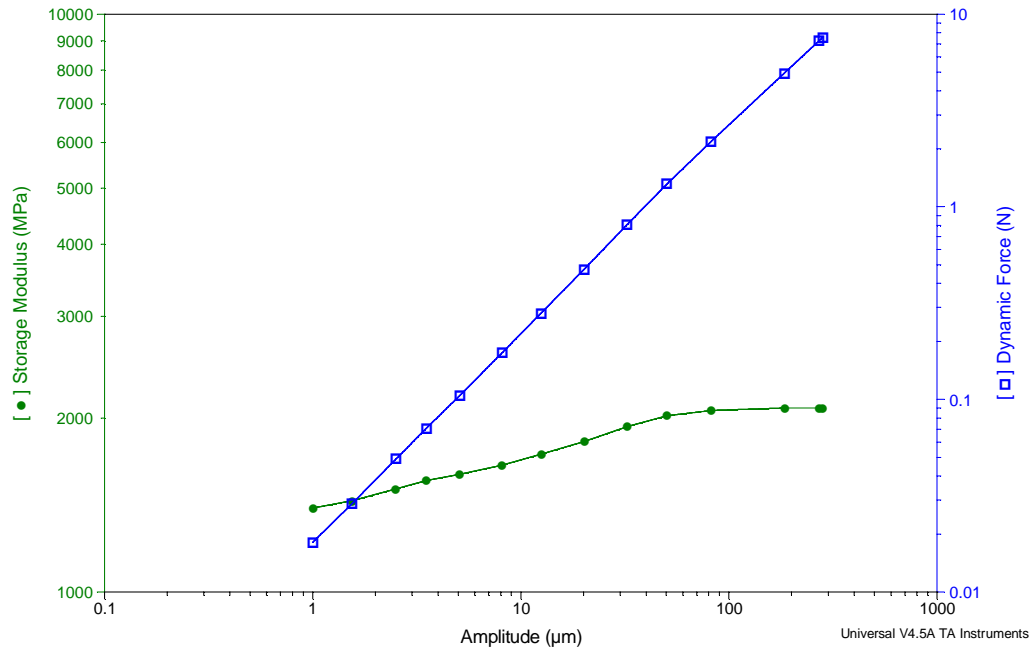
The sample is not flat and not in full contact with the clamp face.  
Solutions: (1) Prepare a flat sample  
(2) Increase force track or increase static force



Sample: ABS strain sweep  
Size: 50.0000 x 12.9100 x 3.1700 mm  
Method: Strain Sweep

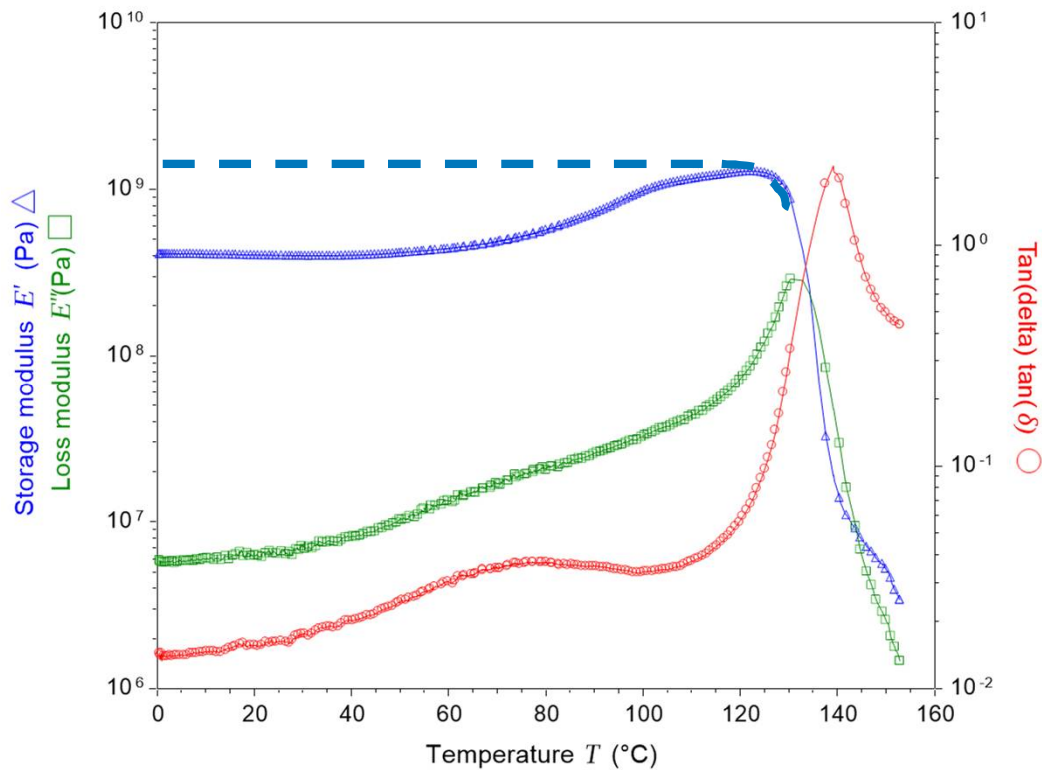
DMA

File: T:\...ABS STRAIN SWEEP.003  
Operator: TC  
Run Date: 23-Jan-2018 14:17  
Instrument: DMA Q800 V21.3 Build 96



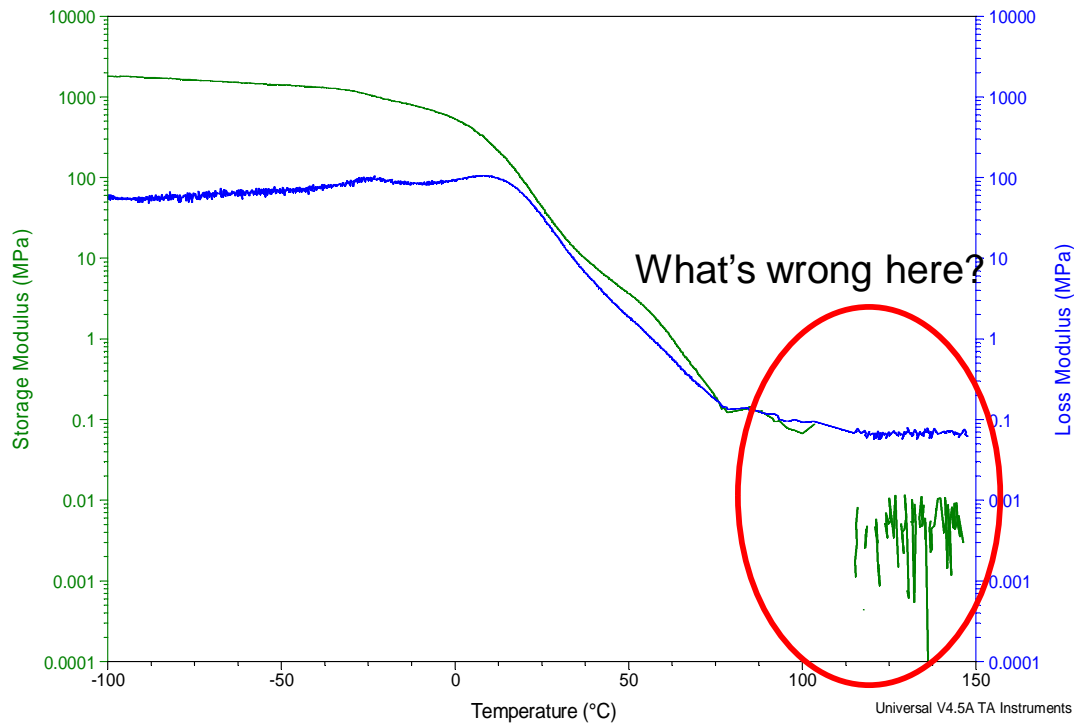
# E' increase in a temp ramp

- The E' of a material should not increase with temperature unless it is crystallized or crosslinked



# Noisy modulus after T<sub>g</sub>

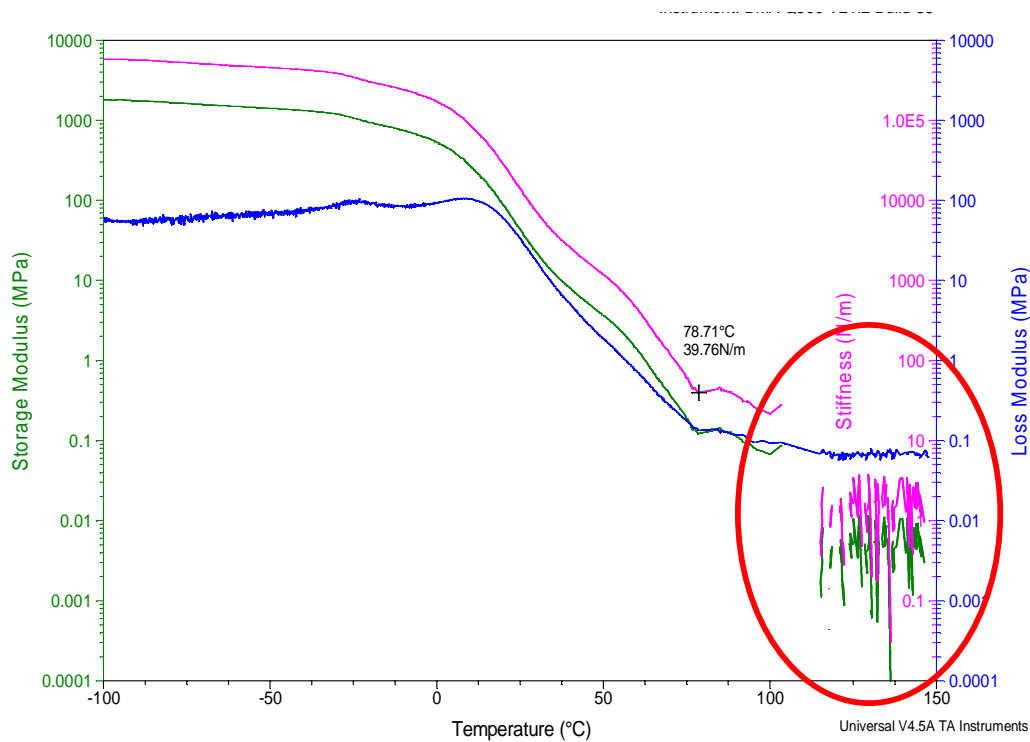
What is the problem with this data collected after T<sub>g</sub>?



Instrument: DMA  
Clamp: tension  
Temperature:  
-100°C to 150°C  
Heating rate: 3°C/min  
Frequency: 1Hz  
Amplitude: 10 μm

# Noisy modulus after T<sub>g</sub>

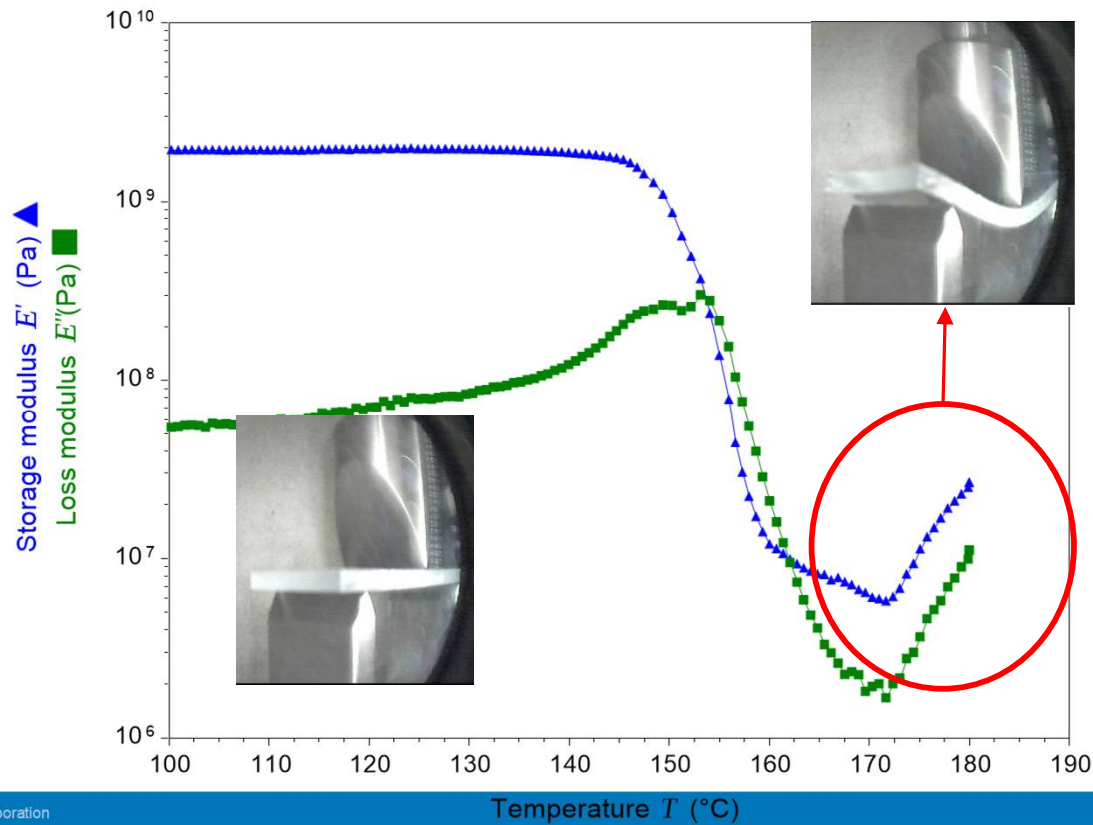
What is the problem with this data collected after T<sub>g</sub>?



Instrument: DMA  
Clamp: tension  
Temperature:  
-100°C to 150°C  
Heating rate: 3°C/min  
Frequency: 1Hz  
Amplitude: 10 μm

# Sample sagging

- Sample sagging after  $T_g$
- Solution: use cantilever clamp instead of 3-p bending

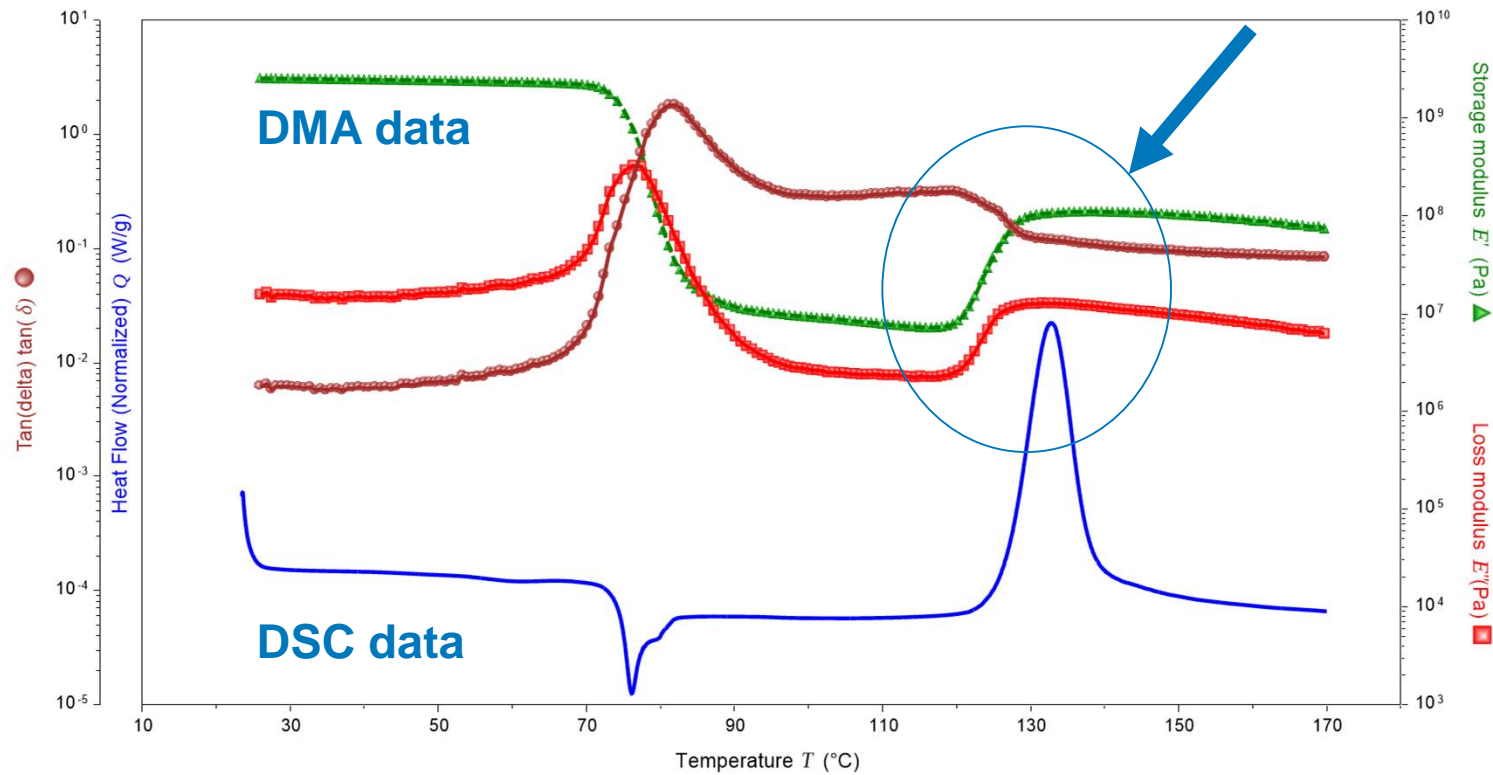


Instrument: RSA G2  
Clamp: 3-p bending  
Temperature:  
50°C to 180°C  
Heating rate: 3°C/min  
Frequency: 1Hz  
Amplitude: 10  $\mu$ m

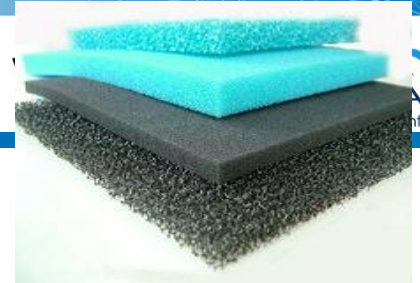


# Cold crystallization after Tg - PLA

- What causes the E' to increase after Tg?

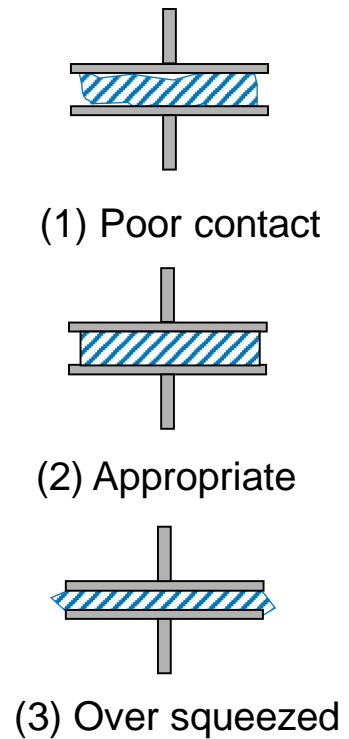
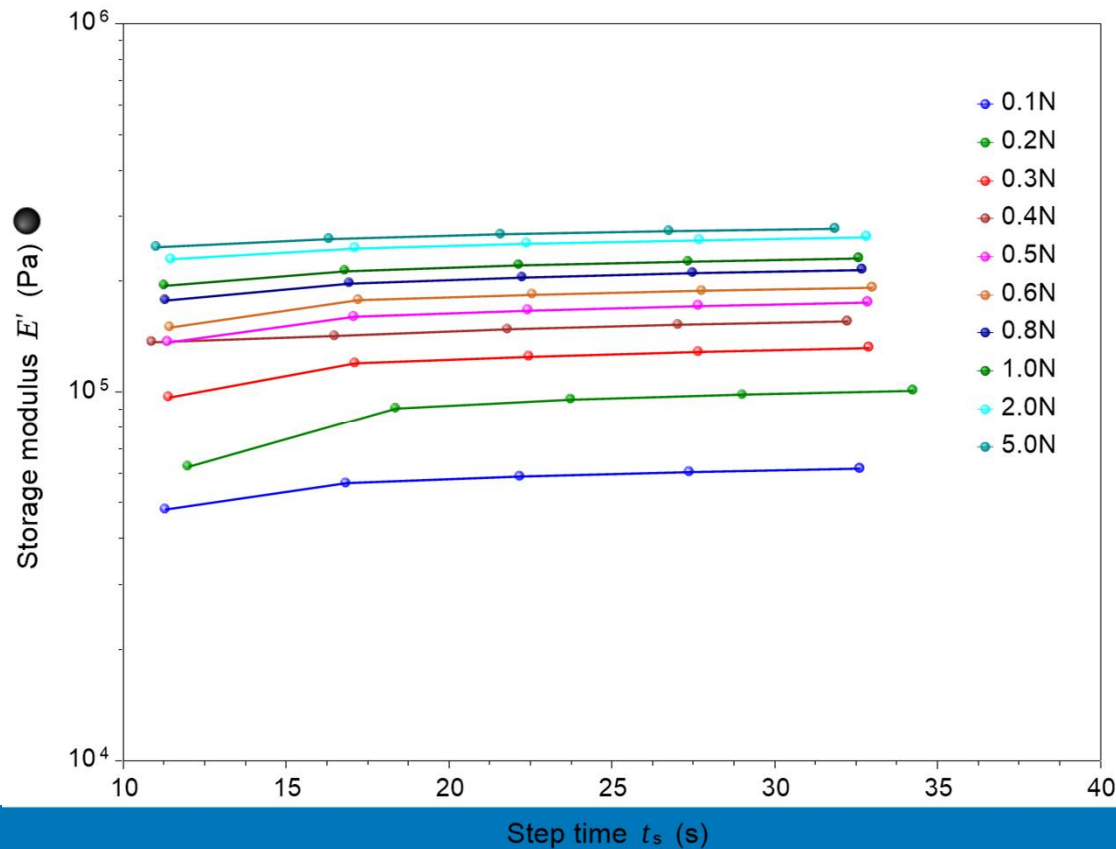


# Compression testing on foam/rubber



Question: How to measure correct modulus?

Answer: (1) Prepare regular sample (2) Apply appropriate static force



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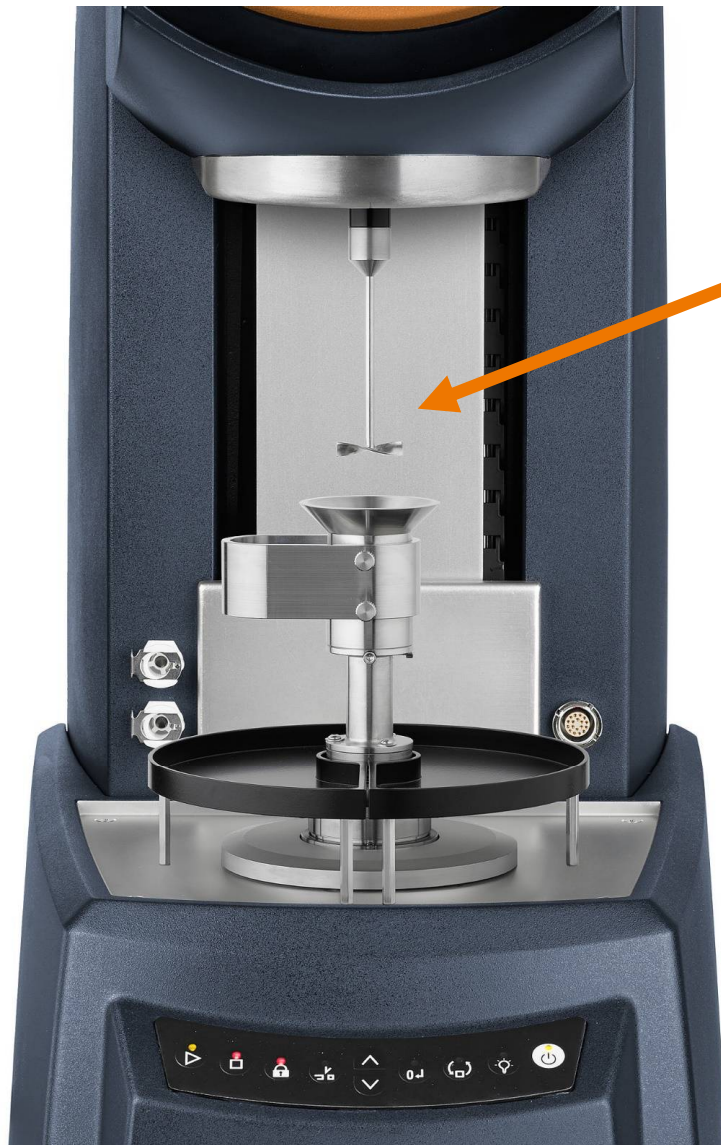
# Introduction to New Rheology Accessories

***Terri Chen, PhD***  
***Principal Application Scientist***  
***TA Instruments – Waters LLC***

## HR x0 Powder Rheology Accessory

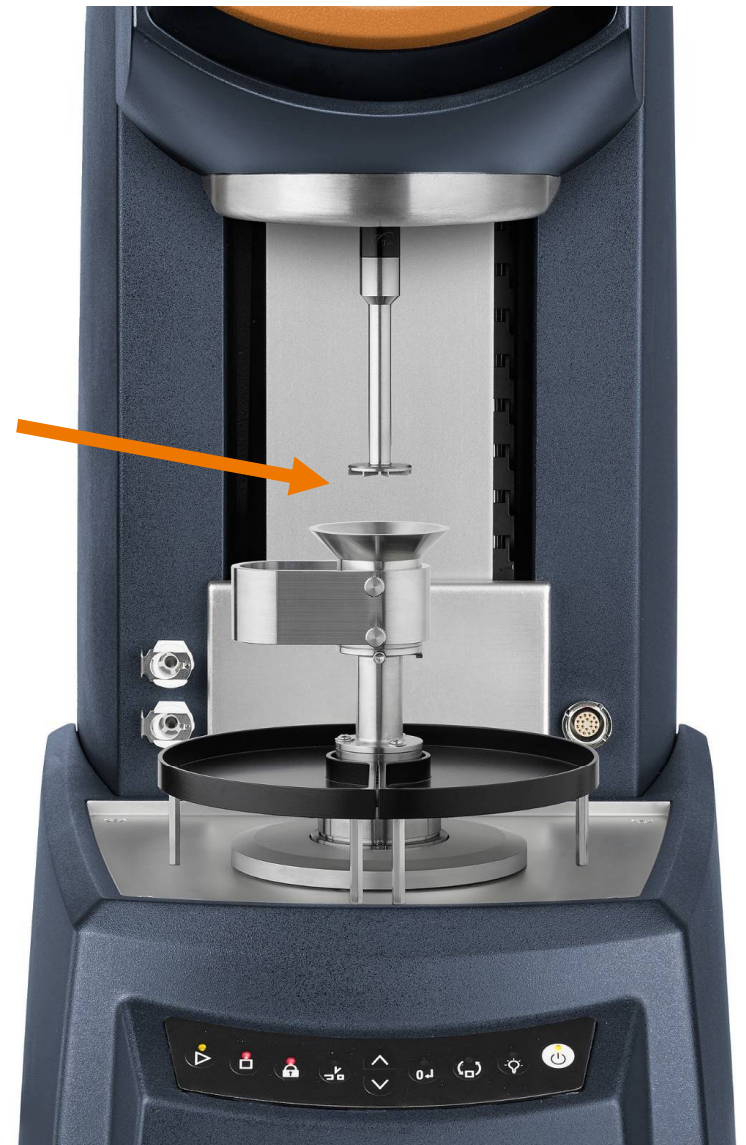
- Available on HR 10, HR20 and HR30 rheometer. Powder solution offers comprehensive powder flow analysis
  - Flowability
  - Shear
  - Wall friction (2023)
  - Compressibility (2023)
- Excellent repeatability (within 5%)
- Easy sample preparation: loading and trimming
- Integrated Smart Swap design. Accessory change in less than 10 seconds
- One click data analysis package in Trios





Flow Cell

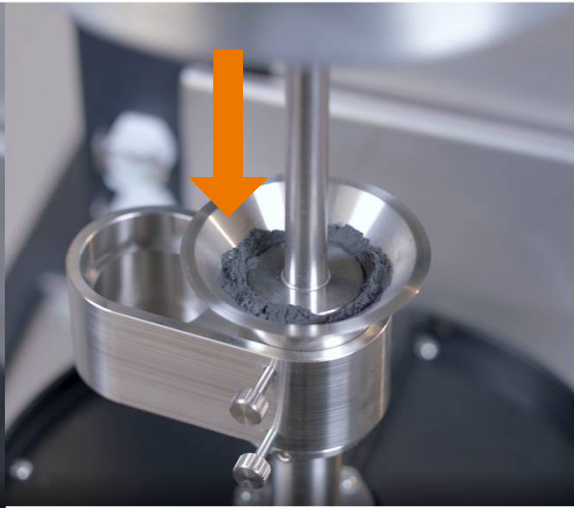
Shear Cell



## Powder Shear Cell sample preparation



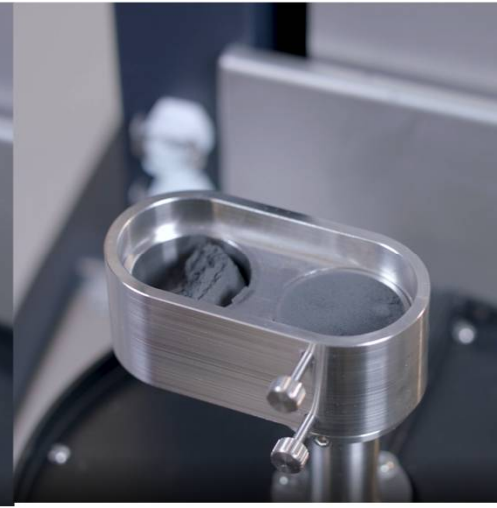
Load Sample  
>15 mL



Sample  
Consolidation



Trim Sample  
User prompt from  
the touchscreen



Start the Test

# TRIOS simplifies Powder Flowability test

1: Powder ▾ Flowability ▾

**Environmental Control**

Temperature  °C  Inherit Set Point

Soak Time  hh:mm:ss

**Test Range**

Upper gap  mm

Lower gap  mm

**Conditioning Parameters**

Tip speed  mm/s

**Unconfined Flow Parameters**

Tip speed up  mm/s

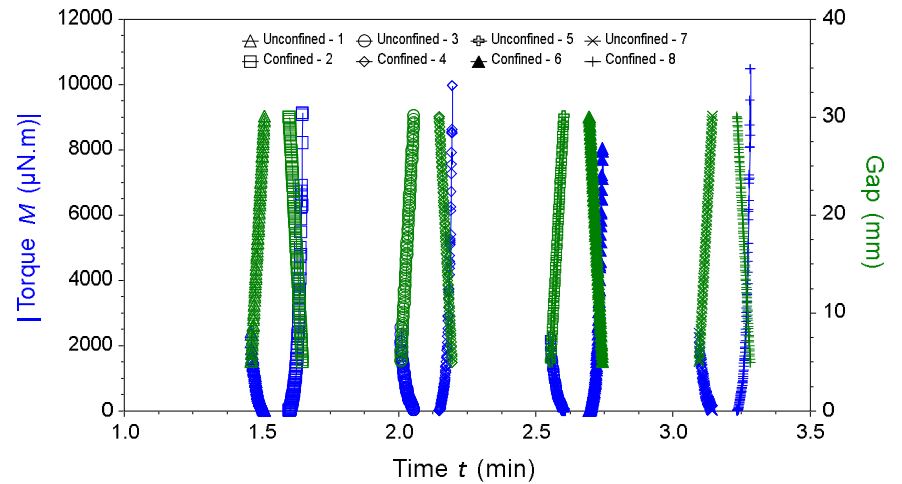
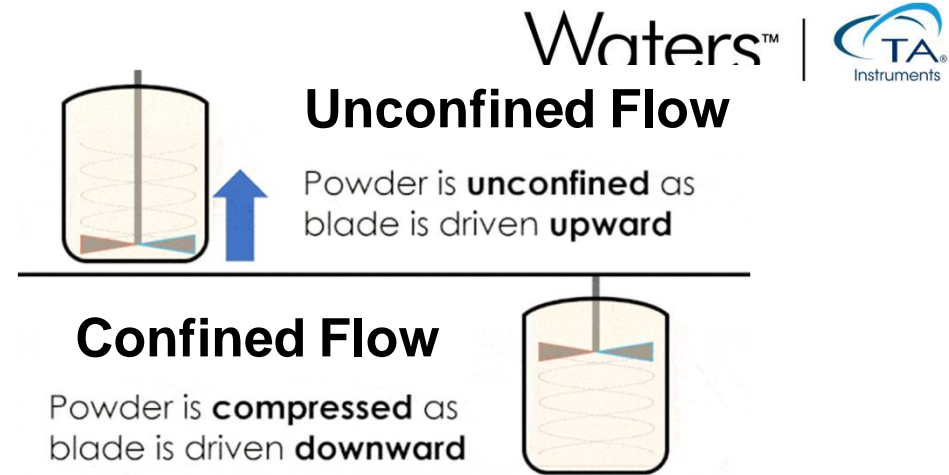
**Confined Flow Parameters**

Tip speed down  mm/s

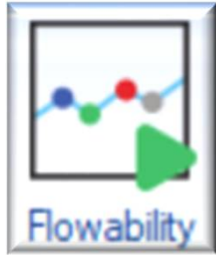
Repeat Count:



- Repeat steps – Stability Index
- Vary Tip Speed – Flow Rate Index

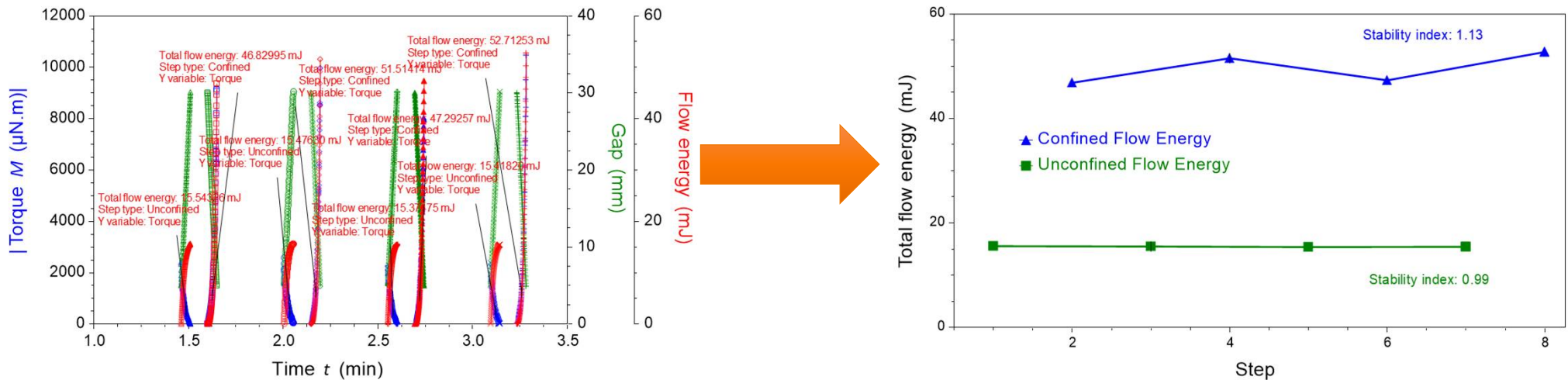


# Powder Analysis Key automates Flowability calculation



## TRIOS Powder Analysis Software key (optional)

- Powder Key Performance Indicators are **One Click away**
- Automated process saves user from complicated mathematical analysis
- Quantitative, relevant, repeatable results



$$\text{Flow Energy} = \int_{\text{Torque energy}} T * d\theta + \int_{\text{Force energy}} N * dh$$



# TRIOS simplifies Powder Shear Test

1: Powder Consolidation  
2: Powder Shear

Environmental Control  
Temperature: 25 °C  Inherit Set Point  
Soak Time: 00:00:00 hh:mm:ss

Test Parameters  
Consolidating stress: 9 kPa  
Test mode: Standard  
Maximum step duration: 00:05:00 hh:mm:ss

	Normal Stress (kPa)	Velocity (rad/s)	Duration (hh:mm:ss)
Pre-shear	9	1.0e-3	00:05:00
1	7	1.0e-	
2	6	1.0e-	
3	5	1.0e-	
4	4	1.0e-3	00:05:00
5	3	1.0e-3	00:05:00

Repeat initial pre-shear  
 Steady state detection  
 Peak detection

TRIOS Unlimited: complete customizability

## TRIOS Powder-Shear test form performs ASTM D7891 measurement

- “Pre-Shear”: Apply consolidating normal stress (9 kPa), pre-shear until steady state
- “Shear” Reduce normal stress, shear until yield
- Repeat consolidating pre-shear
- Repeat shear with decreasing normal stress



# TRIOS simplifies Powder Shear Test

1: Powder Consolidation  
 2: Powder ▾ Shear ▾

Environmental Control  
 Temperature 25 °C  Inherit Set Point  
 Soak Time 00:00:00 hh:mm:ss

Test Parameters  
 Consolidating stress 9 kPa  
 Test mode Standard ▾  
 Maximum step duration 00:05:00 hh:mm:ss

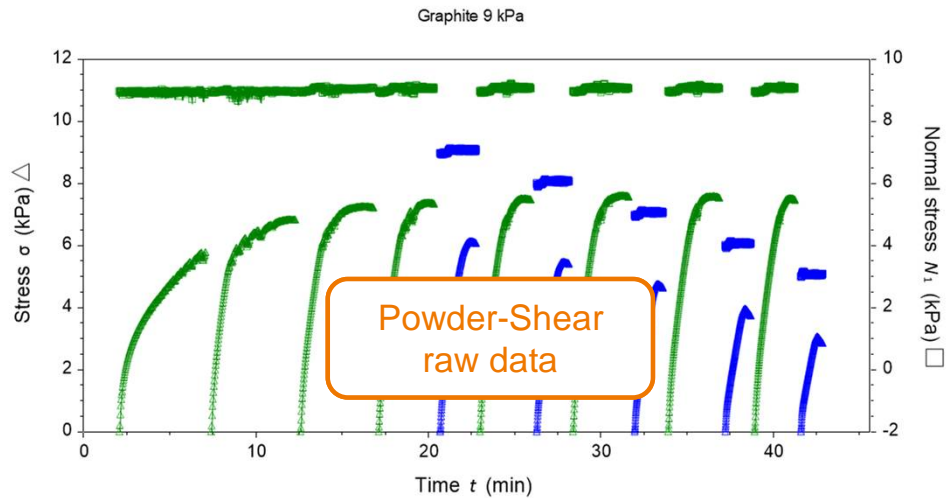
	Normal Stress (kPa)	Velocity (rad/s)	Duration (hh:mm:ss)
Pre-shear	9	1.0e-3	00:05:00
1	7	1.0e-3	00:05:00
2	6	1.0e-3	00:05:00
3	5	1.0e-3	00:05:00
4	4	1.0e-3	00:05:00
5	3	1.0e-3	00:05:00

Repeat initial pre-shear  
 Steady state detection  
 Peak detection

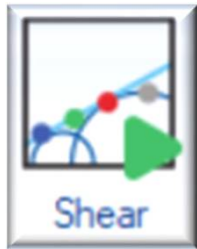


## TRIOS Powder – Shear test form performs measurement per ASTM D7891

- “Pre-Shear”: Apply consolidating normal stress (9 kPa), pre-shear until steady state
- “Shear” Reduce normal stress, shear until yield
- Repeat consolidating pre-shear
- Repeat shear with decreasing normal stress



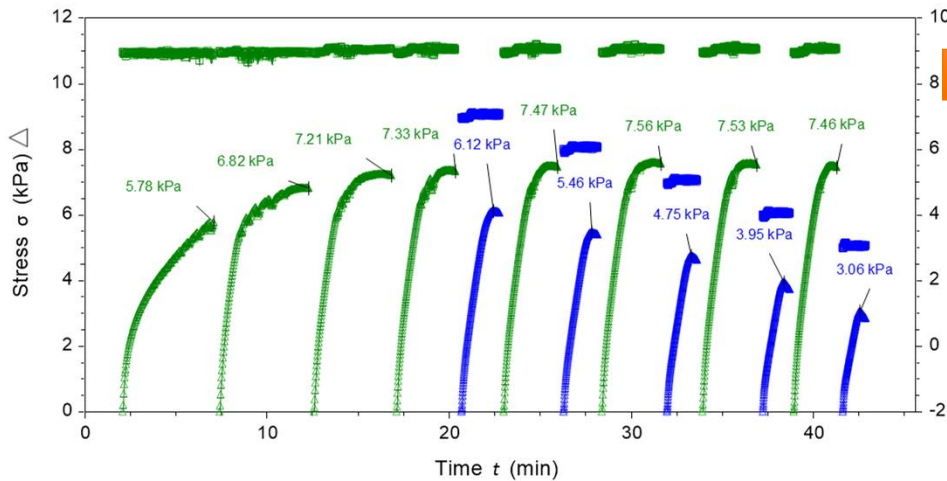
## Powder Analysis Key automates Shear calculations



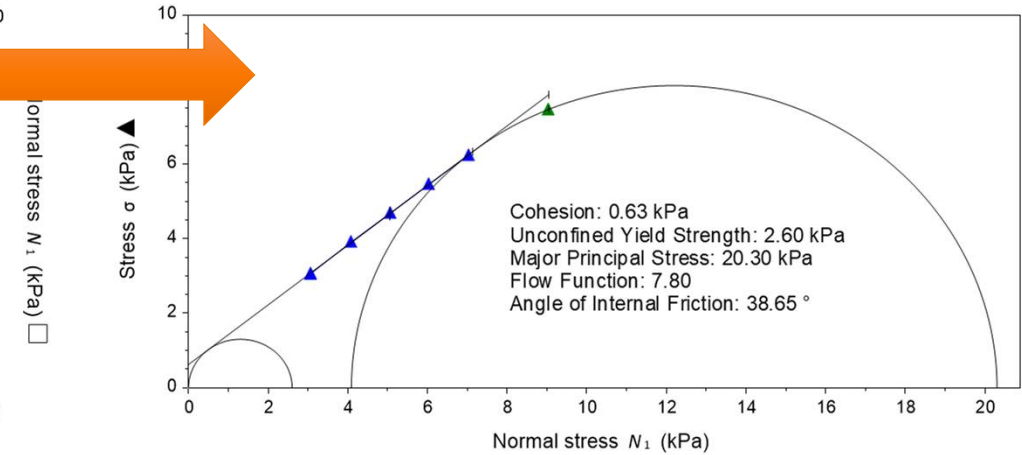
### TRIOS Powder Analysis Software key (optional)

- Powder Key Performance Indicators are **One Click away**
- Automated process saves user from complicated mathematical analysis
- Quantitative, relevant, repeatable results

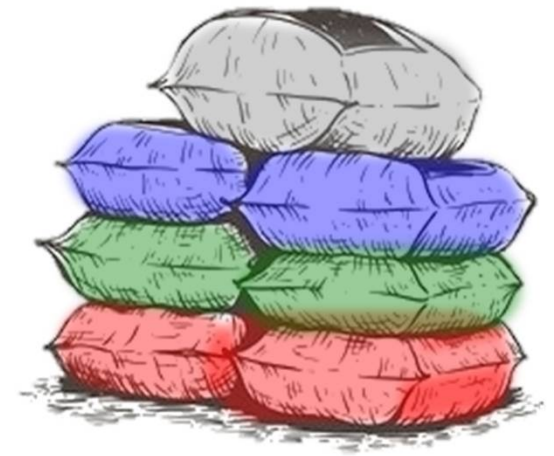
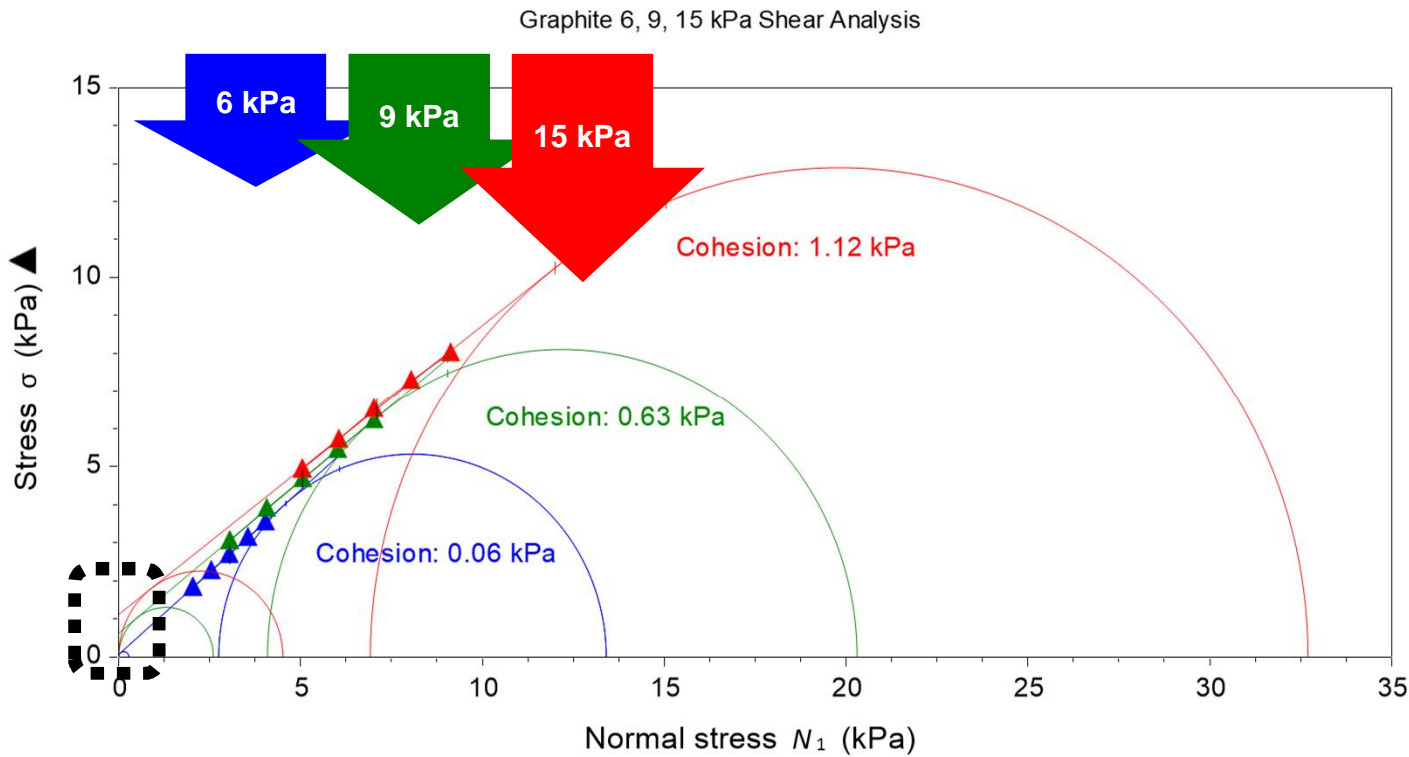
Graphite 9 kPa



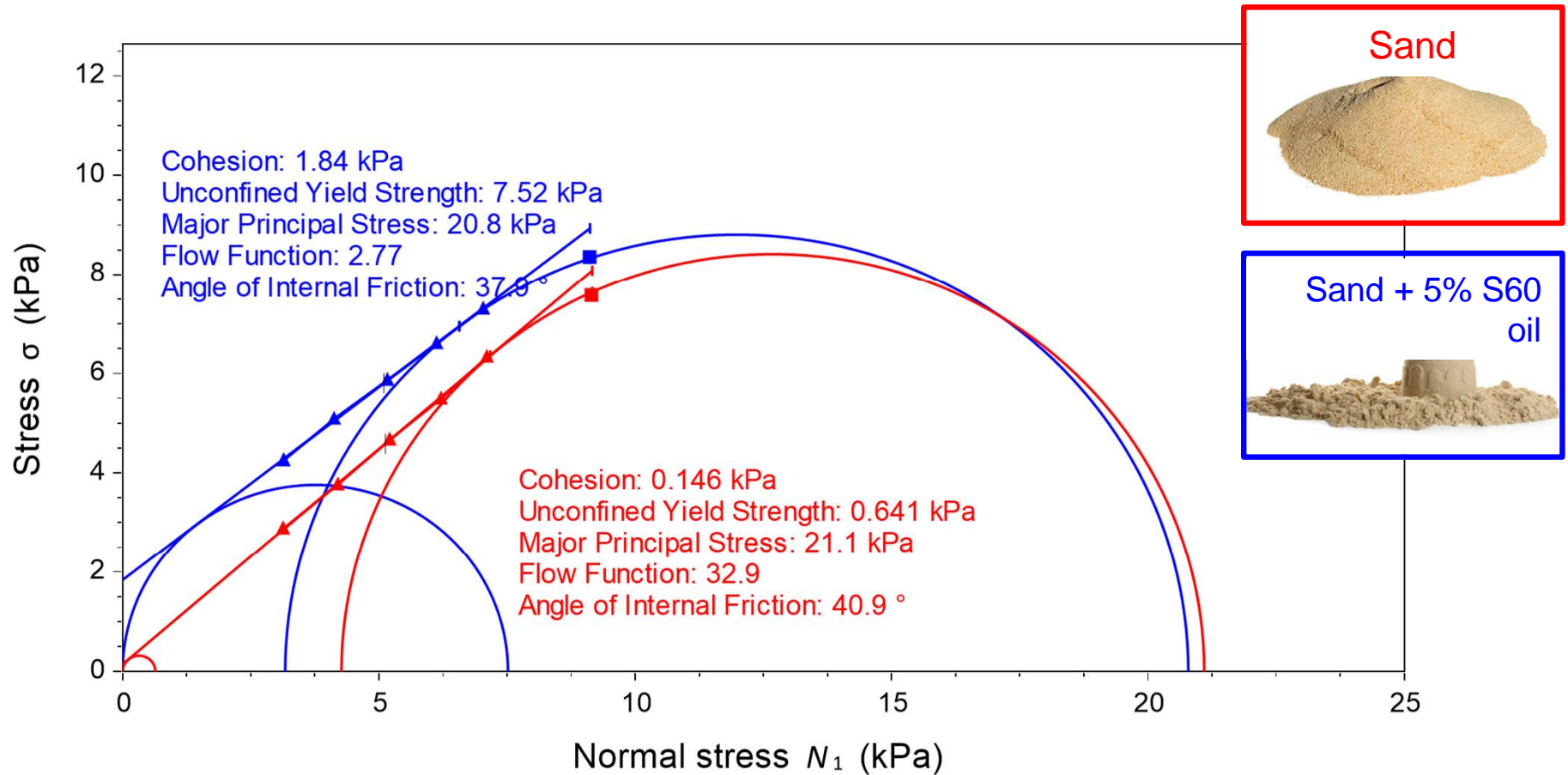
Graphite 9 kPa Shear Analysis



# How do powder properties change with increasing consolidation?



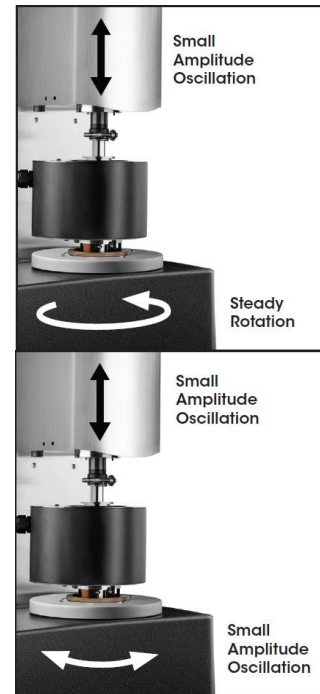
# How do powder properties change with added ingredients?



## OSP Features and Benefits

- Available on both Discovery HR rheometer and ARES G2
- Ensure accuracy in both rotational and axial measurements, avoiding artifacts from pumping effects and surface tension with the specially designed OSP double-gap cup and rotor
- OSP and 2D-SAOS experiments fully programmable from TRIOS Software. Simultaneous measurements in two directions
- Monitor temperature-dependent changes and replicate real-world processing conditions with optional temperature control through the Environmental Test Chamber (-10 °C to 150 °C)

ARES G2 Rheometer



HRx0 Rheometer



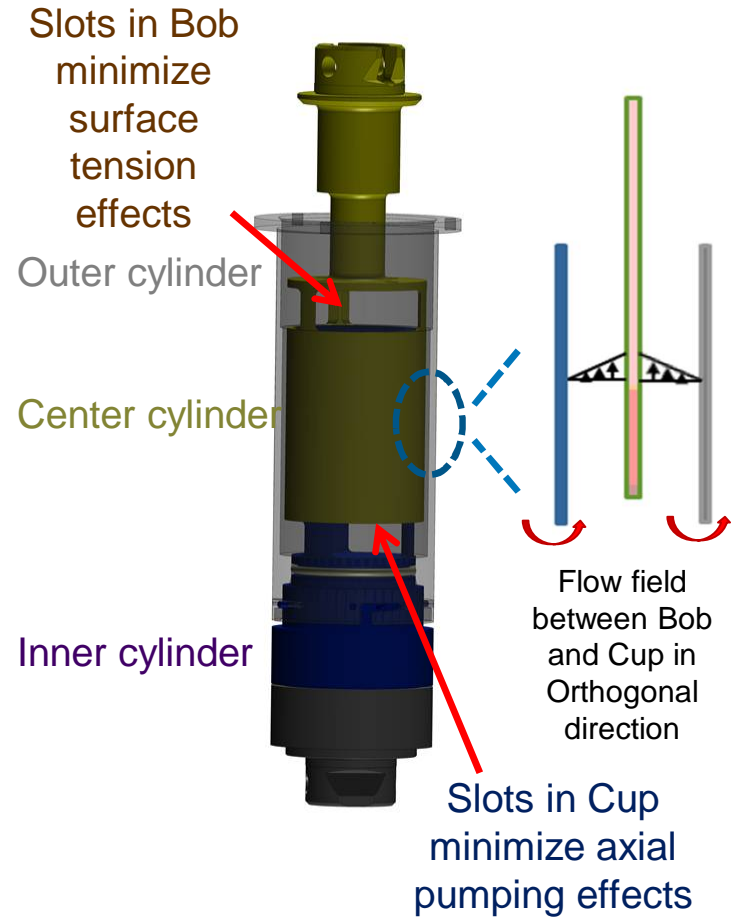
# OSP Geometry



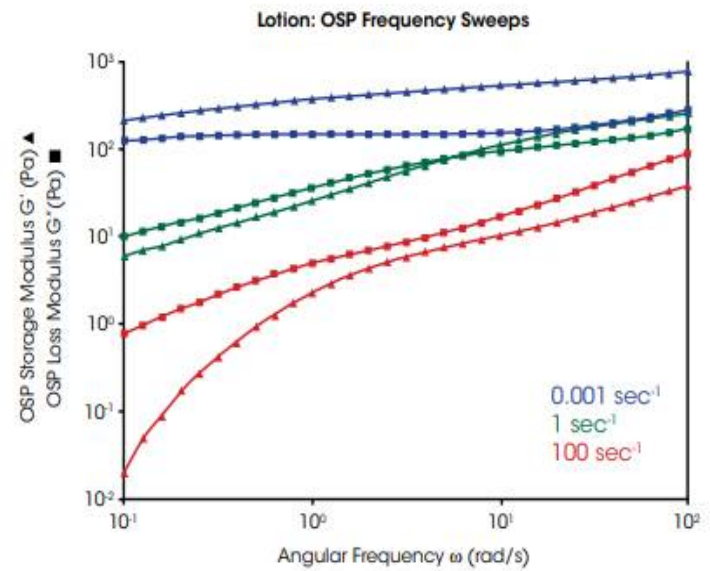
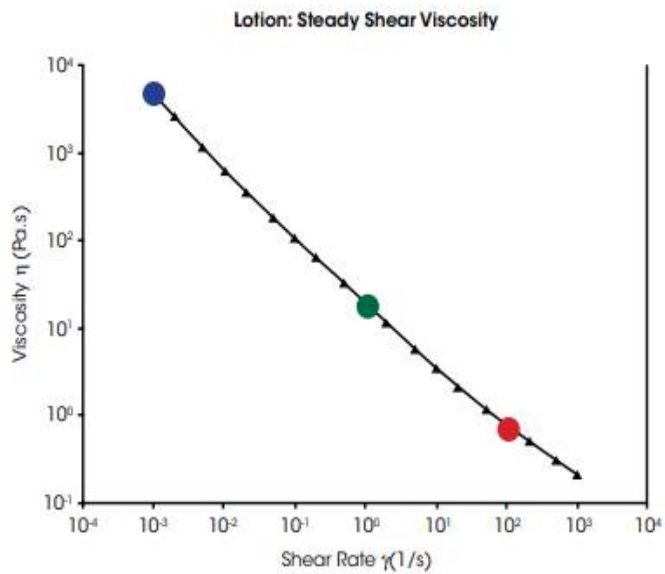
Outer Double Gap Cup

Inner Double Gap Cup with Slots

Bob with Slots



# Example of Orthogonal Superposition analysis on Lotion



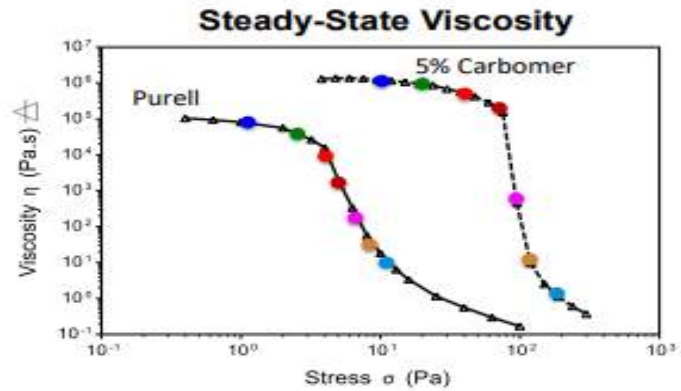


# Change in viscoelasticity during yield

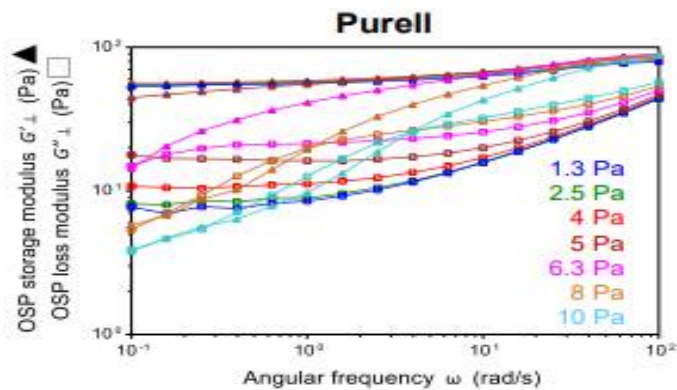
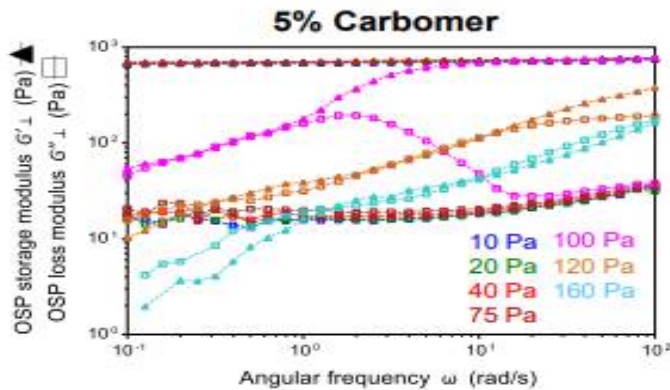
**Materials:** 5% Carbopol 940 NF Purell hand sanitizer

## Shear Rheology:

- Testing Method:
  - Discovery HR-30 rheometer
  - OSP geometry (rotation only)
  - Steady-state flow sweep, stress-controlled
- Both show similar viscosity profile:
  - Plateau decreasing with stress
  - Sharp drop at critical yield stress ( $\sigma_y$ )
  - Newtonian at  $\sigma > \sigma_y$



## OSP Frequency Sweeps under Shear Stress



### Features and Benefits

- Integrated operation with Thermo Fisher™ iXR Raman spectrometer
- Choice of different lasers for maximum versatility
  - 432 nm, 532 nm and 785 nm (high brightness, high power options)
  - User installable laser sets — quick and easy to switch lasers
- Multiple interlocks for class 1 laser classification
- Safe under all conditions of normal use
- Free space coupling maximizes laser intensity at sample
- Software integration provides seamless Rheo-Raman experiments
  - Synchronized data collection between TRIOS and Thermo Scientific™ OMNIC™ software
  - Rheo-Raman data analysis performed in OMNIC software
- Temperature control up to 100 °C using Upper Heated Plate (UHP)
- Optical table provides excellent stability, alignment, and vibration free measurements
- Micrometer driven access to any radial positions
- Fine axial adjustment for focusing inside the sample
- Quartz plates minimize fluorescence artefacts



## Rheo-optics system: Modular Microscope Accessory (MMA)

- Available on Discovery HR rheometers.
- Compact, modular design, that mounts on instrument frame for easy alignment and minimum vibration
- Uses standard Nikon microscopy objectives. Tested with 20x to 100x.
- Fast speed camera for image capture up to 90 fps
- X-Y-Z micrometer stage controls to select observation position
- Brightfield microscopy with cross-polarization
- Modular Options:
  - Counter-rotating plate for zero-velocity stagnation plane
  - Piezo-scanning stage for 100  $\mu\text{m}$  depth profiling
  - Dichroic splitter for fluorescence microscopy
  - UHP for temperature control up to 100°C



# Simultaneous Rheology-Dielectric Measurement

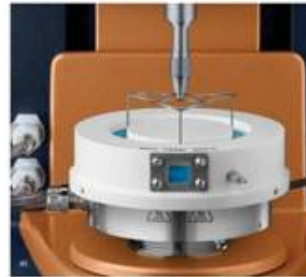


Agilent E4980A LCR meter

Grounded Geometries with Ceramic Insulator (standard or disposable)



Small Angle Light



Interfacial Accessory



Magneto-Rheology



Electro-Rheology



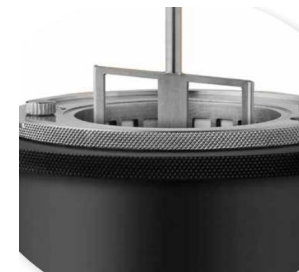
Pressure Cell



Starch Pasting Cell



Immobilization Cell



Building material cell

# Thank You!